

# Privacy in Pharmacogenetics: An End-to-End Case Study of Personalized Warfarin Dosing

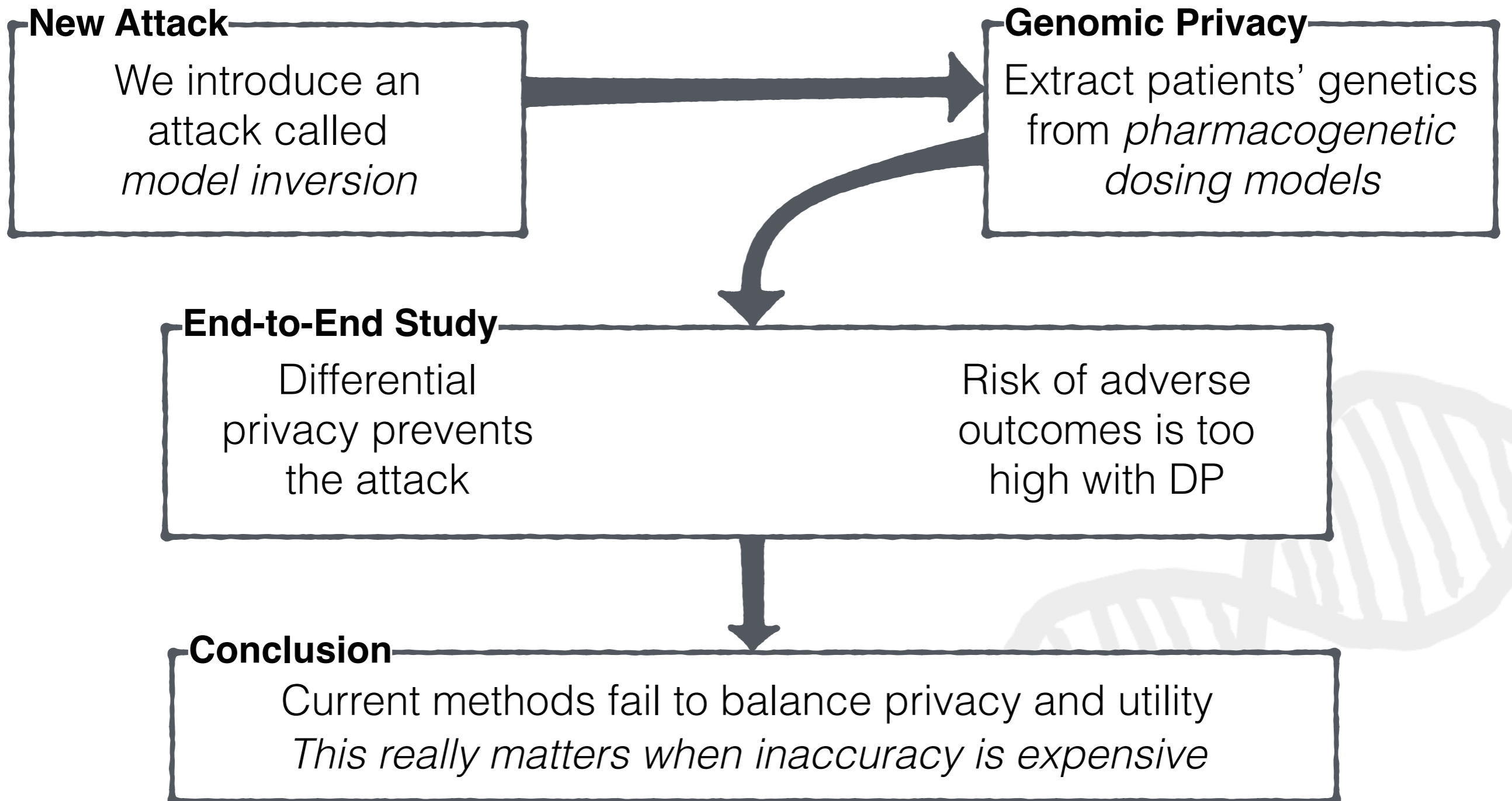
Matthew Fredrikson, Eric Lantz,  
Somesh Jha, David Page, Thomas Ristenpart

University of Wisconsin — Madison

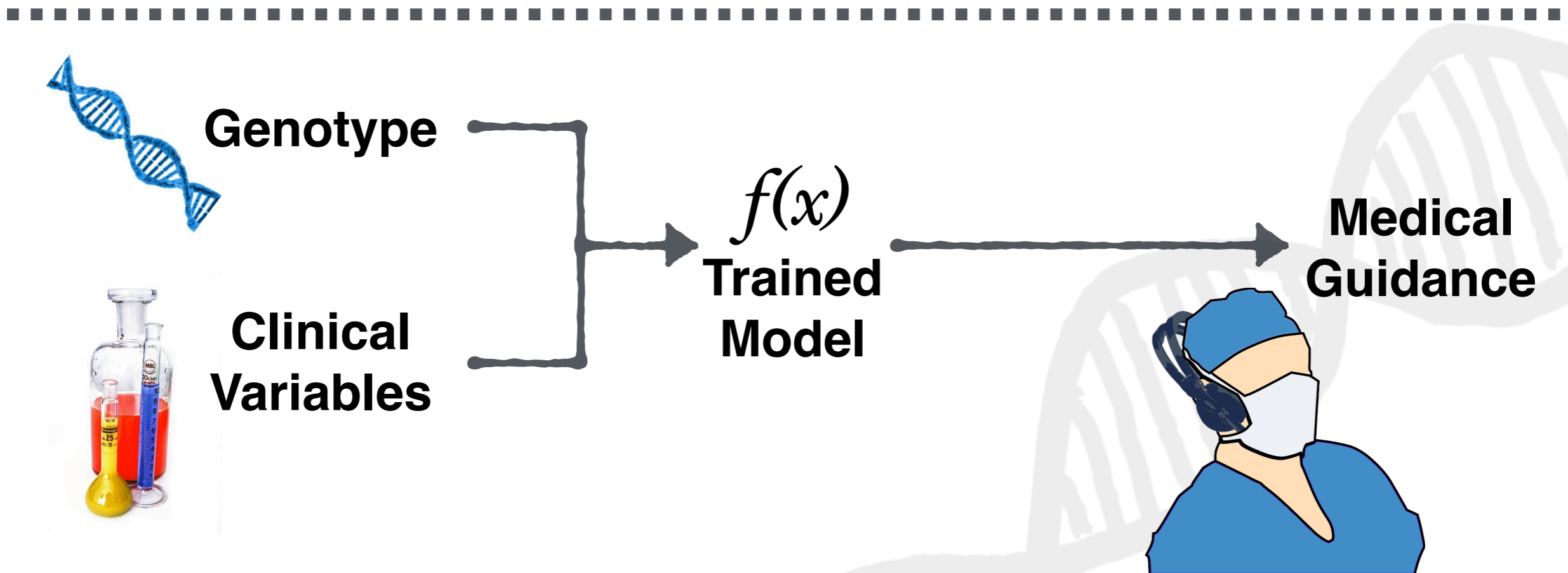
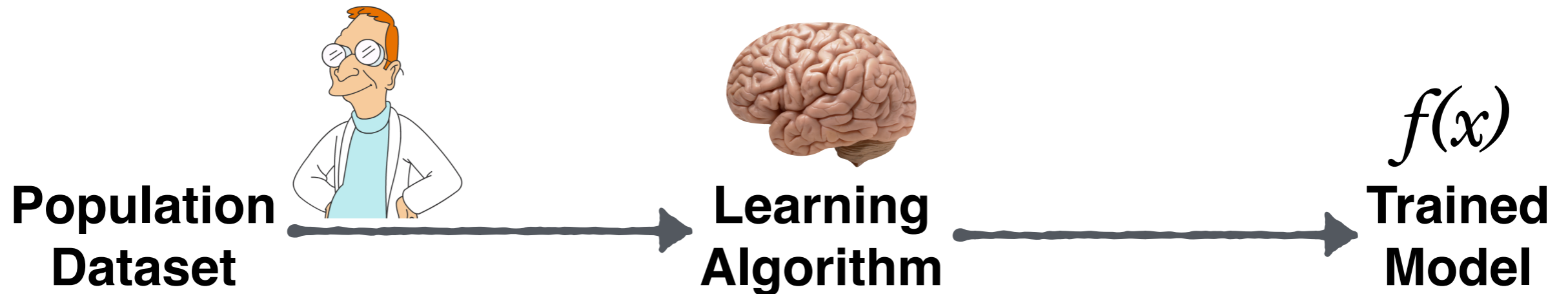
Simon Lin, M.D.

Marshfield Clinic

# This Talk



# Pharmacogenetics

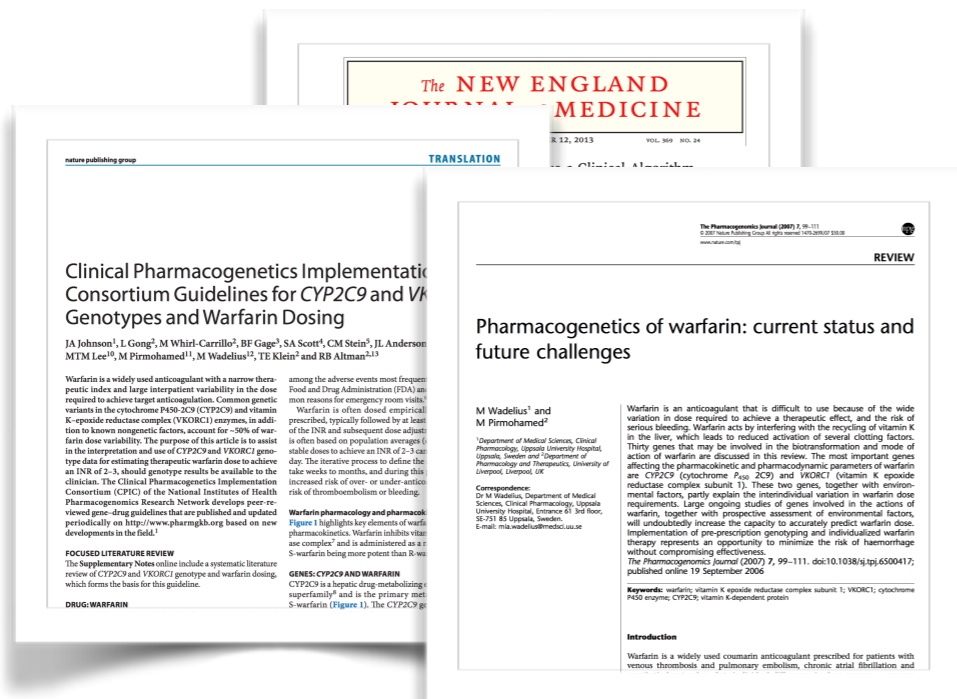


# Warfarin Dosing

Warfarin is the most popular anticoagulant in use today

Anticoagulants are used to prevent stroke and clotting-related incidents

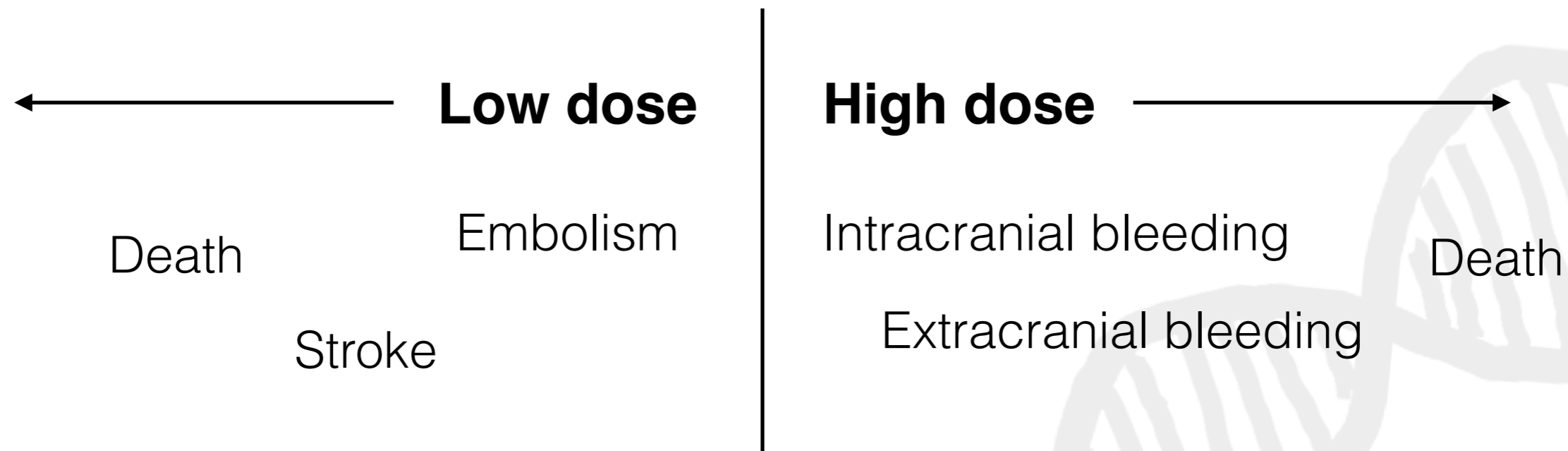
Warfarin is one of the most well-studied targets in pharmacogenetics



100+ articles to date

# The dangers of being wrong

**Warfarin is notoriously difficult to dose correctly**



# KING KONG RAT KILLER

RACUN  
TIKUS

殺鼠藥



UMPAK BERBUNGKAH (BB)

**BACA LABEL SEBELUM GUNA**

Kandungan Bersih : 180 g

No. Pendaftaran. LRMP. R1/0020

Perawis Aktif: warfarin .....	0.05%	w/w
Perawis Lengai: .....	99.95%	w/w

Didaftarkan oleh:

TOHTONKU SDN. BHD.

186, Jalan Burma, (38311-A)

10350 Pulau Pinang.

Tel: 04-2287161

Jika berlaku **KERACUNAN**, sila hubungi: **PUSAT RACUN NEGARA**  
-1-800-88-8099 (waktu pejabat) -012-4309499 (lepas waktu pejabat)

JAUHKAN DARIPADA  
MAKANAN  
DAN KANAK-KANAK

**KELAS IV**

勿貯藏在靠近  
食品或兒童  
所接觸的地方

ERANGGA  
OL (AE)

LRMP. R1/8012  
450 g (600 ml)  
SEBELUM GUNA

Delthrin (75/25) ....	0.11%	w/w
.....	0.07%	w/w
.....	99.82%	w/w

(M) Sdn. Bhd. (Co. No. 175141-H)  
Jalan PJJU 7/5, Mutiara Damansara,  
Jaya, Selangor.  
Faks: 03-7719 1195

LAS IV

勿貯藏在靠近  
食品或兒童  
所接觸的地方

KEEP AWAY  
FOODS  
CHILDREN

# The IWPC Warfarin Model

Population  
Dataset



Learning  
Algorithm



Trained  
Model



**5700 patients from  
21 sites in 6 countries, 4 continents**

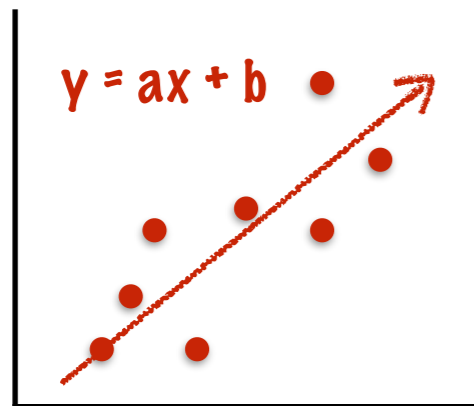


# The IWPC Warfarin Model



age	height	weight	race	history	vkorc1	cyp2c9	dose
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independent variables: patient demographics, physical characteristics, comorbidities, and drug interactions  
dependent variable: Warfarin dose



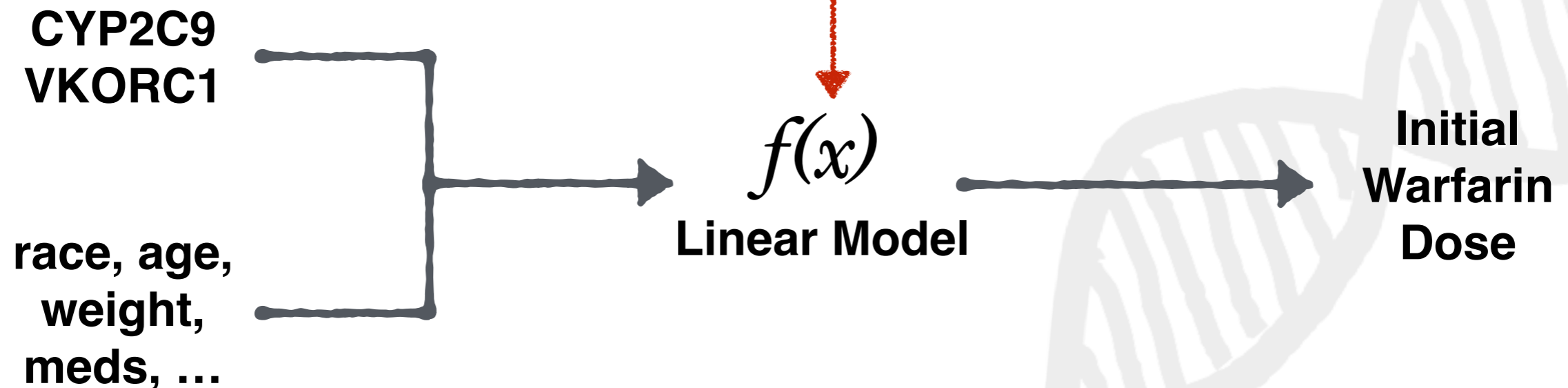
The IWPC found ordinary linear regression to be the best learning algorithm



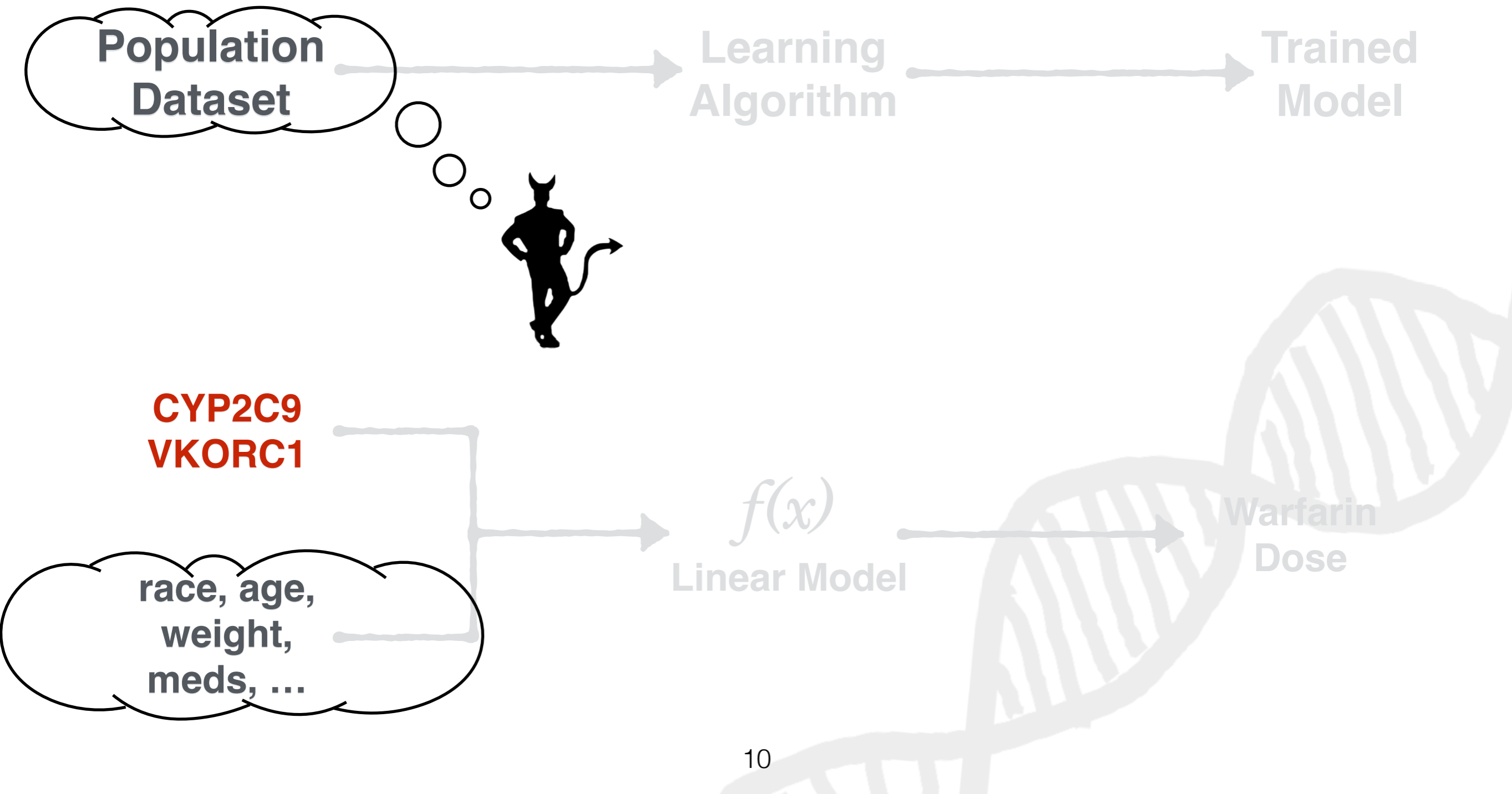
# Pharmacogenetic Warfarin Dosing



$$\sqrt{\text{dose}} = 5.6044 + 0.2614 * \text{age} + 0.1092 * \text{asian race} - 0.2760 * \text{black or african american} - 0.8677 * \text{vkorc1=A/G} - 1.6974 * \text{vkorc1=A/A} - 1.9206 * \text{cyp2c9=*2/*3} - 2.3312 * \text{cyp2c9=*3/*3} + \dots$$

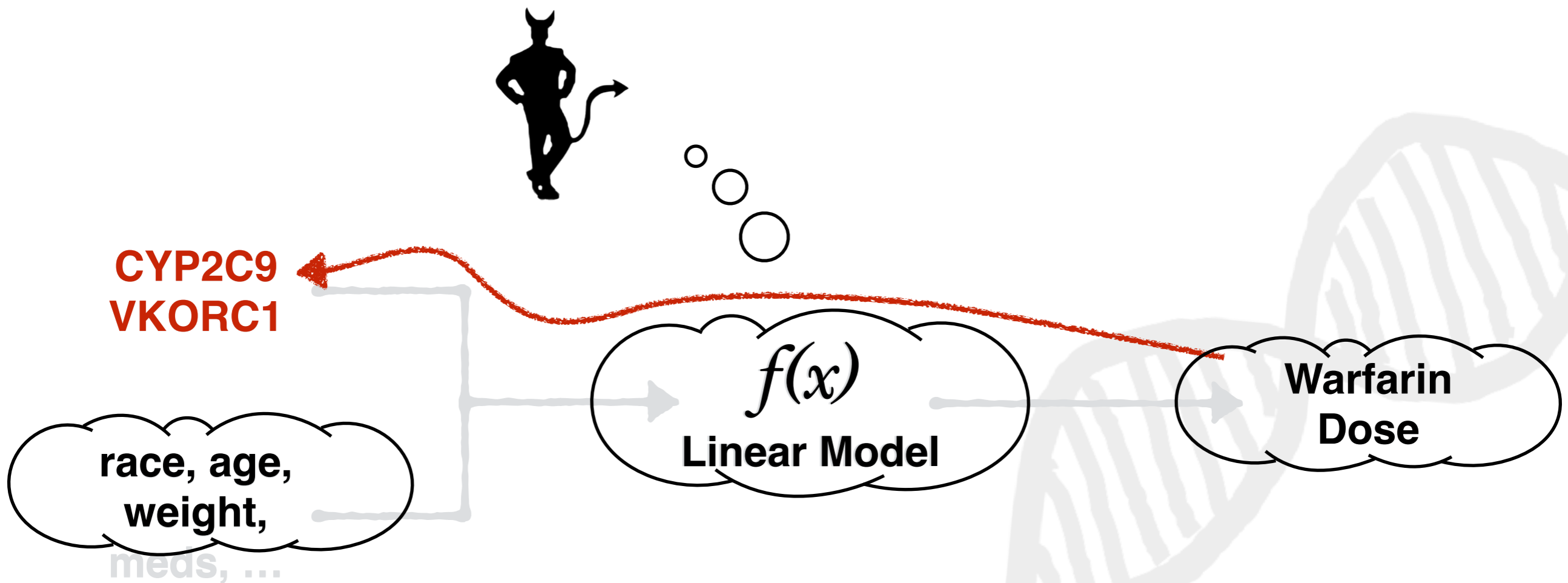


# Pharmacogenetic Privacy



# Pharmacogenetic Privacy

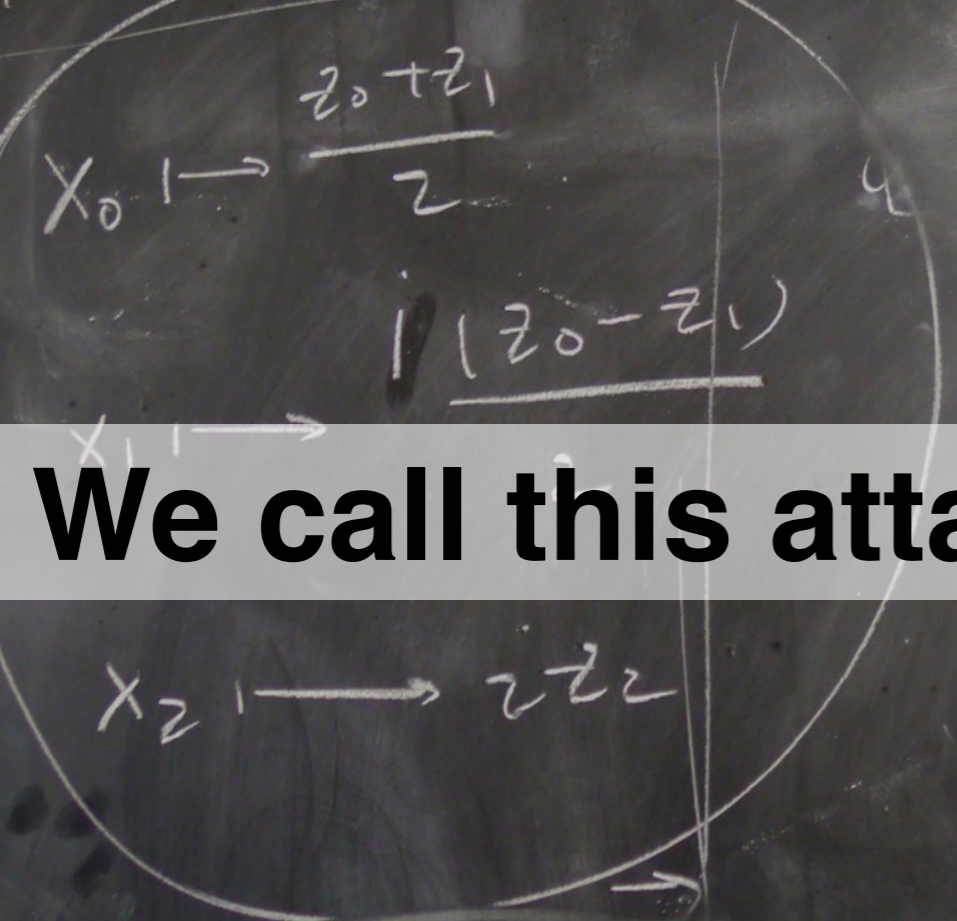
age	height	weight	race	history	vkorc1	cyp2c9	dose
50-60	176.2	185.7	asian	cancer	A/G	*1/*3	42.0



$\sqrt{(x_0^2 + x_1^2 + x_2^2)}$   $\mathbb{P}^2$   
 $x_0^2 + x_1^2 + x_2^2 = 0$   
 Is this a trivial Fibration Mukai?  
 ask Ramadoss  
 $V = V(x_0^2 + x_1^2 + x_2^2) \subseteq \mathbb{P}^2$   
 $\langle 0, 0, 1 \rangle$

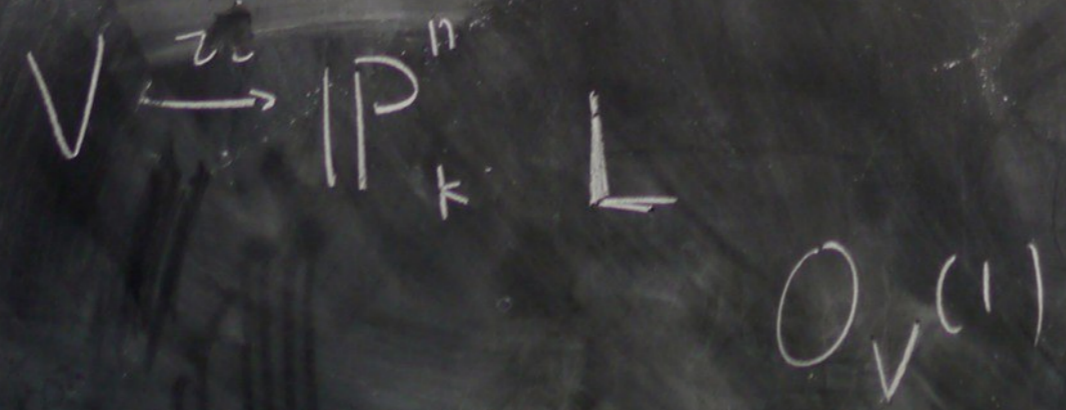
**We call this attack *model inversion***

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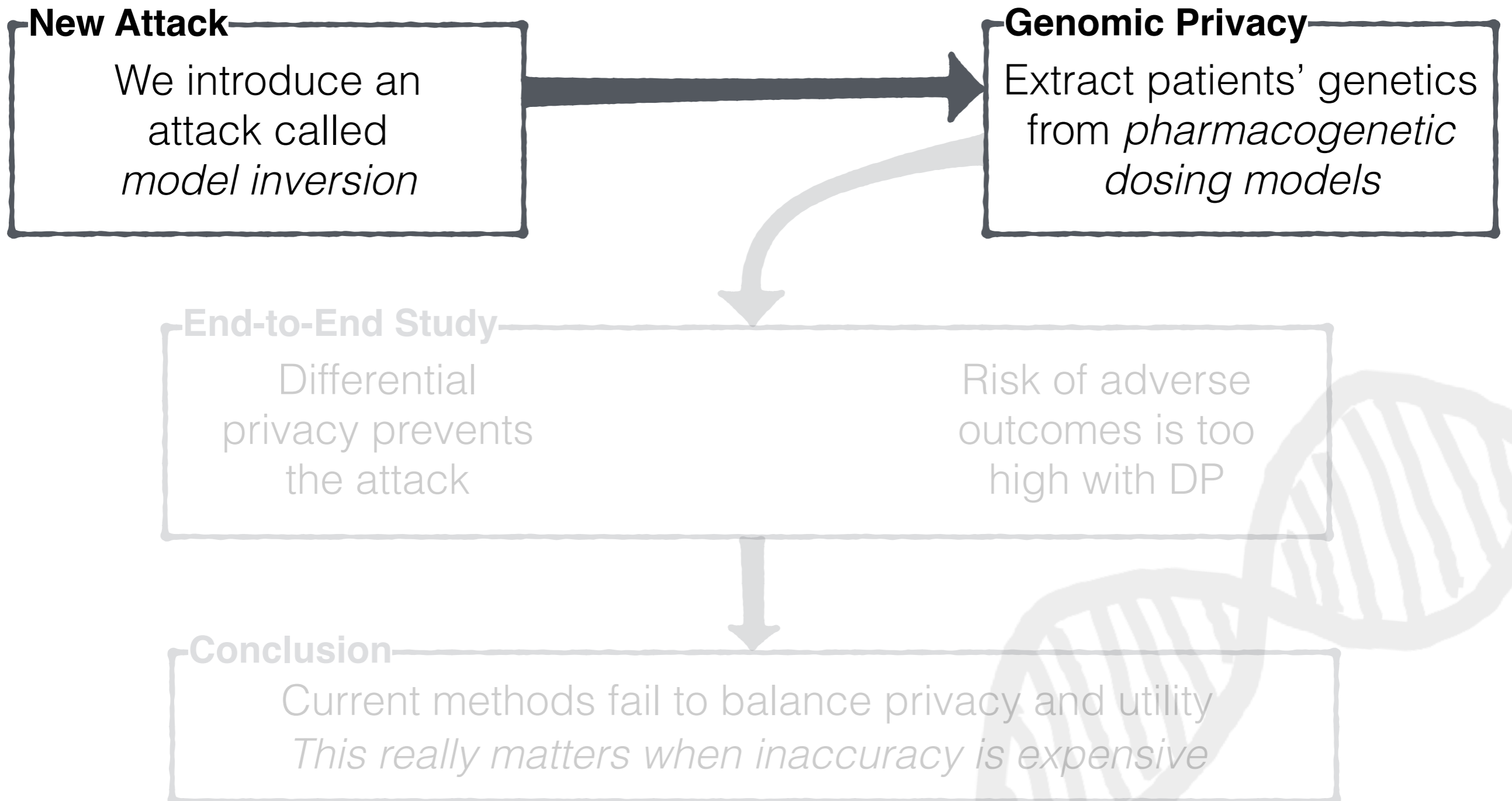


$\text{Coh}(V) \cong \text{Coh}(\mathbb{P}^2)$

$\frac{k[x_0, x_1, x_2]}{(x_0^2 + x_1^2 + x_2^2)} \cong \bigoplus_{i \geq 0} \text{Hom}(O, O(i))$



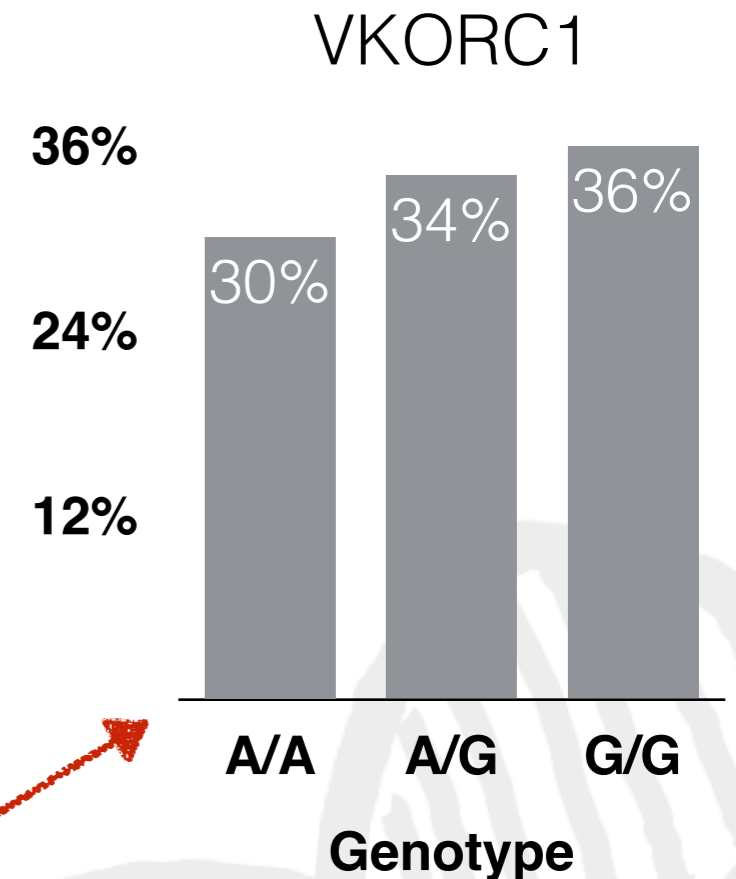
# This Talk



# Model Inversion



basic demographics  
stable warfarin dose  
black-box access to model  
marginal priors on patient distribution



... with better accuracy than the given "baseline" priors

**Goal: infer the patient's genetic markers from this information**

# Our Model Inversion

## 1. Compute all values that agree with given information

$f(x)$

age	height	weight	race	history	vkorc1	cyp2c9	dose
50-59	176.53	144.2	white				42.0
50-59	176.53	144.2	white				42.0
50-59	176.53	144.2	white				42.0

49.7	$p=0.23$
42.0	$p=0.75$
39.2	$p=0.01$

## 2. Find the most likely values among those that remain

Use the marginal probabilities, model output to approximate this quantity



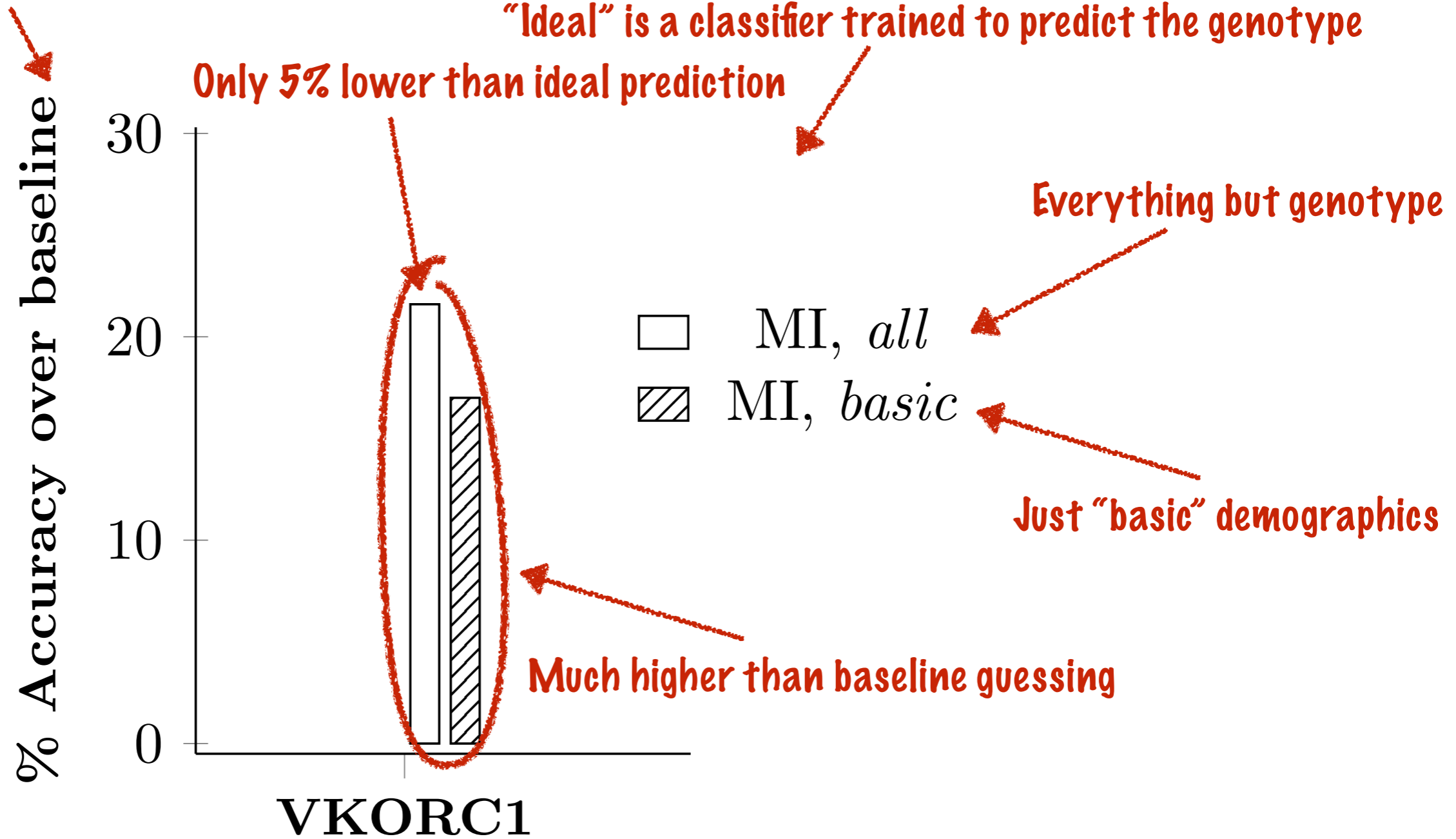
**This algorithm is optimal given the available information**



# Results

“baseline” means guessing without the model

“Ideal” is a classifier trained to predict the genotype



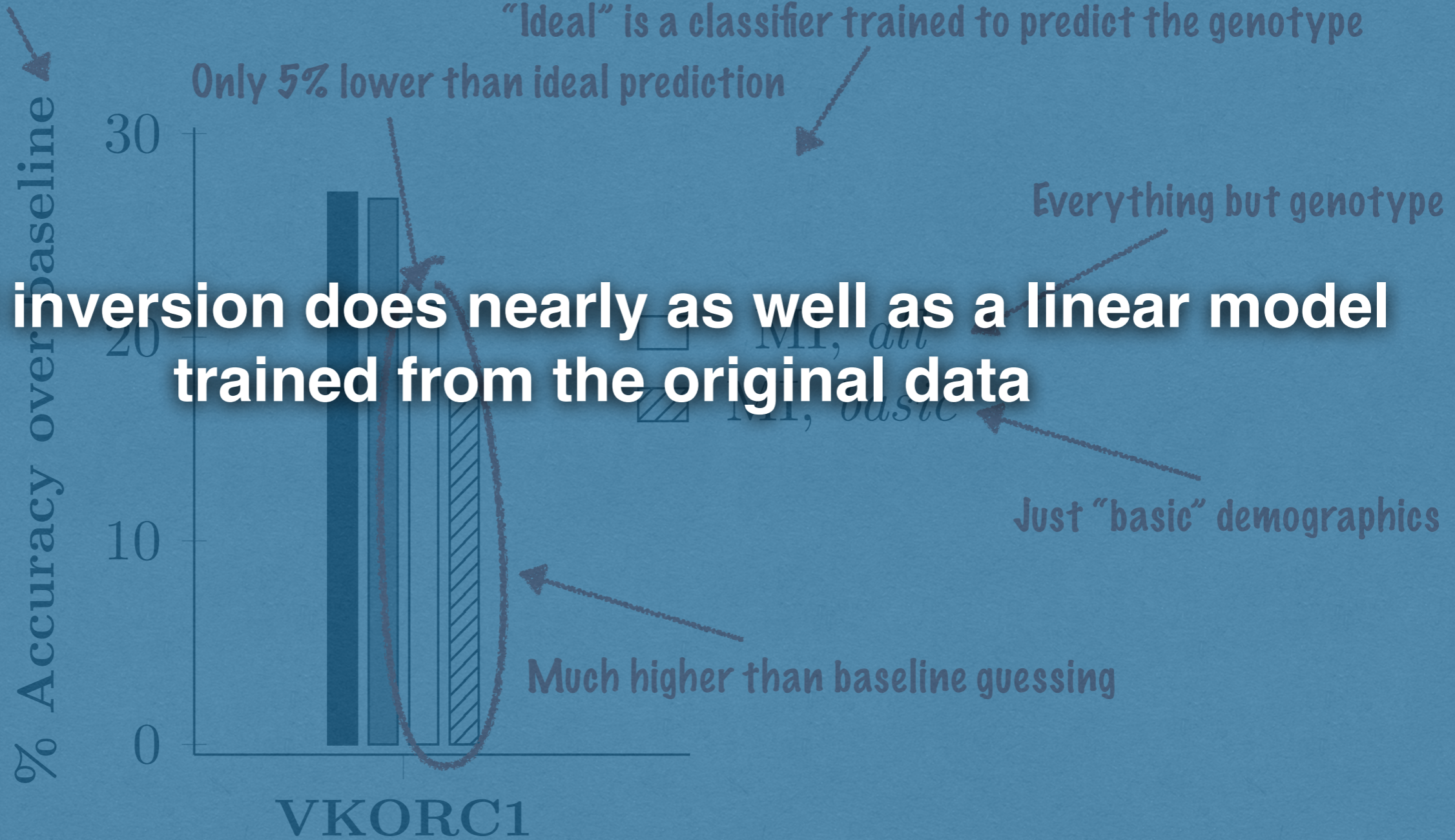
# Results

"baseline" means guessing without the model

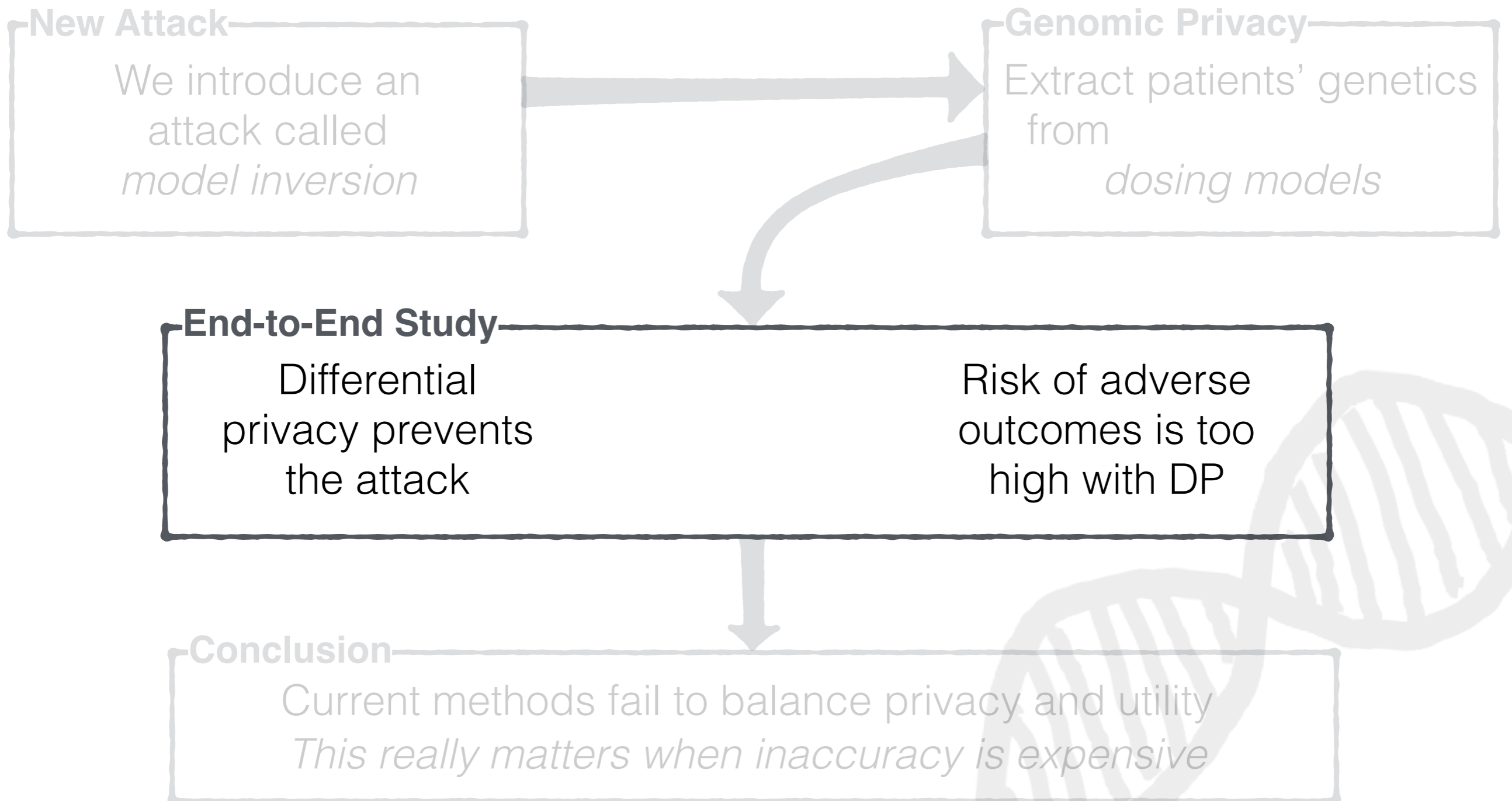
"Ideal" is a classifier trained to predict the genotype

Only 5% lower than ideal prediction

**Model inversion does nearly as well as a linear model trained from the original data**



# This Talk



# Seeking a Remedy

MI is a problem, so how can we prevent it?

We examine the use of differential privacy for preventing MI

For  $D, D'$  differing in one row  
*Any output should be about as likely  
regardless of whether or not I am in the dataset*  
 $\Pr[R(D) = s] \leq \exp(\epsilon) \times \Pr[R(D') = s]$

Clean, provable guarantee

Most DP mechanisms “add noise” according to privacy budget

Evidence that this protects attributes in linear models  
(Kasiviswanathan et al., SODA 2013)

# Seeking a Remedy

**Goal: see if a “reasonable” privacy budget solves the problem**

## End-to-End Study

Find budget that prevents model inversion

Evaluate risk of adverse events at these budgets

## Private Linear Regression

[Zhang et al., VLDB 2012]

## Private Histograms

[Vinterbo, ECML-PKDD 2012]

Run model inversion experiments from before on DP models

# Clinical Efficacy

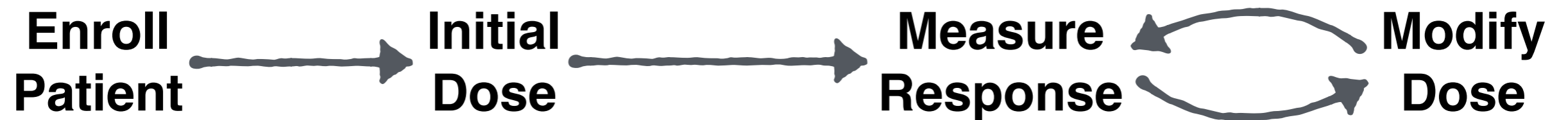
## End-to-End Study

Find budget that prevents model inversion

Evaluate risk of adverse events at these budgets

**Simulate clinical trials to make this calculation**

# Simulated Clinical Trials



Day 1

Days 1-2

Days 2-90

Days 3-90

Sample patient from  
IWPC validation set

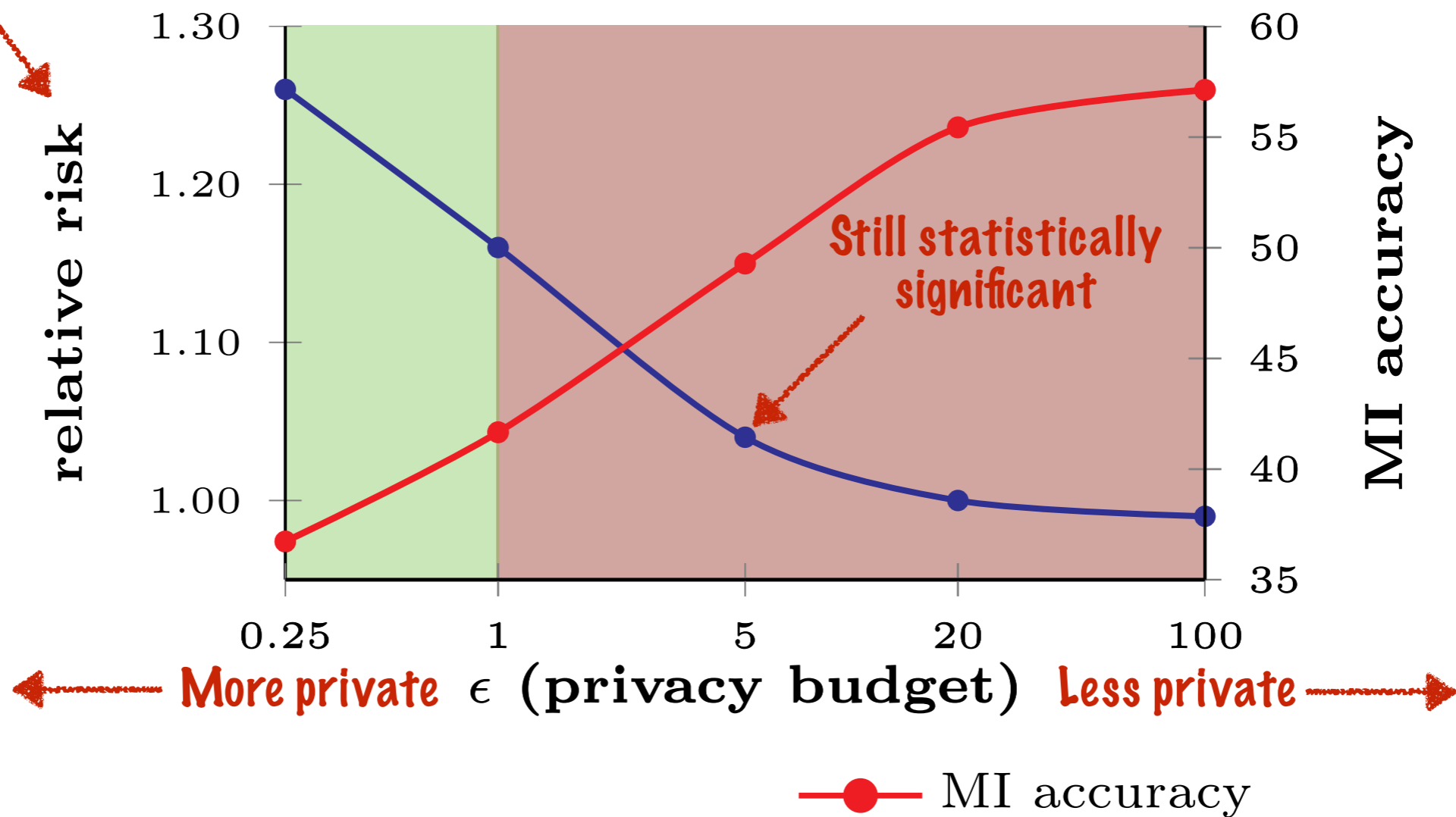
standard fixed dose  
private model

Simulate body's response  
using PK/PD models  
(Hamberg et al., Clin. Pharm.  
Theory, 2007)

Defined in previous  
clinical trials

Relative to fixed-dose protocol

### End-to-End Results, Private LR





**We did not observe a budget that significantly prevented model inversion, without introducing risk over fixed dosing.**

ATTACH TO TOE

NO. 666

NAME OF DECEASED  
Rygnor

CAUSE OF DEATH  
Sudden Coronary

PLACE OF DEATH  
Deceleration Trauma

DATE OF DEATH  
OCT 19 2012

PHYSICIAN(S)  
Boek, Maine

TIME OF DEATH  
22:43

COMMENTS  
Case No. 1138

OFFICE OF THE CORONER

# Thanks!

