

Karma: Resource Allocation for Dynamic Demands



Midhul Vuppalapati



Giannis Fikioris



Rachit Agarwal



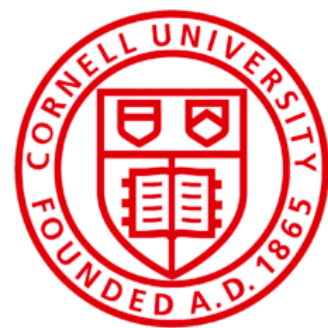
Asaf Cidon



Anurag Khandelwal



Éva Tardos



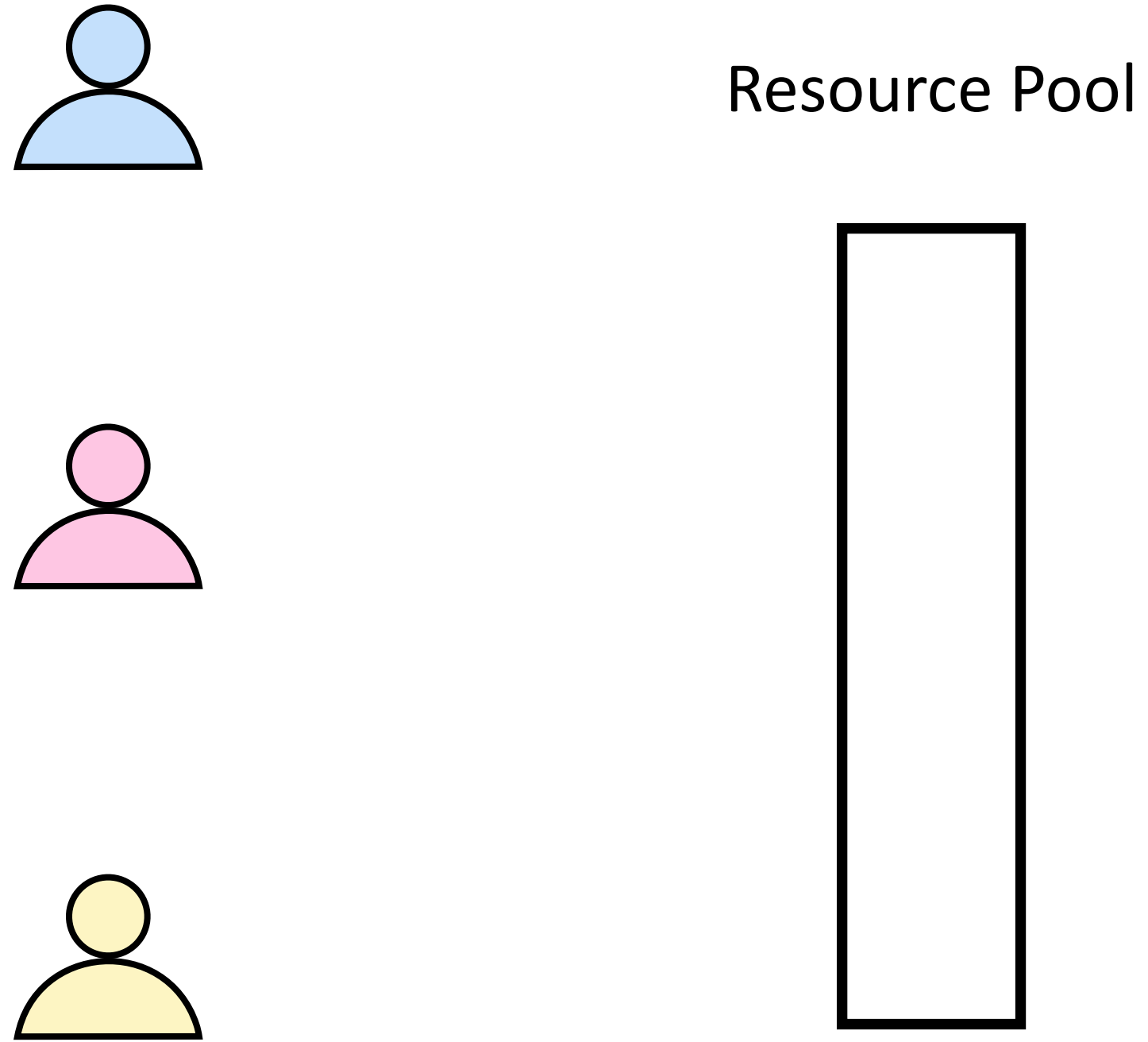
Cornell University



Yale University

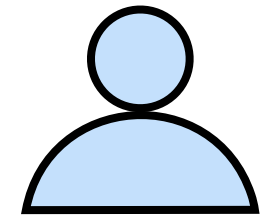
Resource allocation is a fundamental problem

Allocating a resource (e.g. CPU, Memory) with a fixed capacity across multiple users

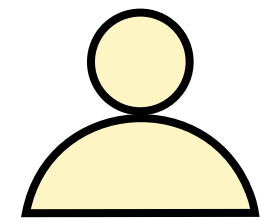
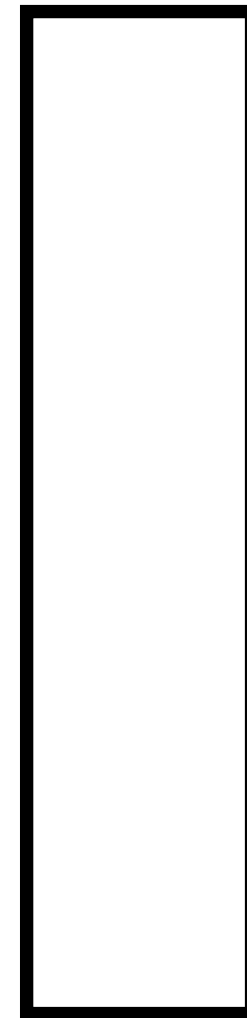
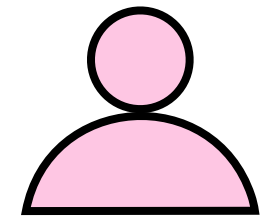


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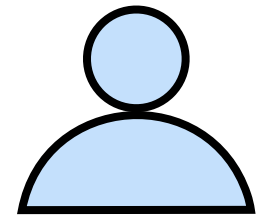
Resource Pool



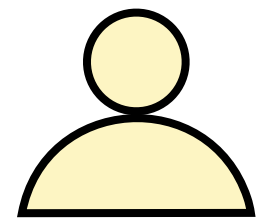
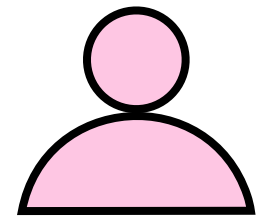
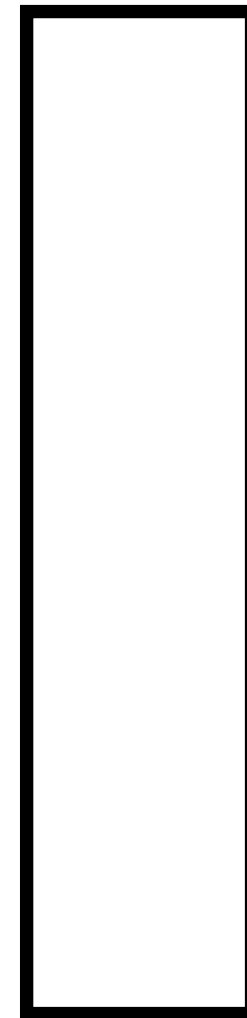
Key Desirable Properties

Resource allocation is a fundamental problem

Allocating a resource (e.g. CPU, Memory) with a fixed capacity across multiple users



Resource Pool



Key Desirable Properties

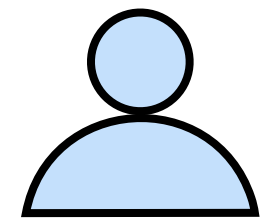


Pareto efficiency

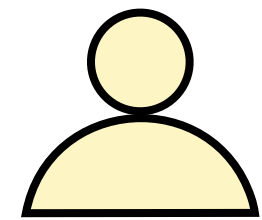
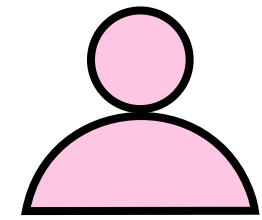
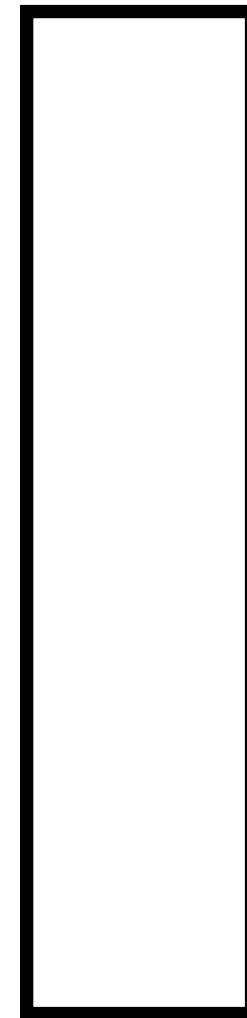
Resources should not remain unused if there is demand

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Resource Pool

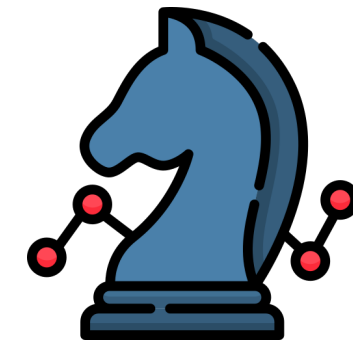


Key Desirable Properties



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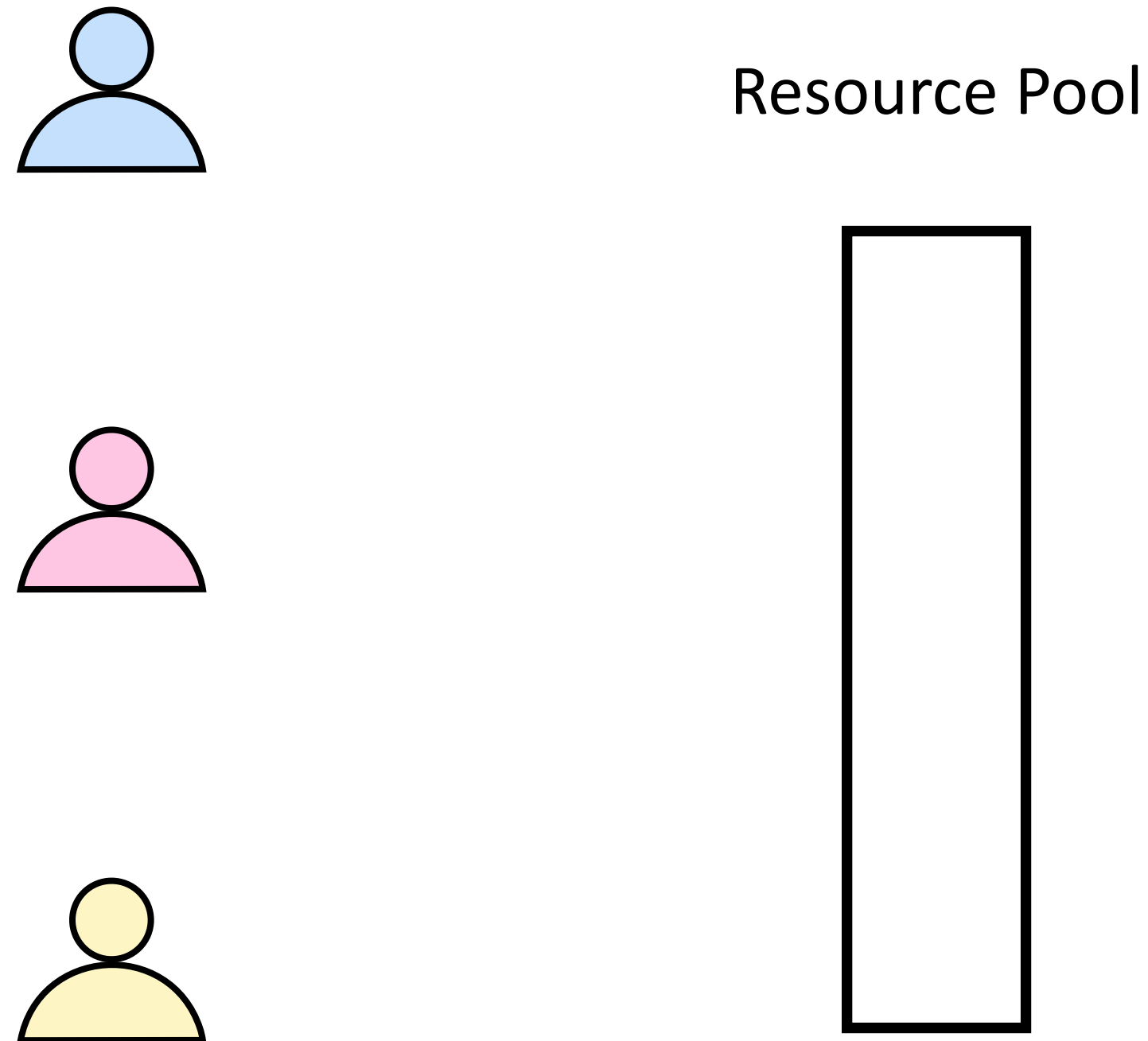


Strategy-proofness

Selfish users cannot increase their allocation by lying
(selfish \neq adversarial)

Resource allocation is a fundamental problem

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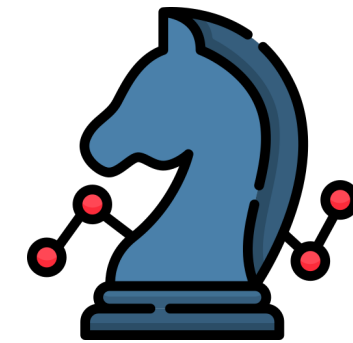


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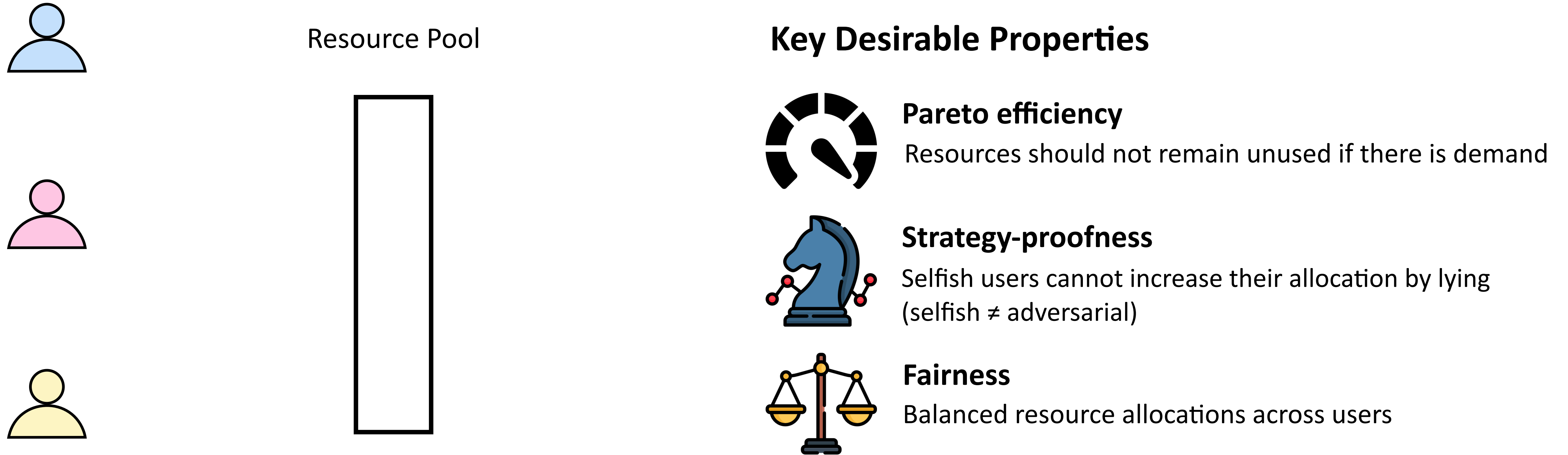


Fairness

Balanced resource allocations across users

Resource allocation is a fundamental problem

Allocating a resource (e.g. CPU, Memory) with a fixed capacity across multiple users

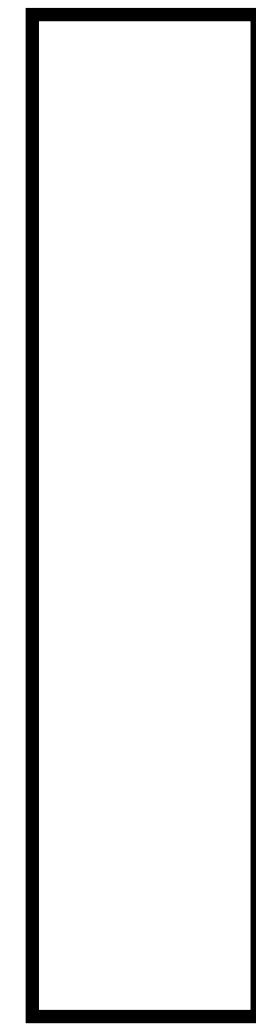
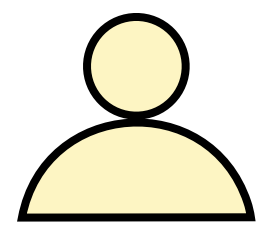
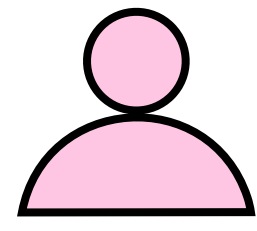
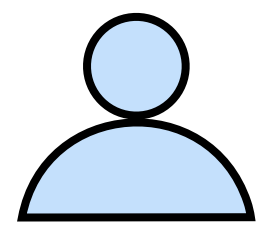


**Two popular resource allocation mechanisms (for single resource type):
strict partitioning and max-min fairness**

Strict partitioning

Allocating the resource equally across all users (“fair share”) **independent of their demands**

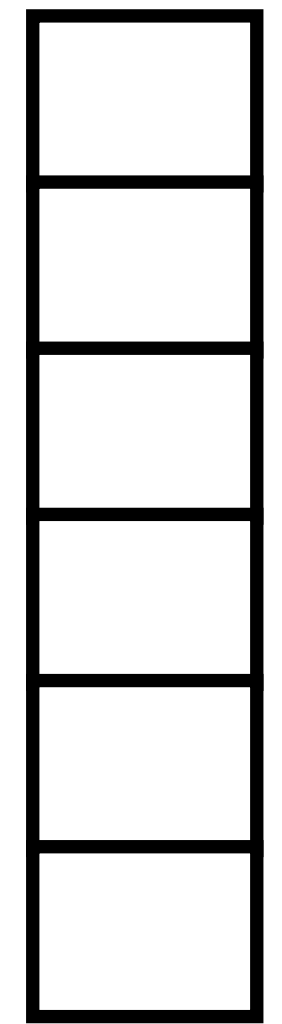
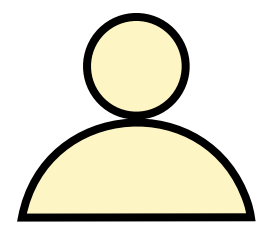
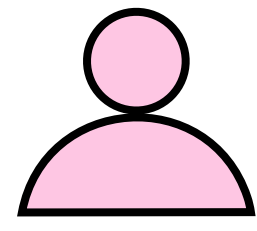
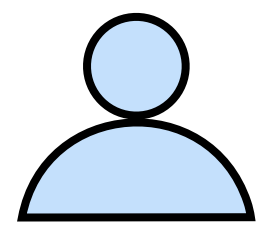
Resource Pool



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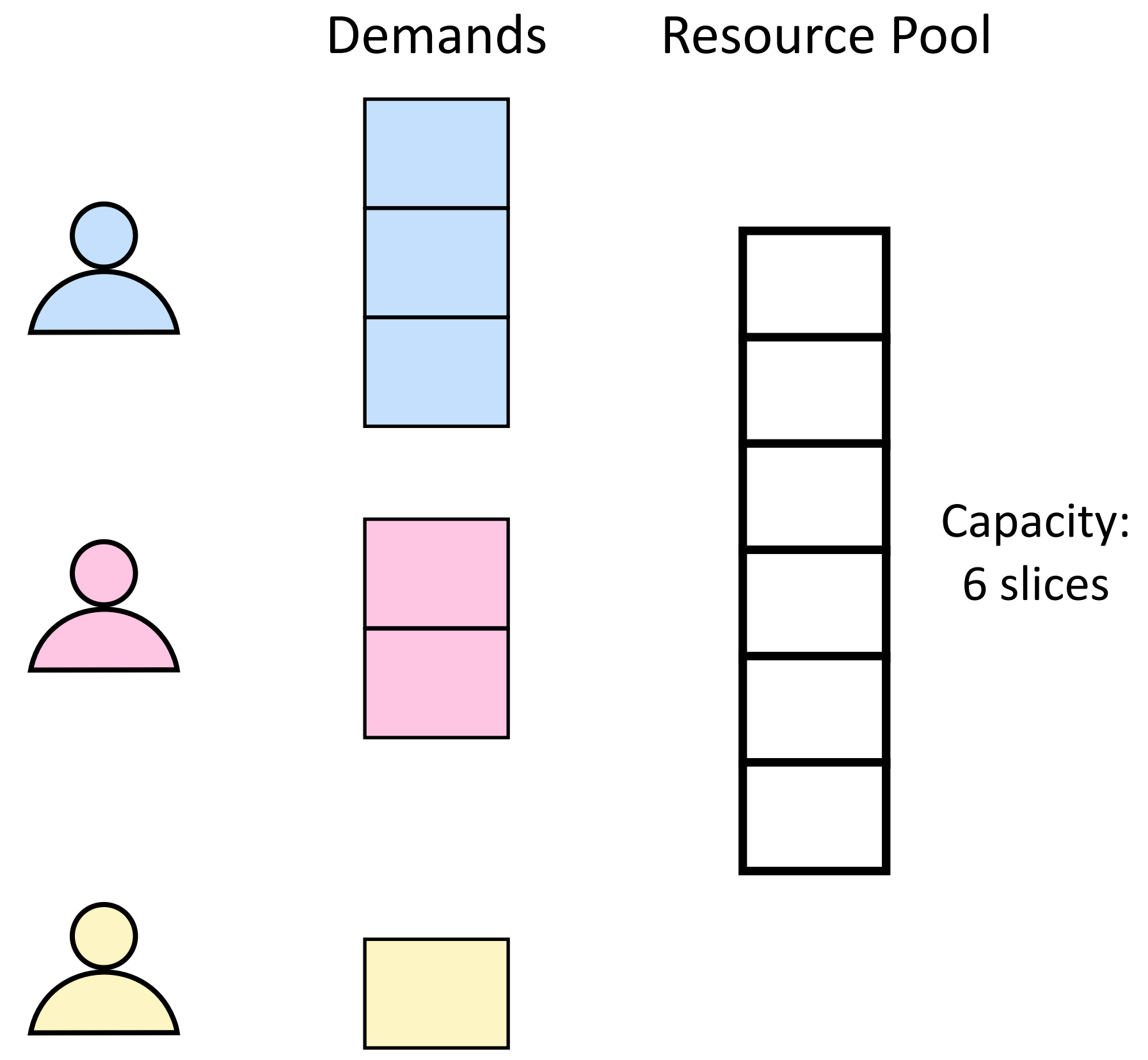
Resource Pool



Capacity:
6 slices

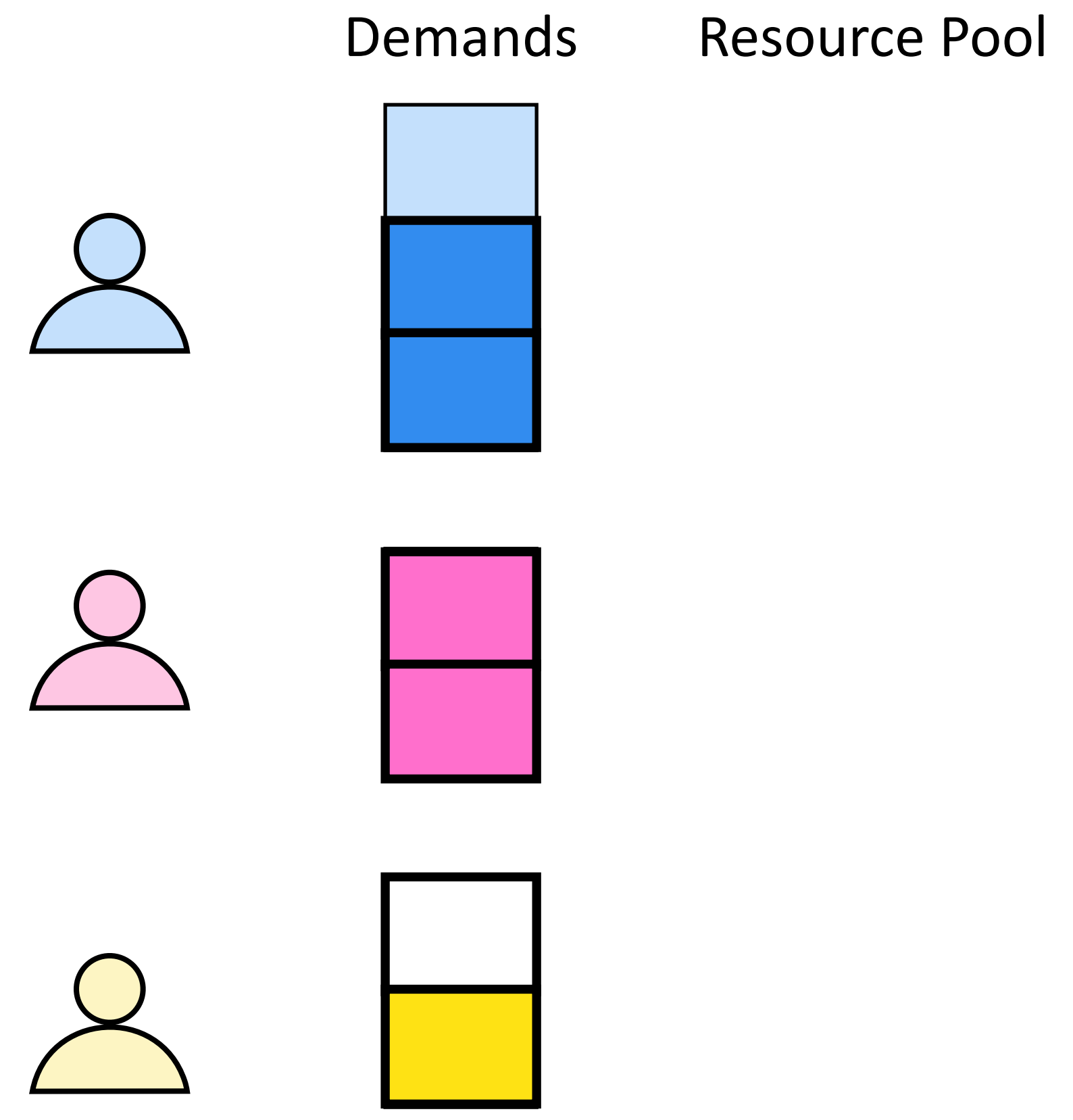
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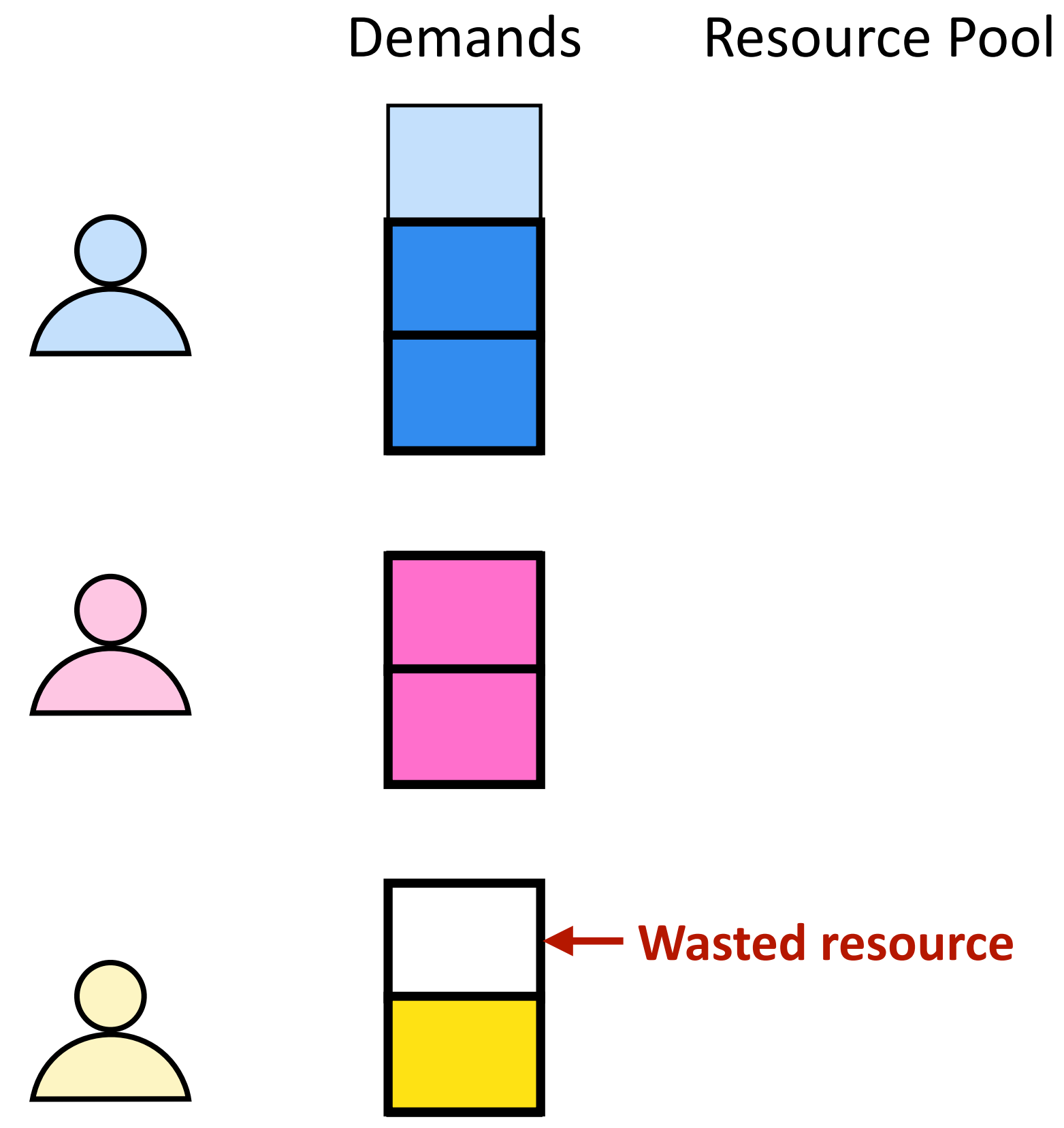
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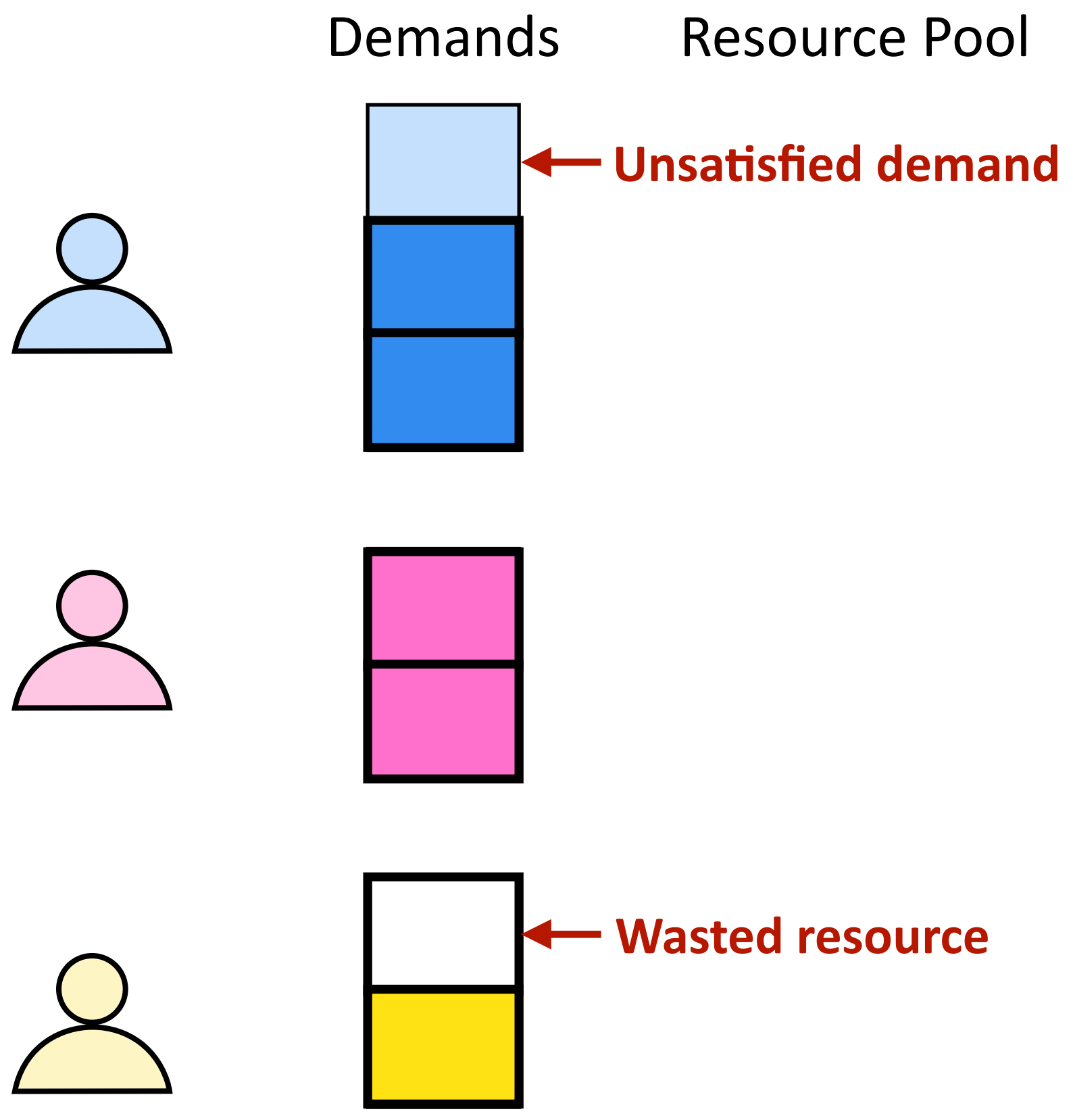
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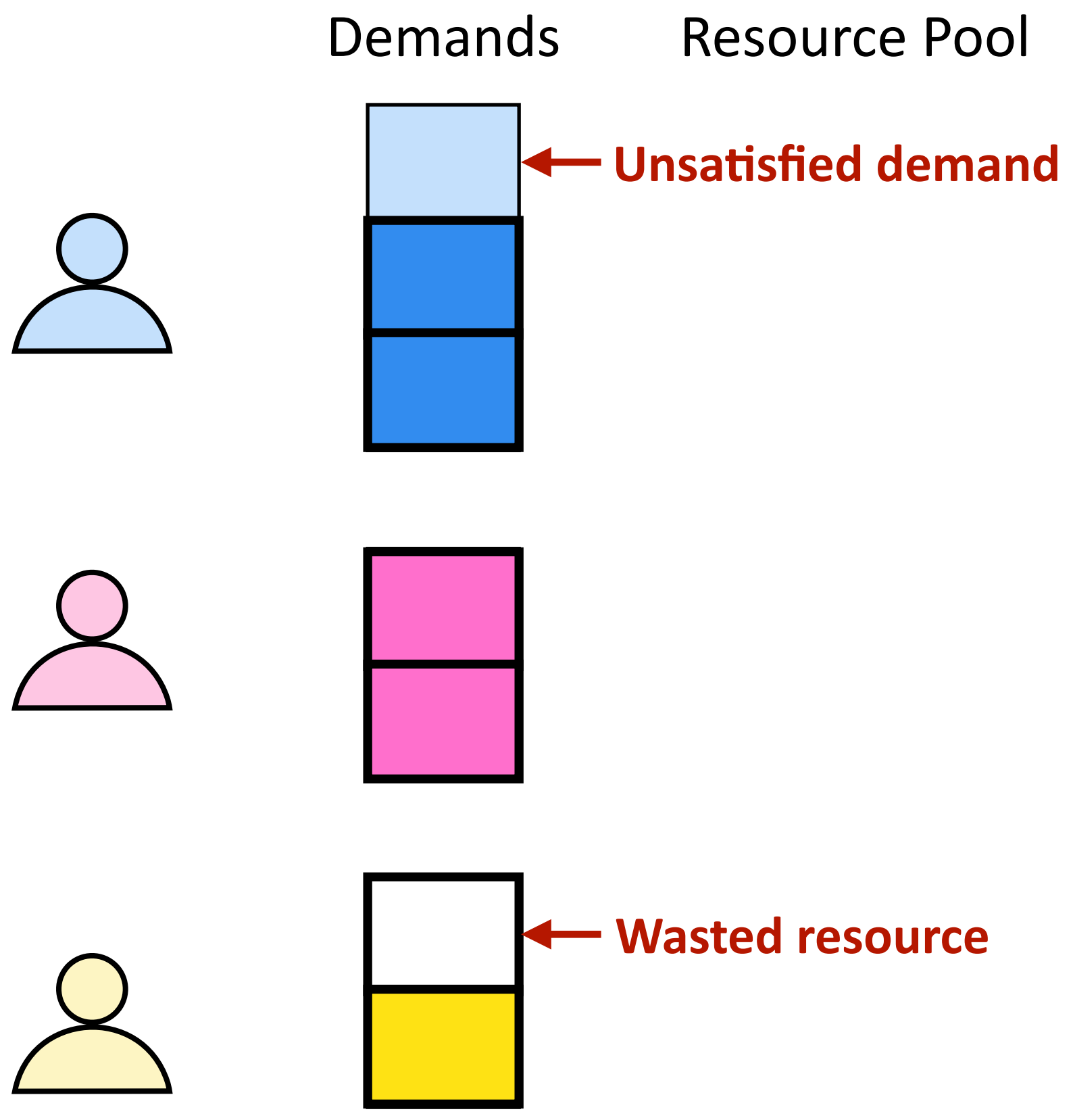
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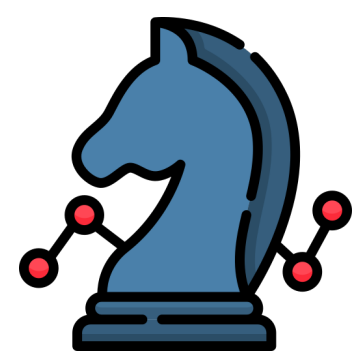
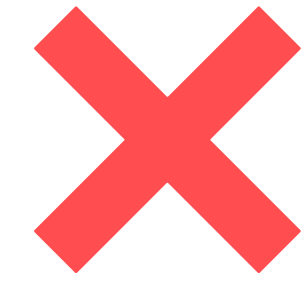


Strict partitioning

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Pareto efficiency



Strategy-proofness

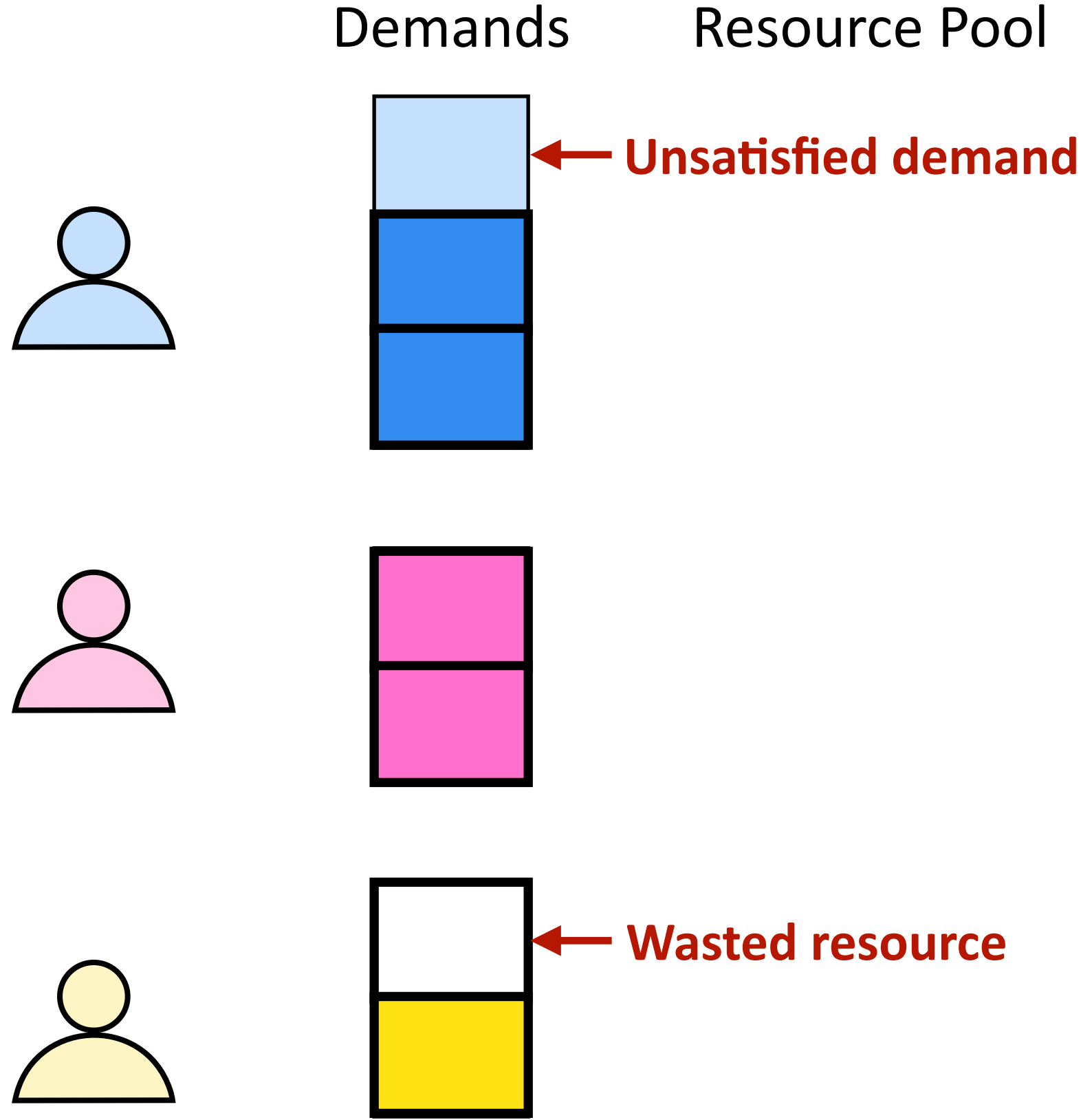


Fairness

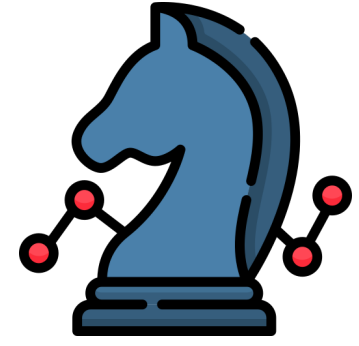
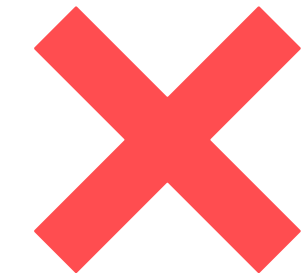


Strict partitioning

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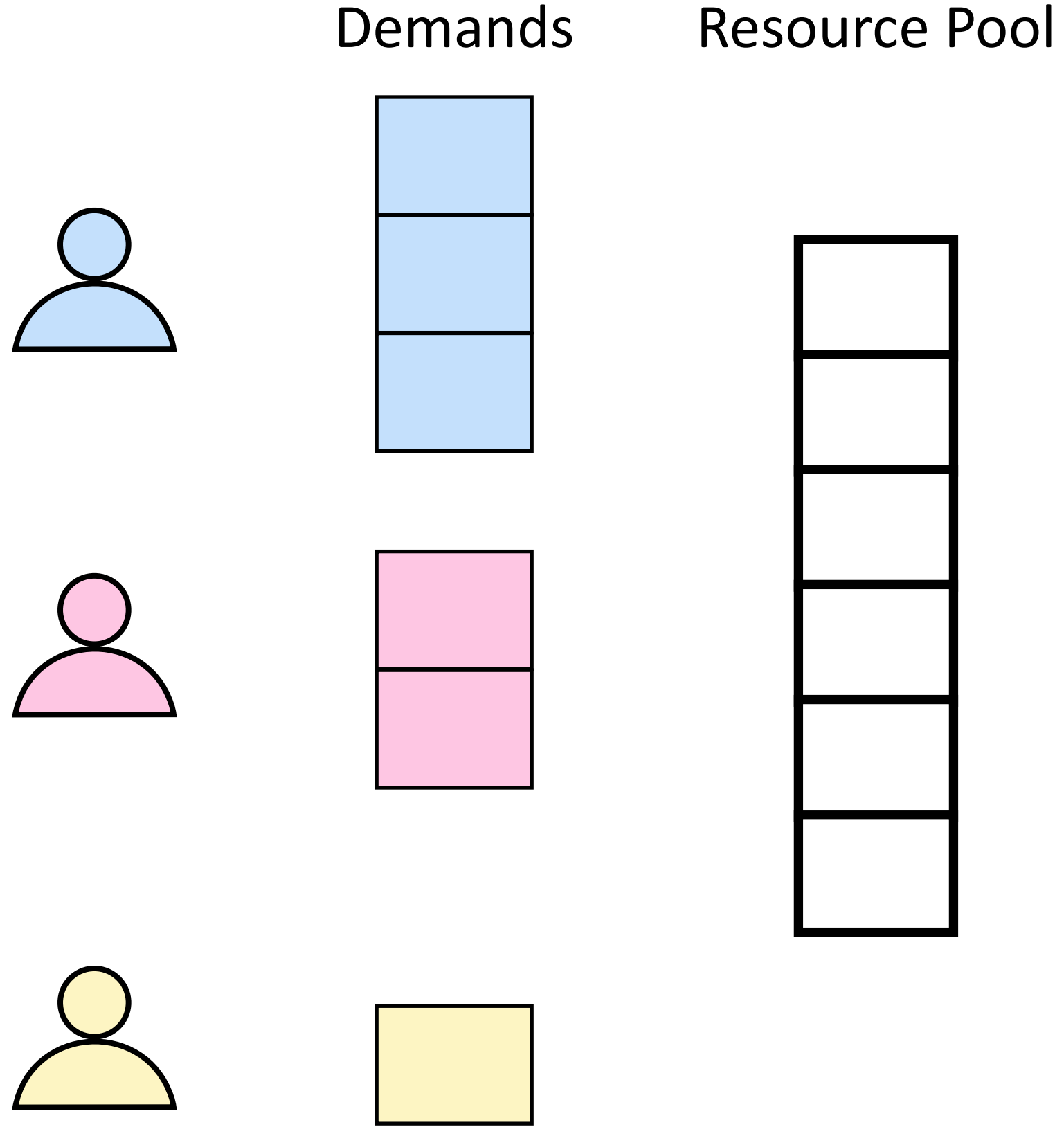
Fairness



Strict partitioning does not guarantee Pareto efficiency

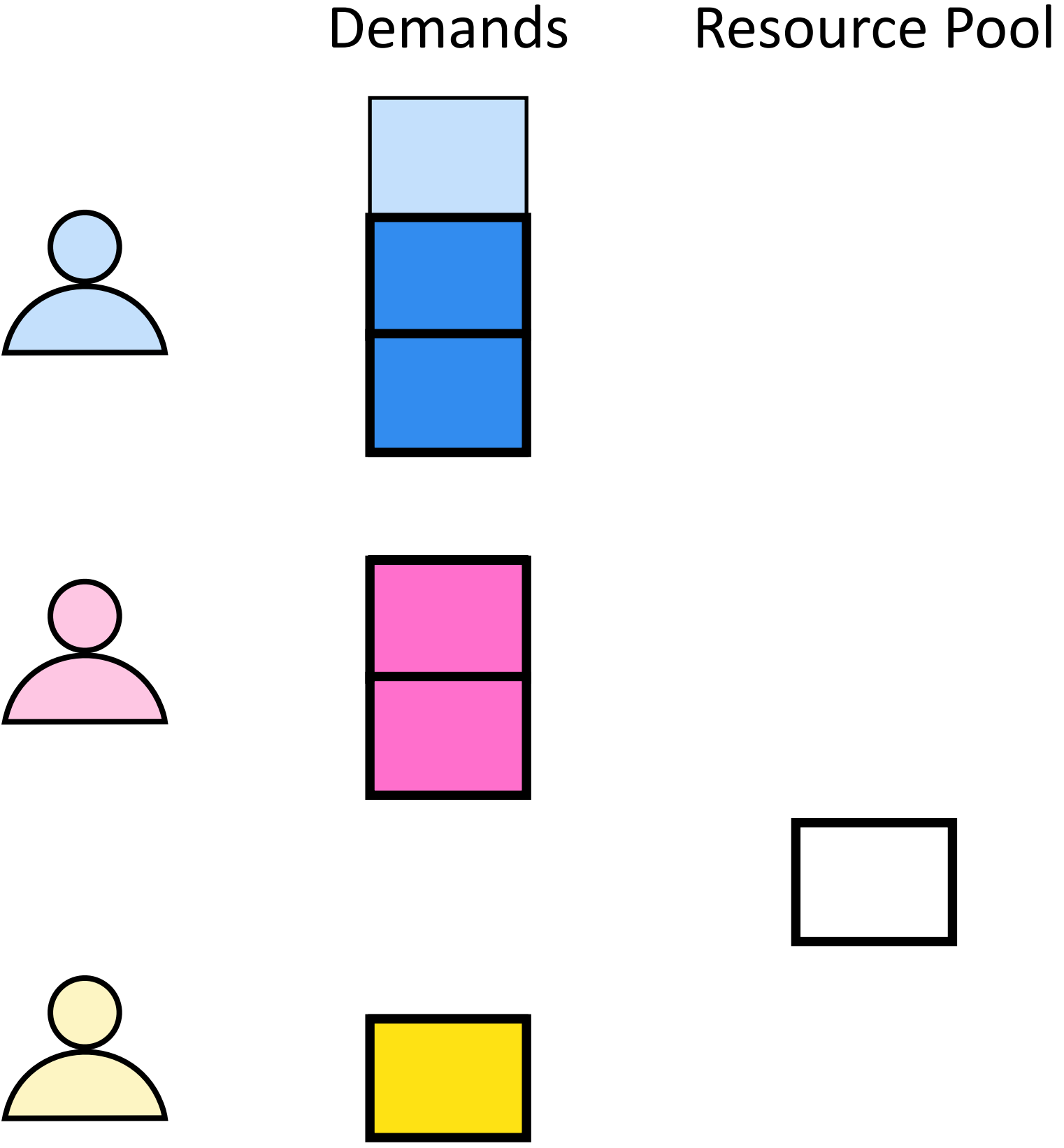
Max-min Fairness alleviates the limitations of strict partitioning (under an assumption) ⁵

Maximizing minimum allocation across users while ensuring allocation \leq demand for each user



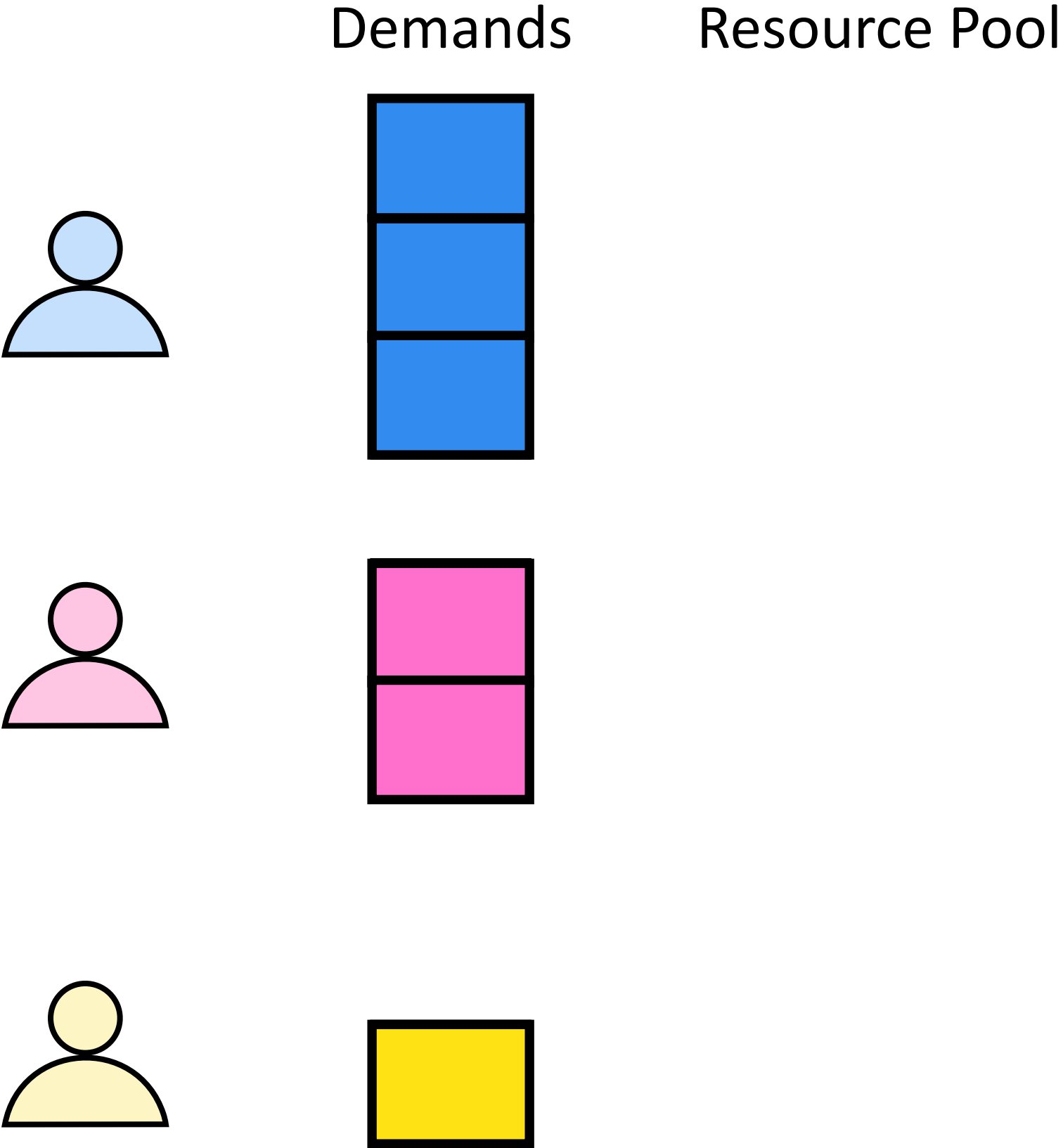
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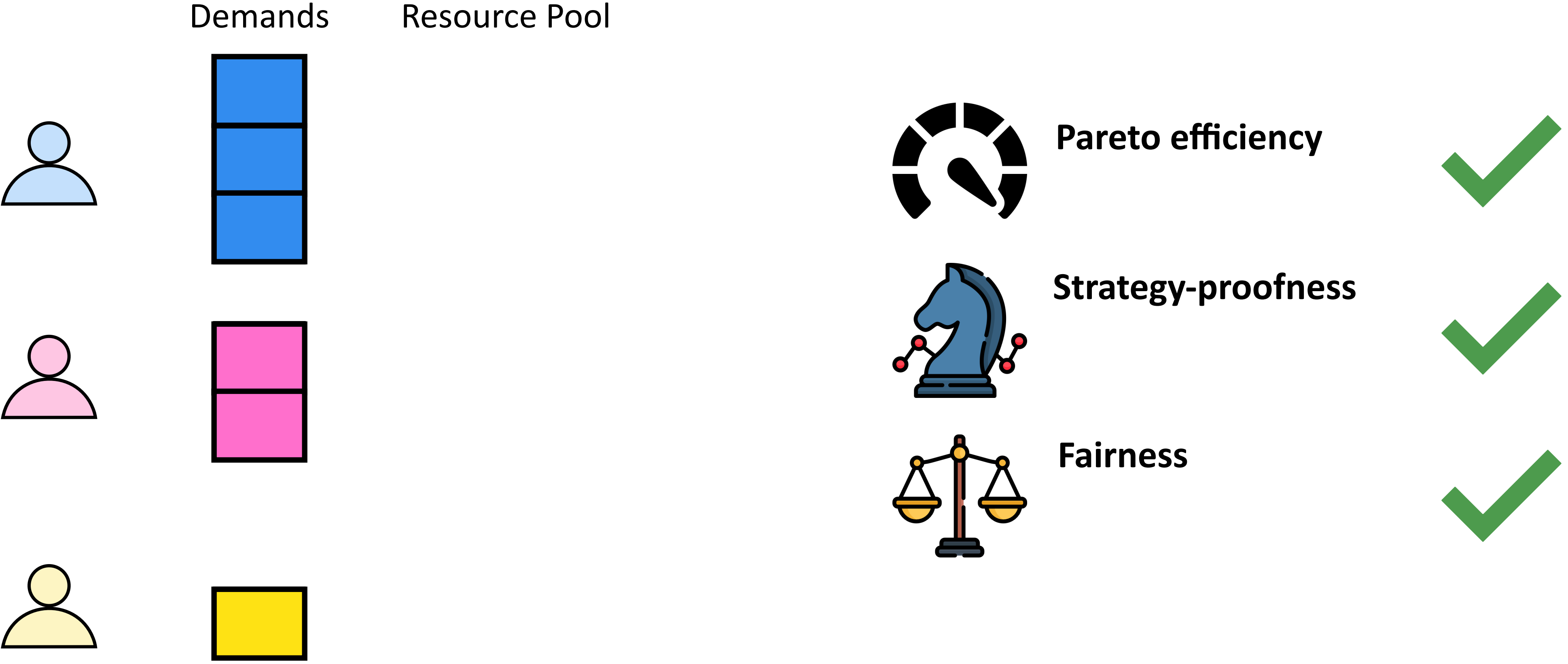
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Maximizing minimum allocation across users while ensuring allocation \leq demand for each user



Classical result: Max-min fairness satisfies Pareto efficiency, strategy-proofness and fairness

Underlying assumption: User demands are static

Dynamic demands are the norm in real world deployments

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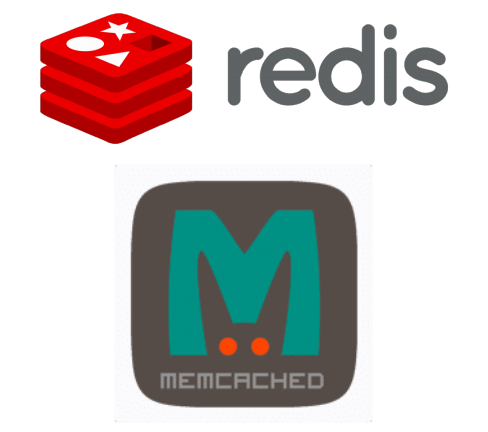


Shared Analytics Clusters

Dynamic demands are the norm in real world deployments

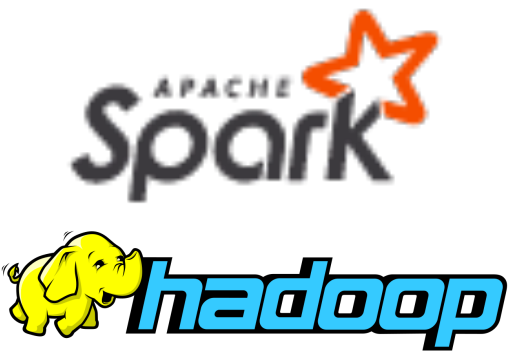


Shared Analytics Clusters

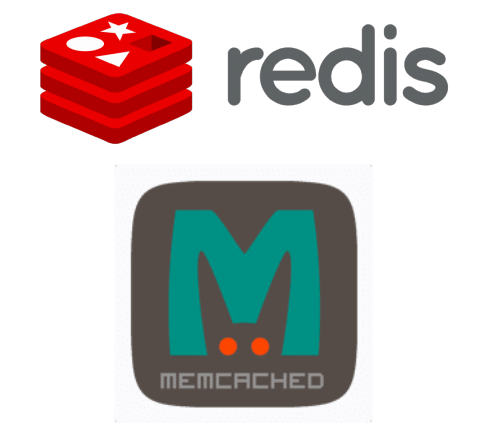


In-memory Key-Value Caches

Dynamic demands are the norm in real world deployments



Shared Analytics Clusters



In-memory Key-Value Caches



Inter-datacenter Network Links

Dynamic demands are the norm in real world deployments

Analysis of real world workloads



Shared Analytics Clusters



In-memory Key-Value Caches



Inter-datacenter Network Links

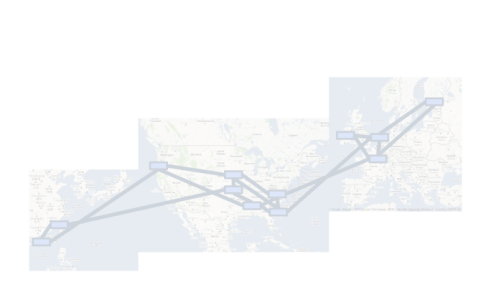
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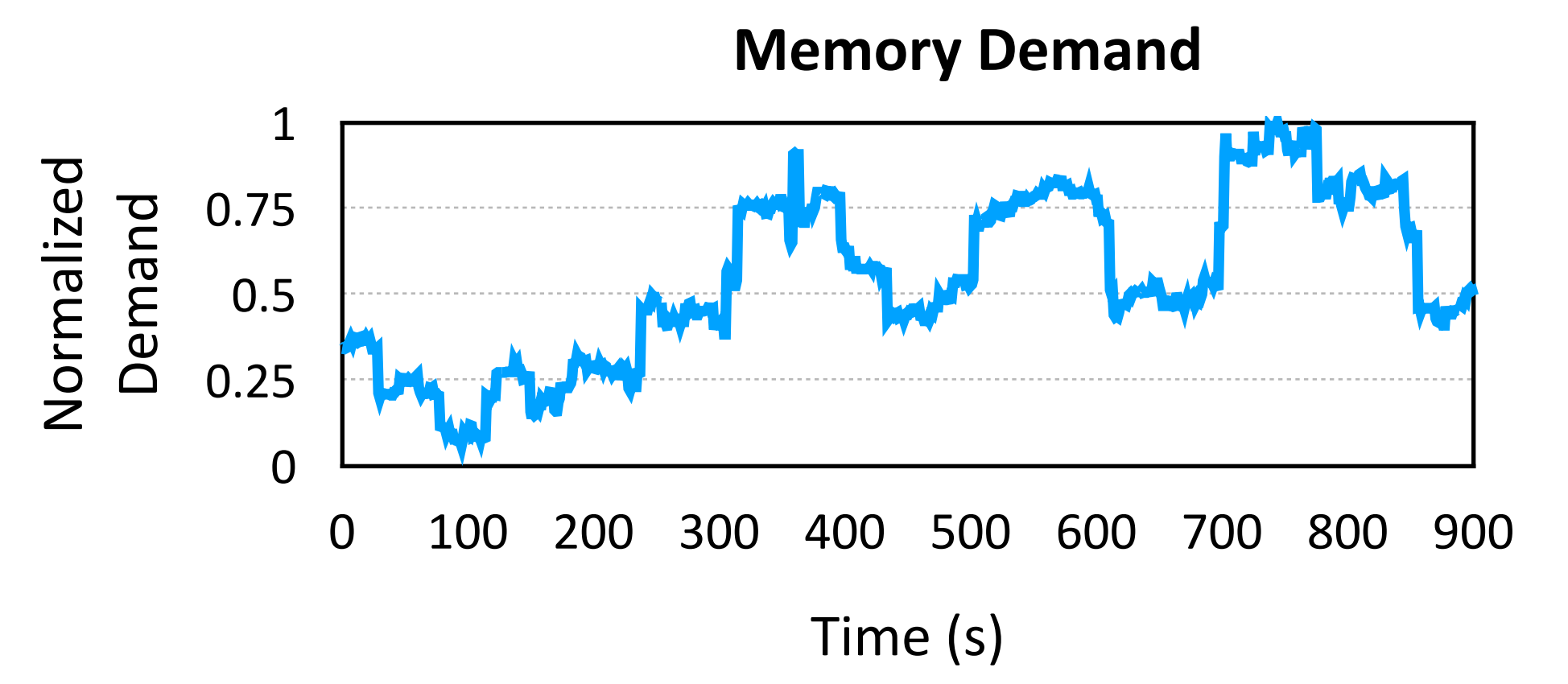
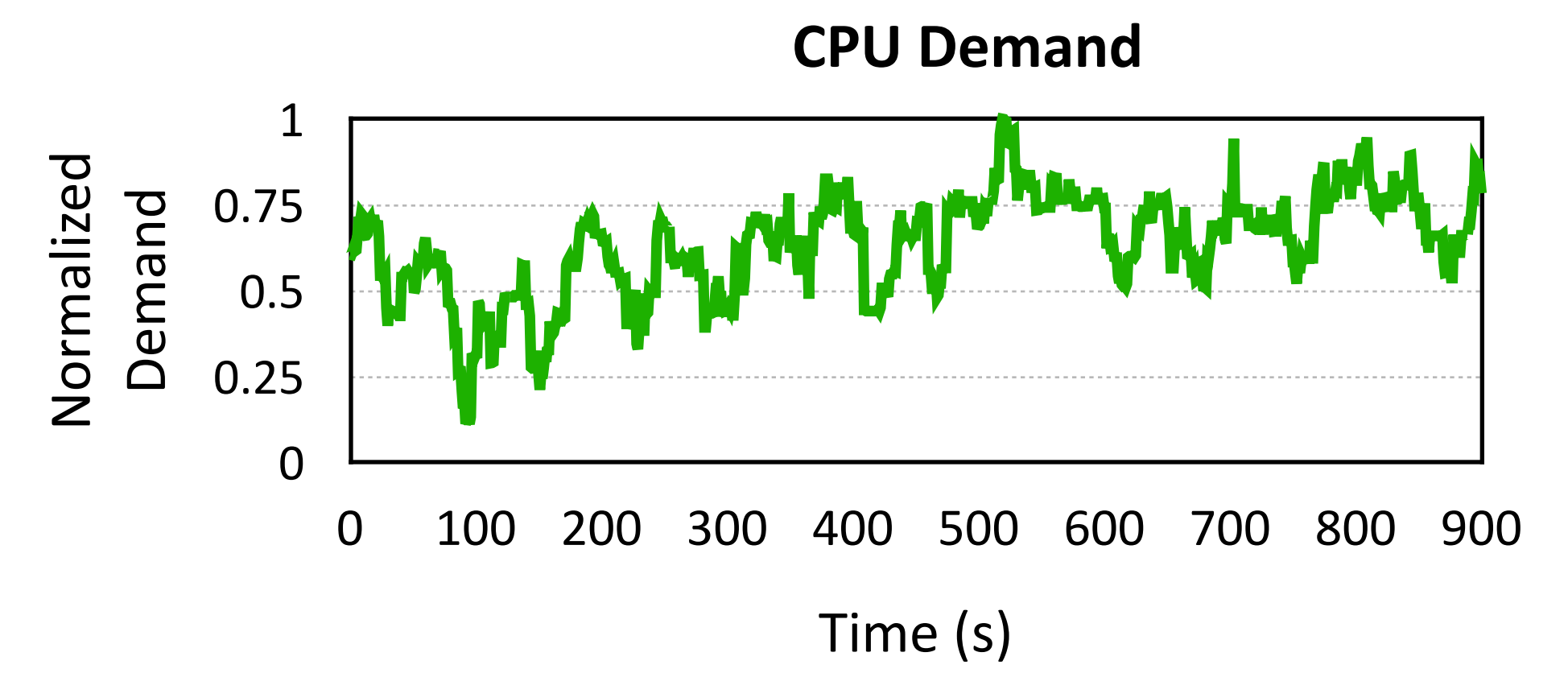


In-memory Key-Value Caches



Inter-datacenter Network Links

Analysis of real world workloads



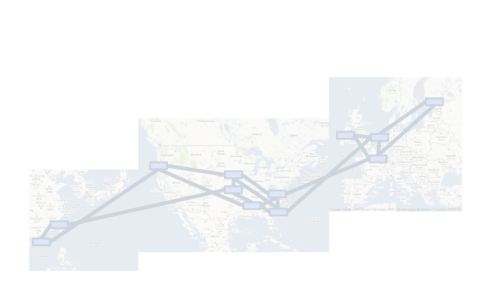
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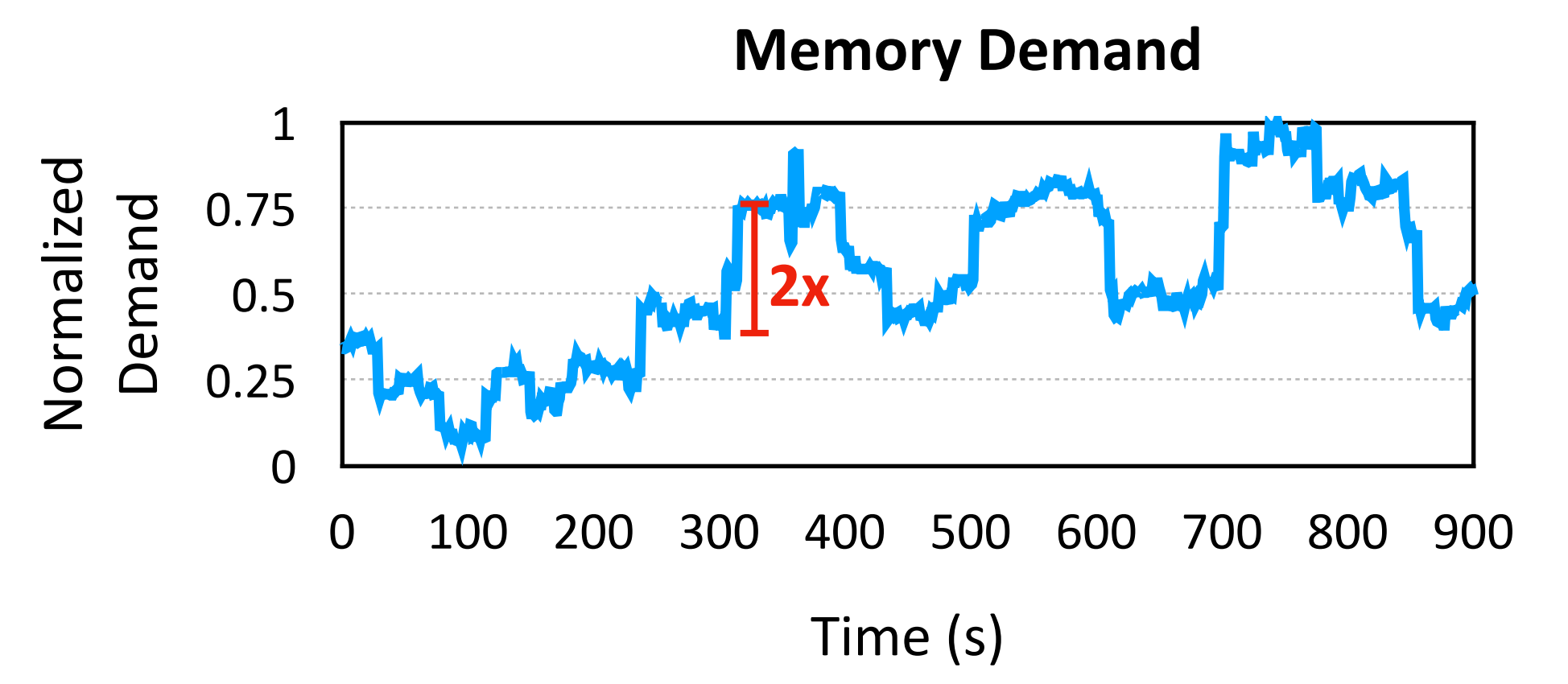
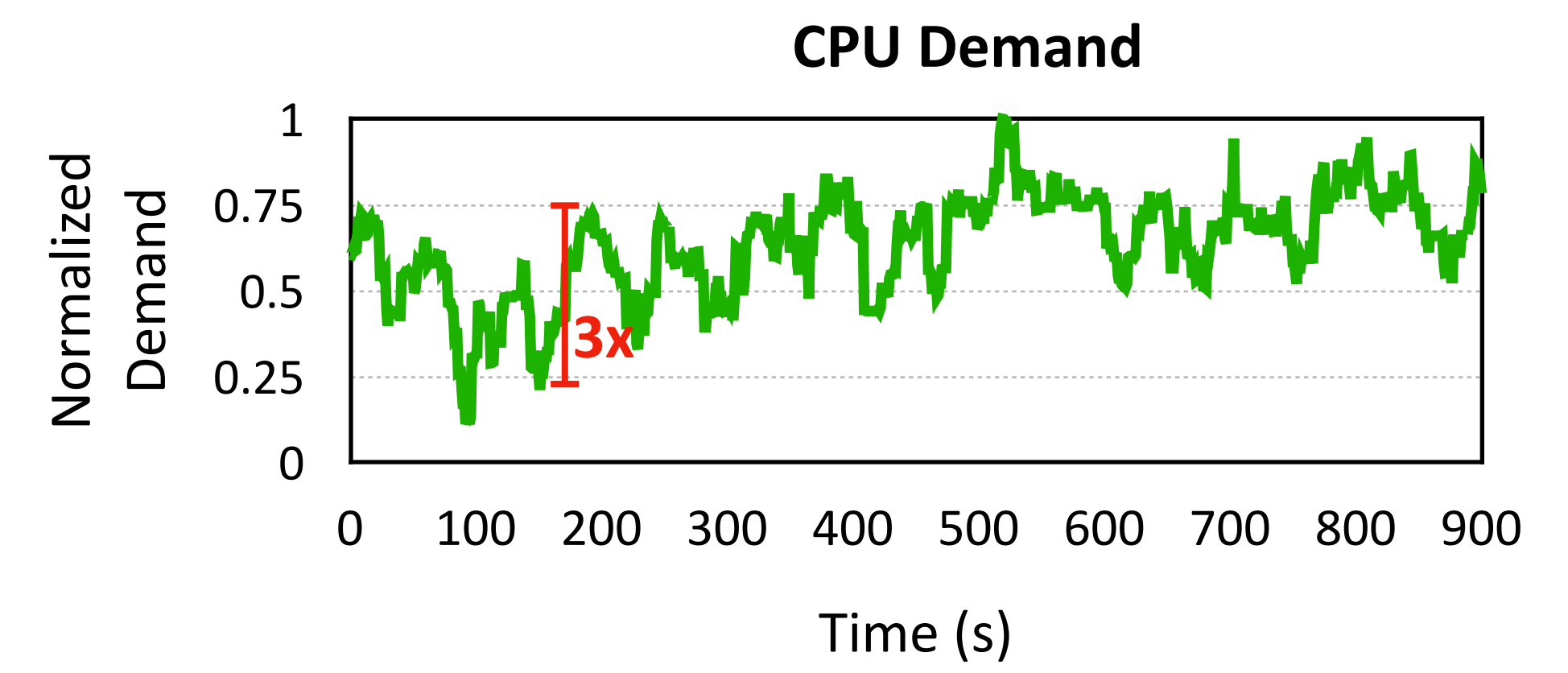


In-memory Key-Value Caches



Inter-datacenter Network Links

Analysis of real world workloads



2-3x variation in demands over 10s of seconds

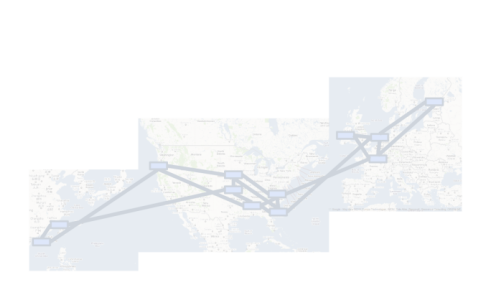
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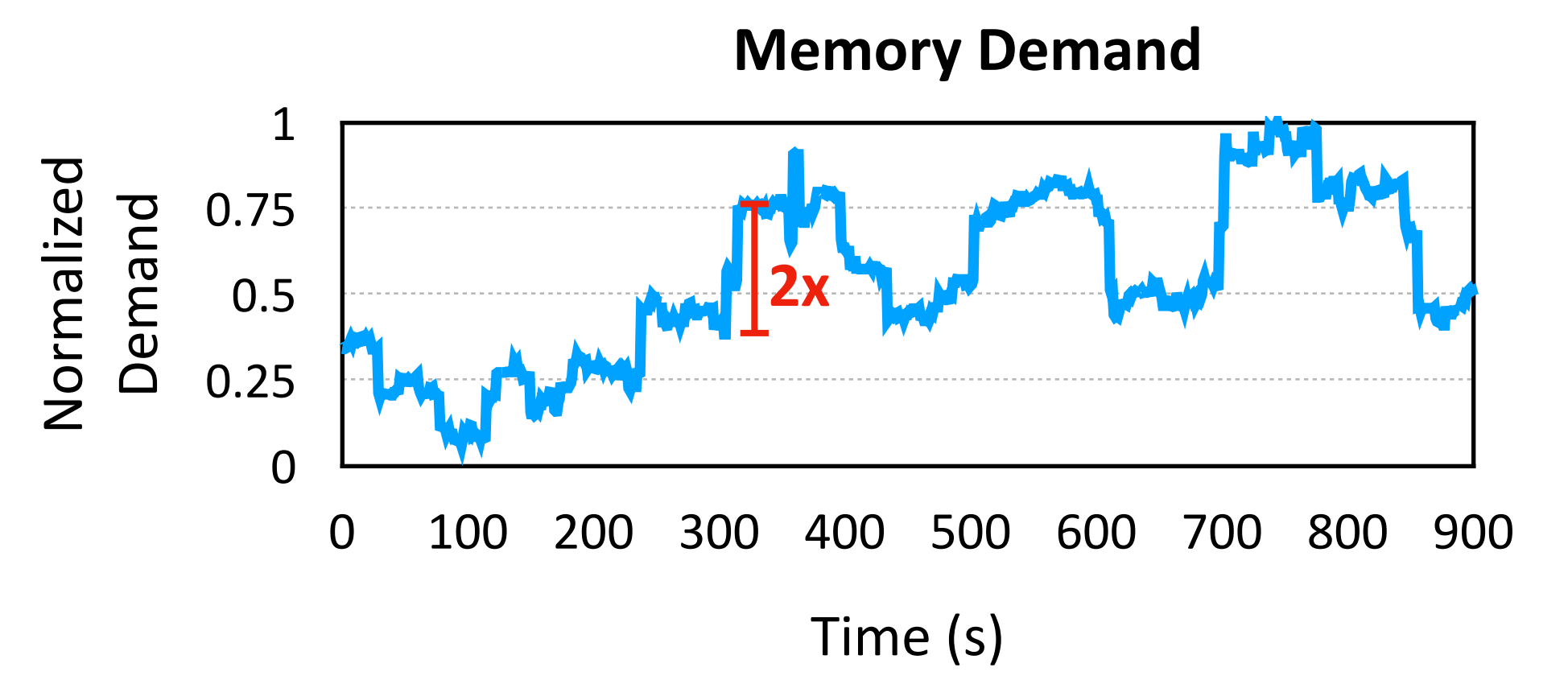
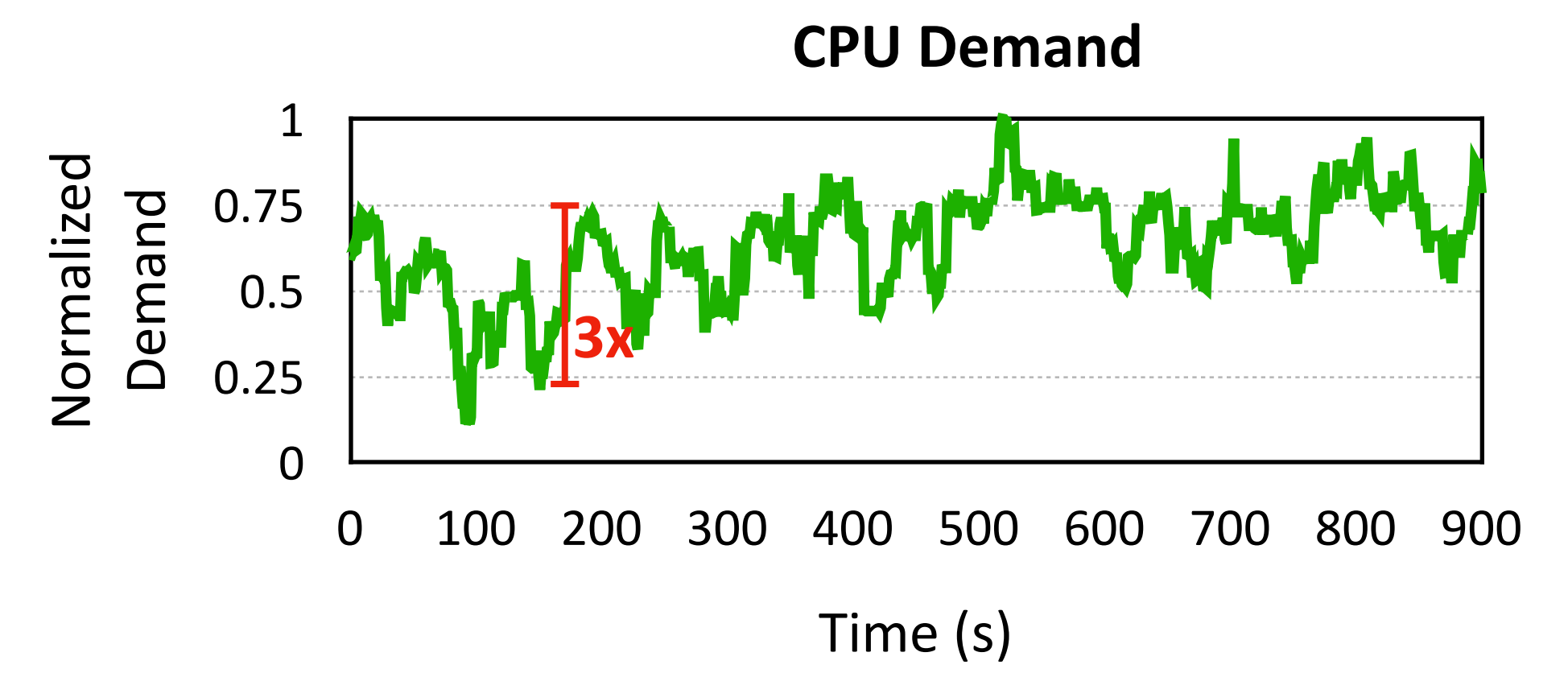


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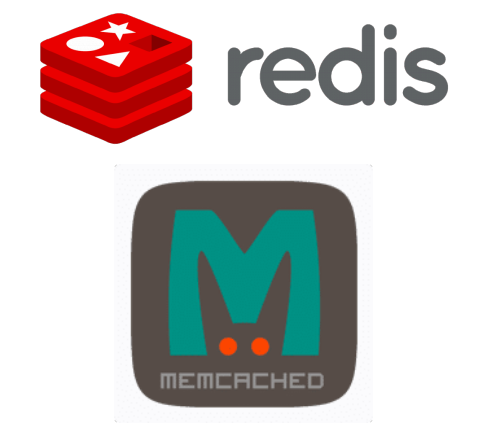
40-70% of users have standard deviation of demands > 1/2 mean

Dynamic demands are the norm in real world deployments



Shared Analytics Clusters

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In-memory Key-Value Caches



Inter-datacenter Network Links

Dynamic demands are the norm in real world deployments



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2-3x variation in demands over 10s of seconds



In-memory Key-Value Caches



More than 5x variation in demands within an hour

[Twitter, Yang et al., OSDI'20]



Inter-datacenter Network Links

35% variation in demands over 5 minute intervals

[Microsoft, Abuzaid et al., NSDI'21]

Dynamic demands are the norm in real world deployments



Shared Analytics Clusters



2-3x variation in demands over 10s of seconds



In-memory Key-Value Caches



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Inter-datacenter Network Links

35% variation in demands over 5 minute intervals

[Microsoft, Abuzaid et al., NSDI'21]

Significant variation in user demands over time in real workloads

Max-min fairness under dynamic demands: loses one or more of its properties ⁹



Pareto efficiency



Strategy-proofness



Fairness

Max-min fairness under dynamic demands: loses one or more of its properties ⁹

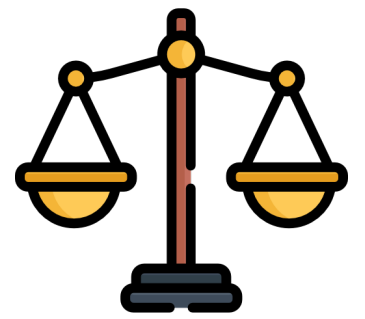
Max-min fairness
based on demands at $t=0$



Pareto efficiency



Strategy-proofness



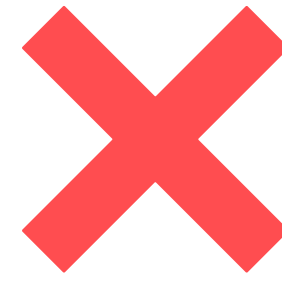
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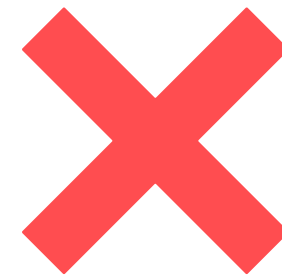
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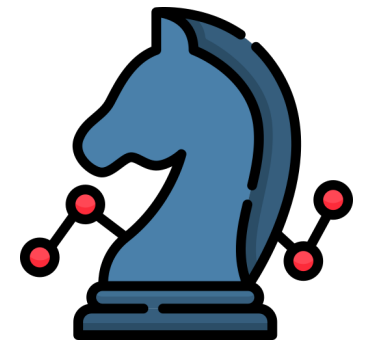
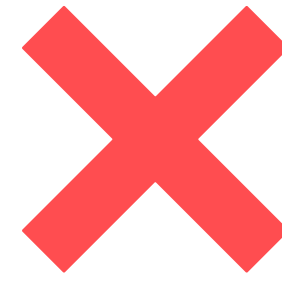
(Explained in paper)

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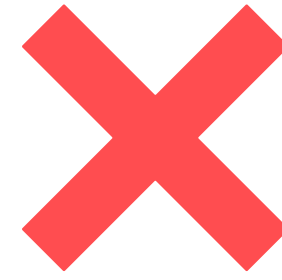
	Max-min fairness based on demands at $t=0$	Max-min fairness applied periodically
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Pareto efficiency



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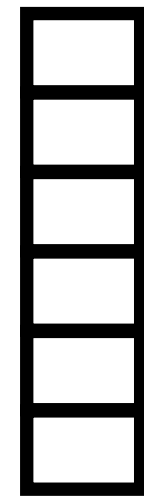
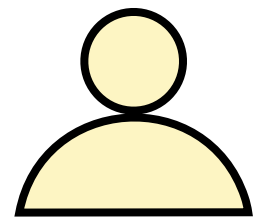
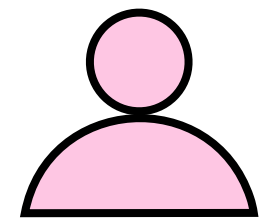
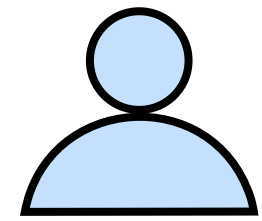
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 Pareto efficiency		✗
 Strategy-proofness		✗
 Fairness		

Max-min fairness under dynamic demands: loses one or more of its properties ¹⁰

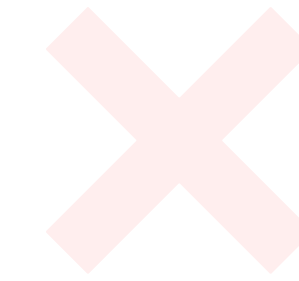
Running Example

Demands

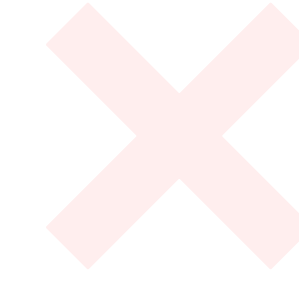
Resource Pool



Pareto efficiency



Strategy-proofness



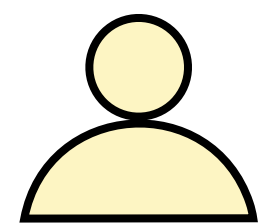
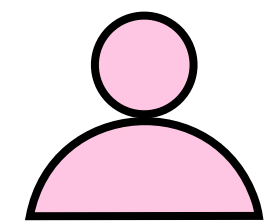
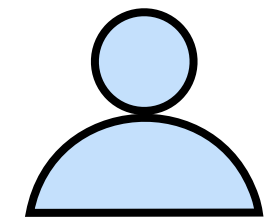
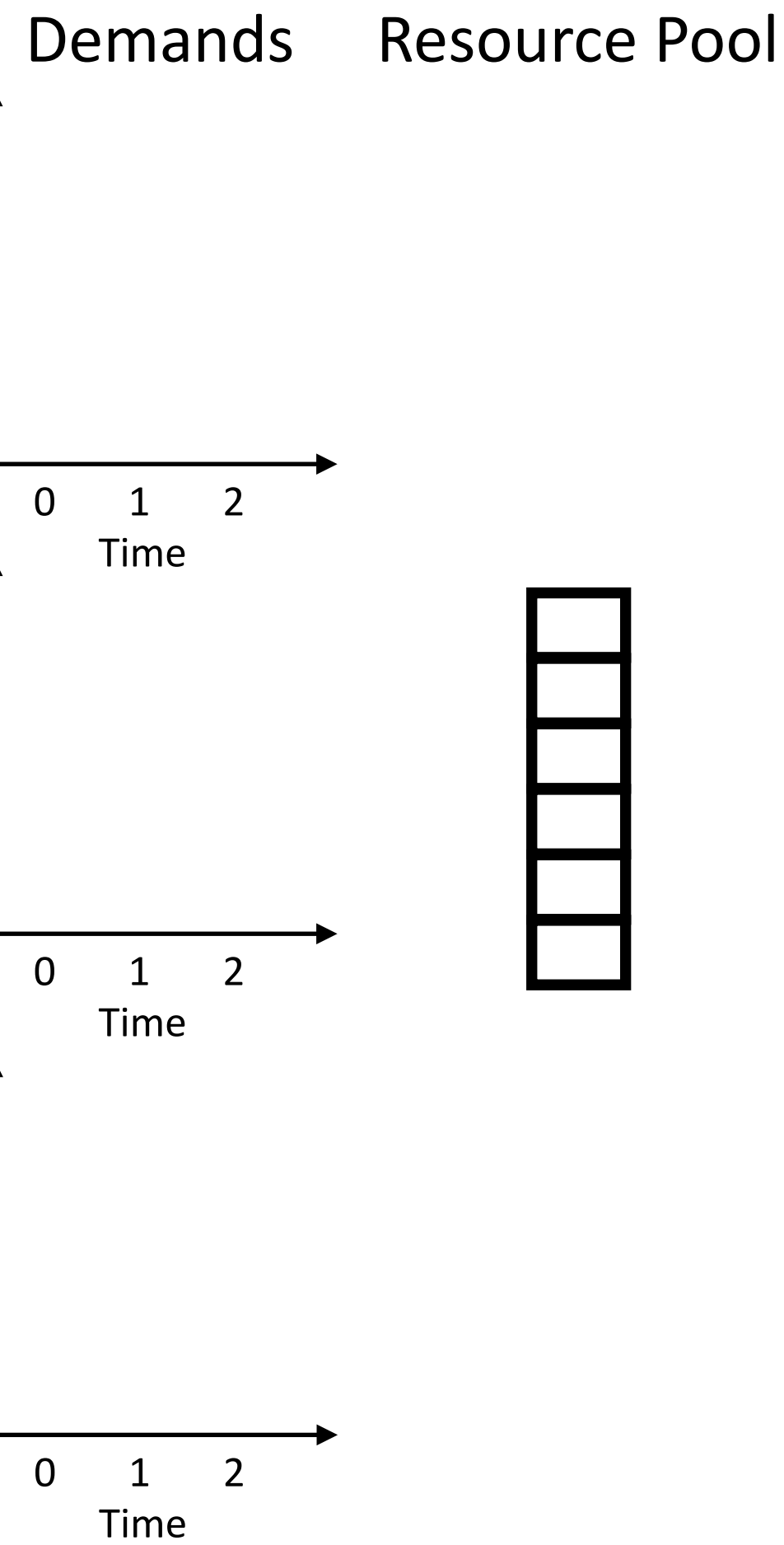
Fairness

Max-min fairness
based on demands at $t=0$

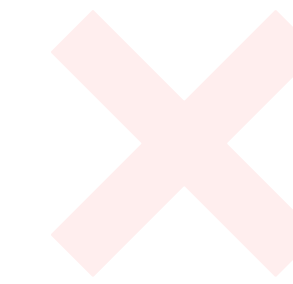
Max-min fairness
applied periodically

Max-min fairness under dynamic demands: loses one or more of its properties 10

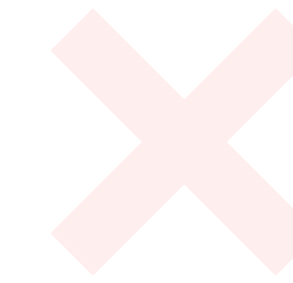
Running Example



Pareto efficiency



Strategy-proofness



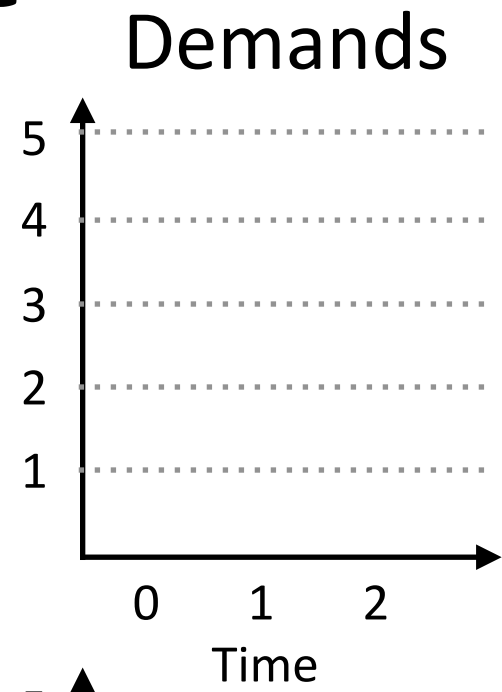
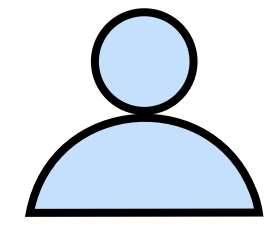
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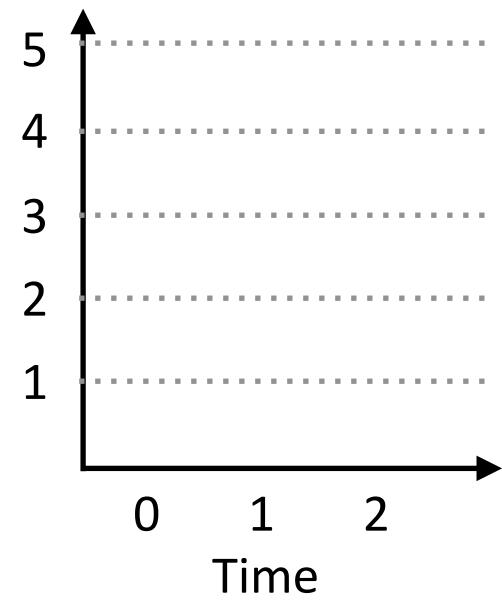
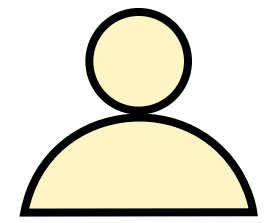
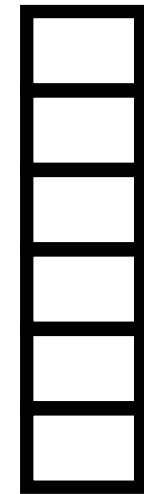
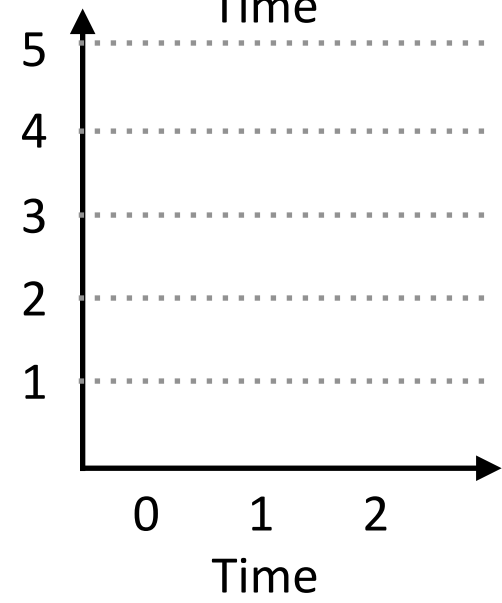
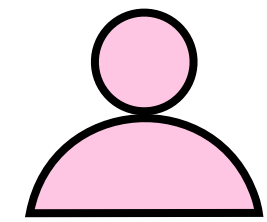
Max-min fairness
applied periodically

Max-min fairness under dynamic demands: loses one or more of its properties 10

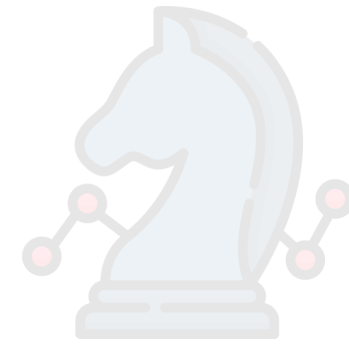
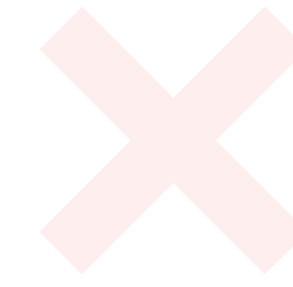
Running Example



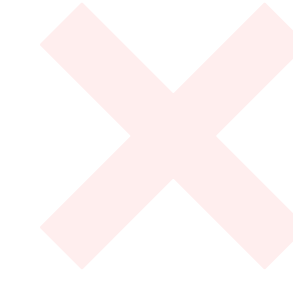
Resource Pool



Pareto efficiency



Strategy-proofness

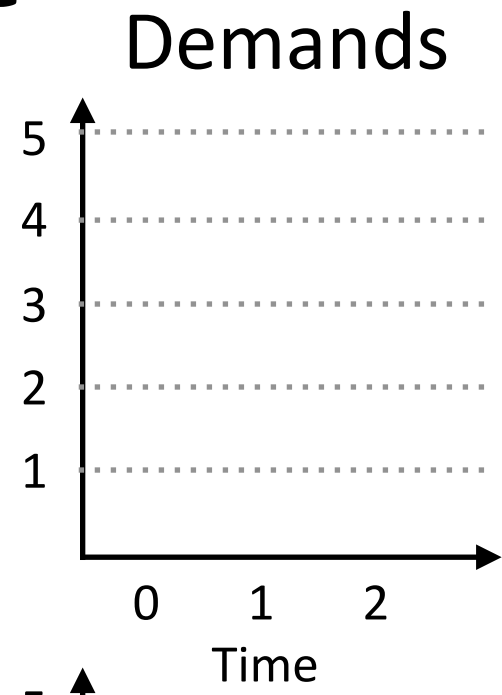
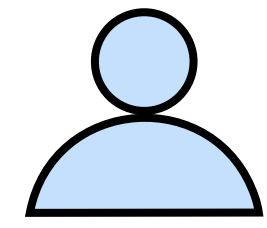


Fairness

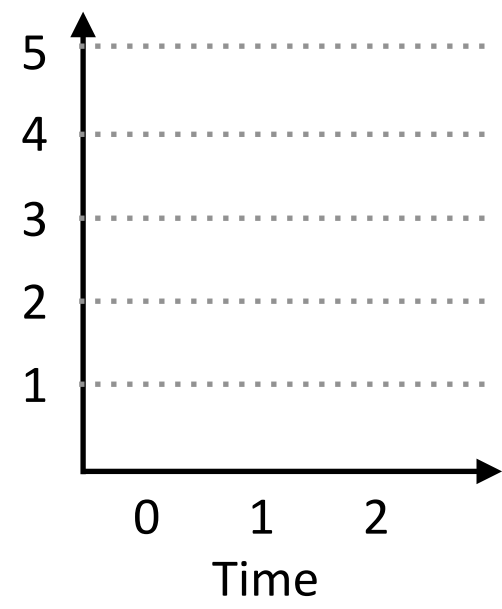
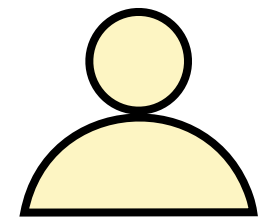
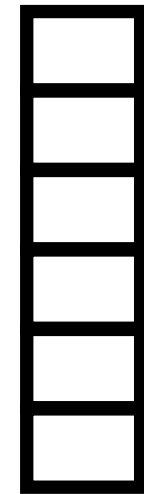
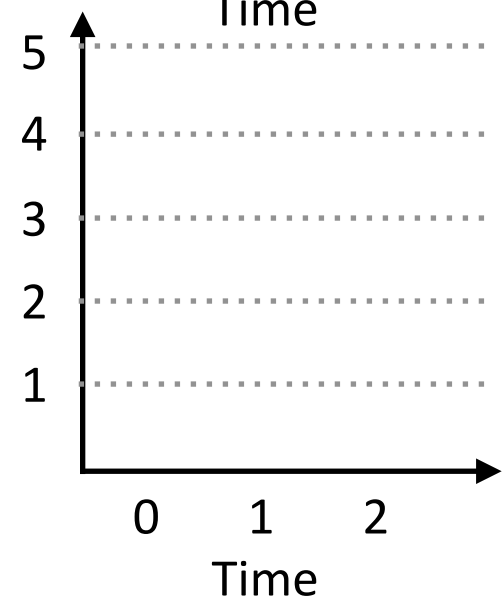
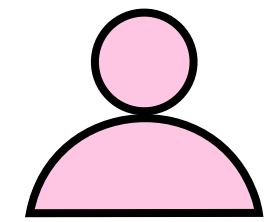
Max-min fairness applied periodically

Max-min fairness under dynamic demands: loses one or more of its properties 11

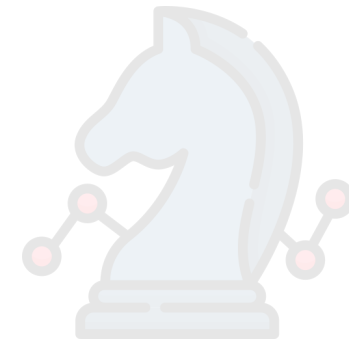
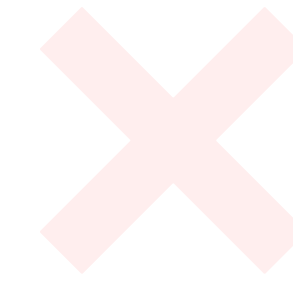
Running Example



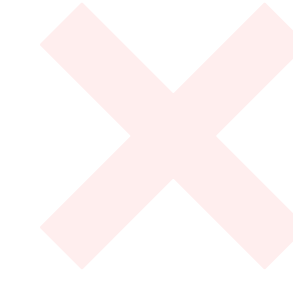
Resource Pool



Pareto efficiency



Strategy-proofness



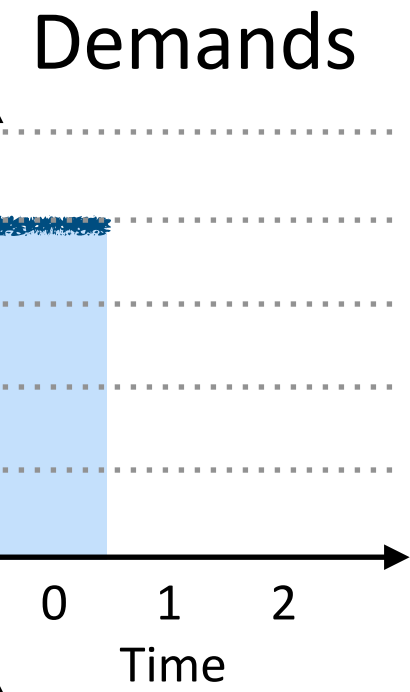
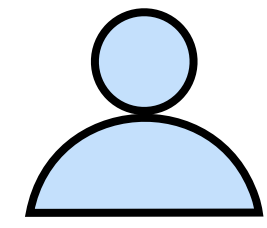
Fairness

Max-min fairness
based on demands at $t=0$

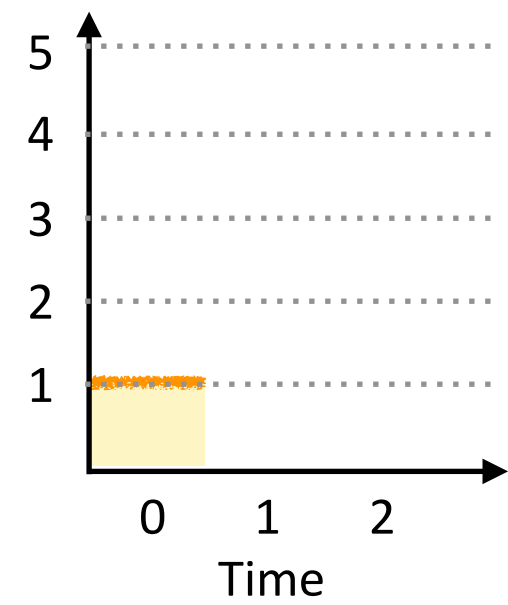
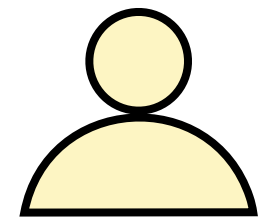
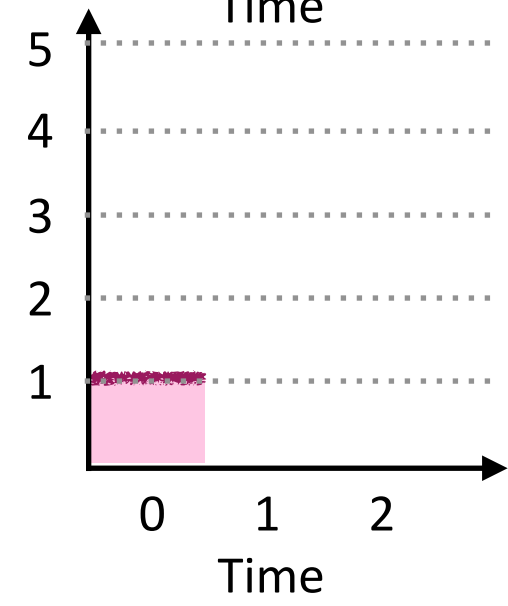
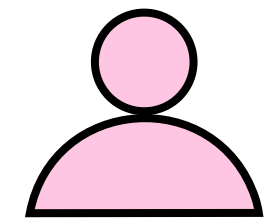
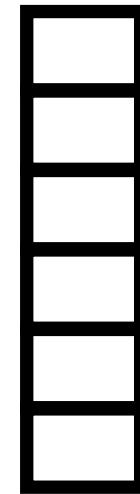
Max-min fairness
applied periodically

Max-min fairness under dynamic demands: loses one or more of its properties 11

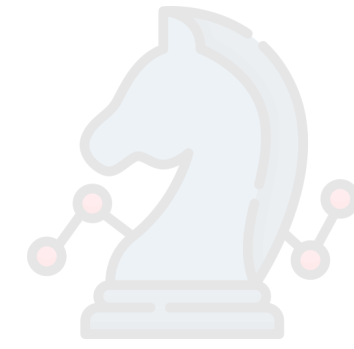
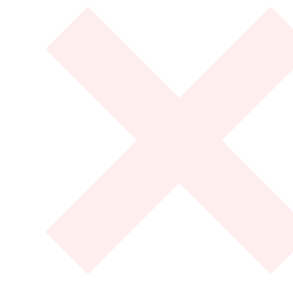
Running Example



Resource Pool



Pareto efficiency



Strategy-proofness

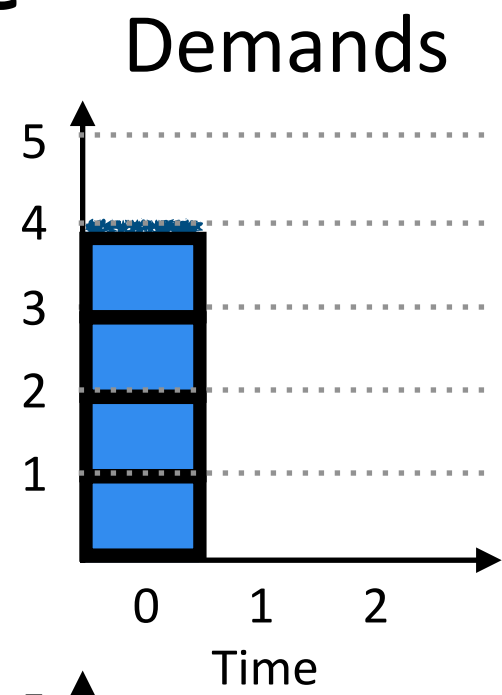
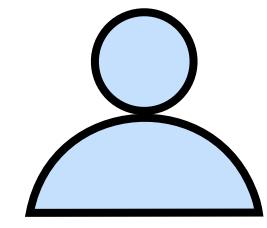


Fairness

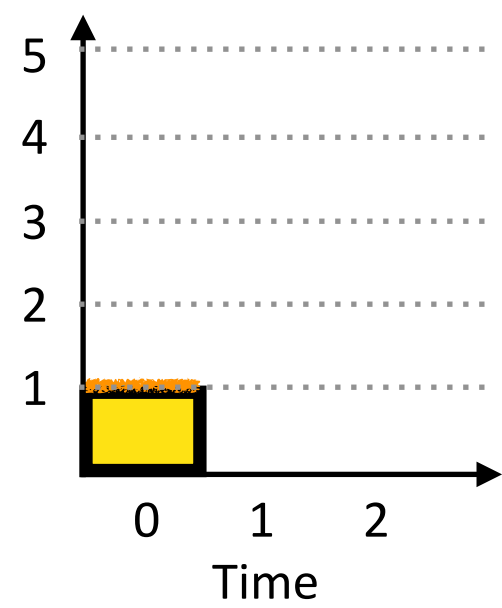
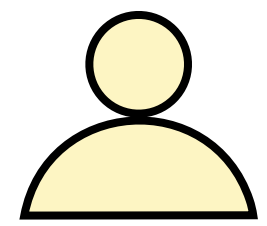
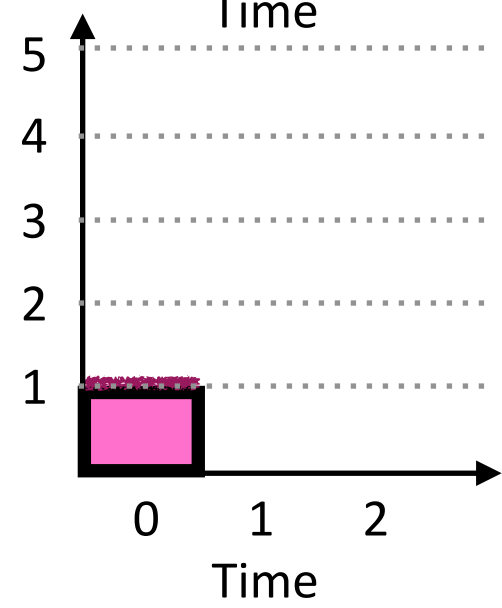
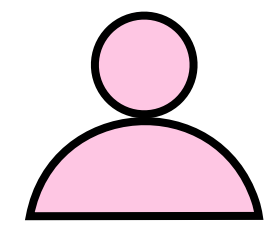
Max-min fairness applied periodically

Max-min fairness under dynamic demands: loses one or more of its properties 12

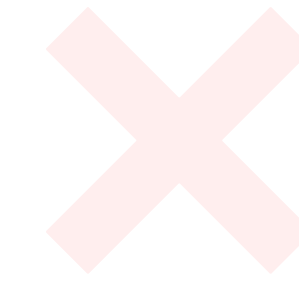
Running Example



Resource Pool



Pareto efficiency



Strategy-proofness



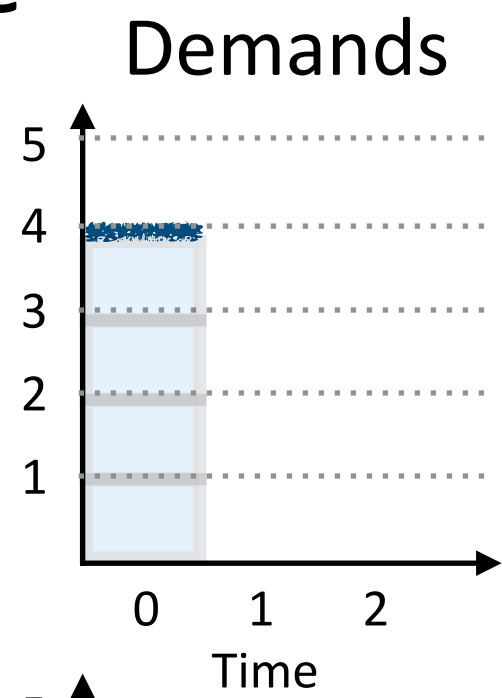
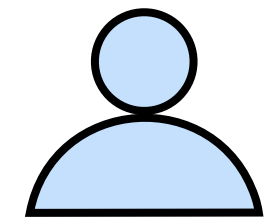
Fairness

Max-min fairness
based on demands at $t=0$

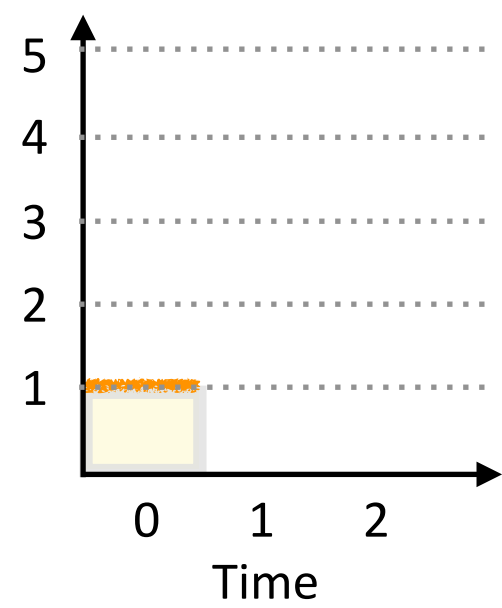
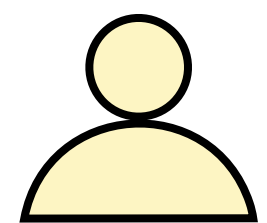
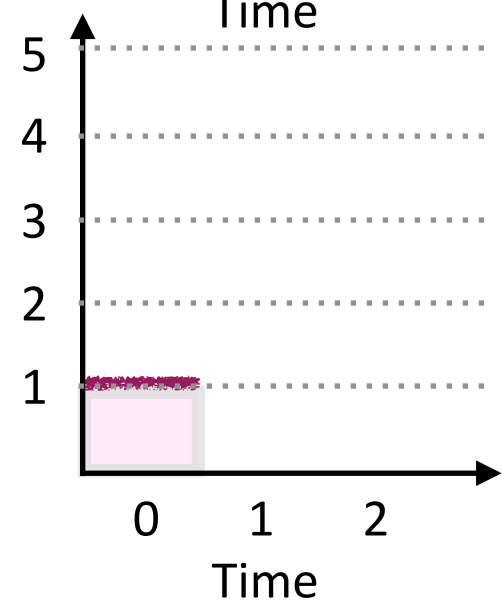
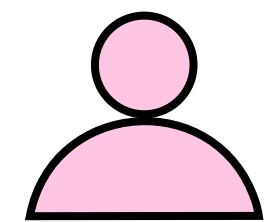
Max-min fairness
applied periodically

Max-min fairness under dynamic demands: loses one or more of its properties 13

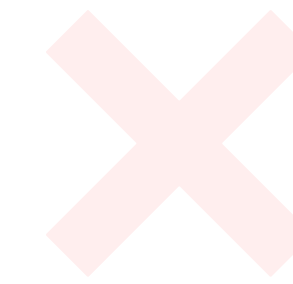
Running Example



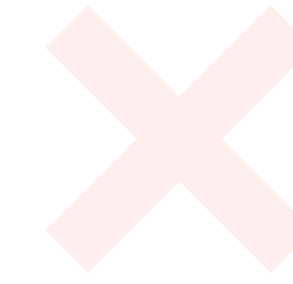
Resource Pool



Pareto efficiency



Strategy-proofness



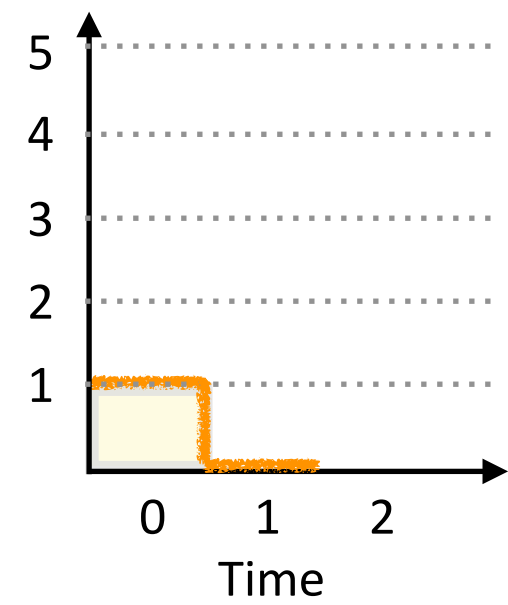
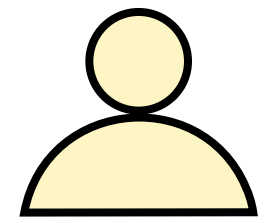
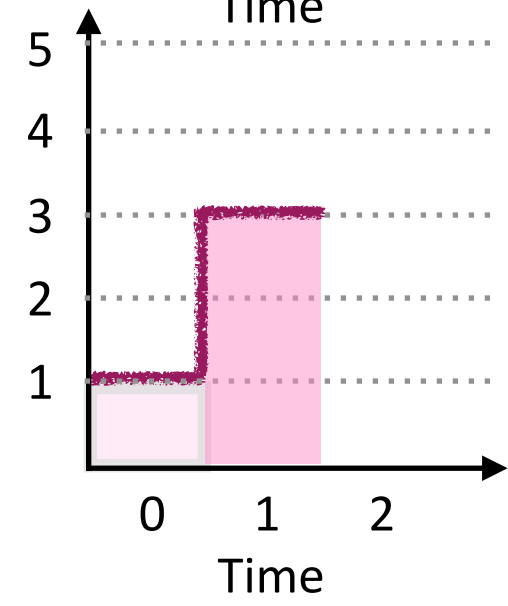
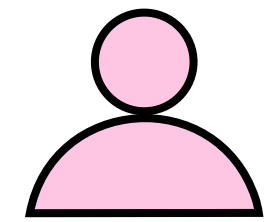
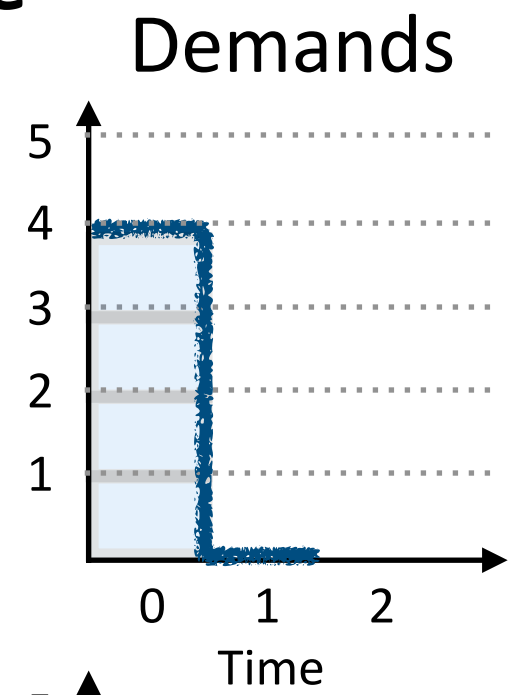
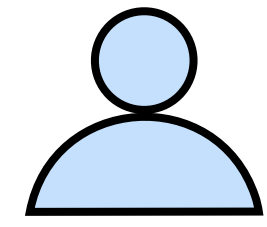
Fairness

Max-min fairness
based on demands at $t=0$

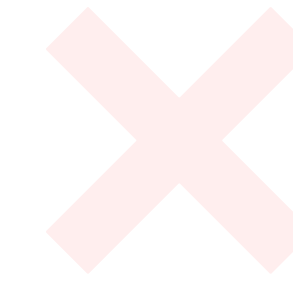
Max-min fairness
applied periodically

Max-min fairness under dynamic demands: loses one or more of its properties 13

Running Example



Pareto efficiency



Strategy-proofness



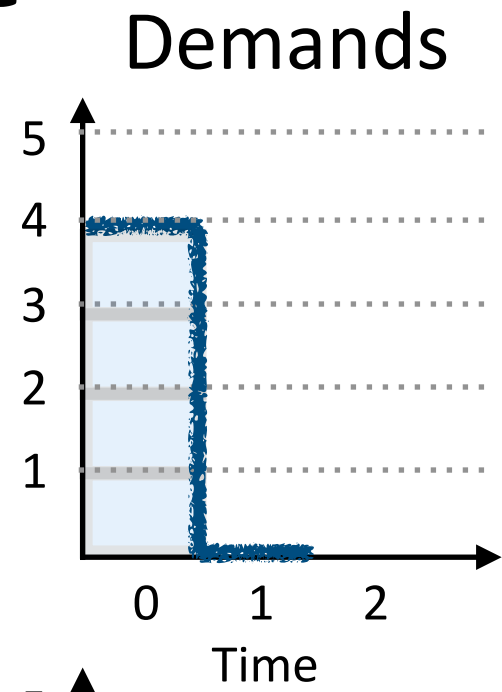
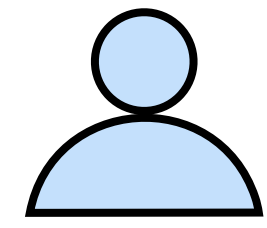
Fairness

Max-min fairness
based on demands at $t=0$

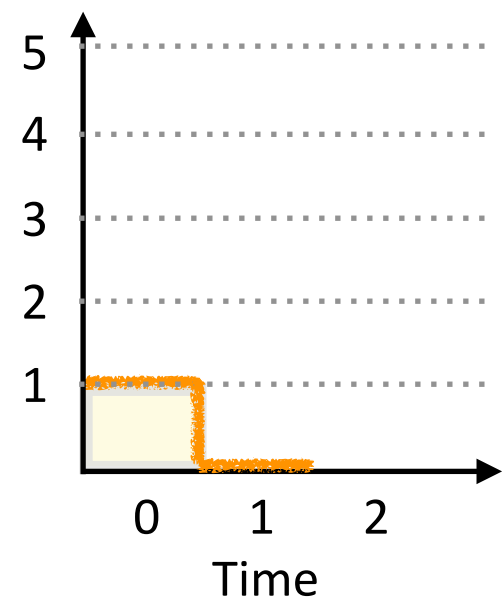
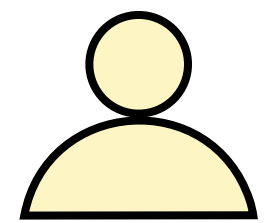
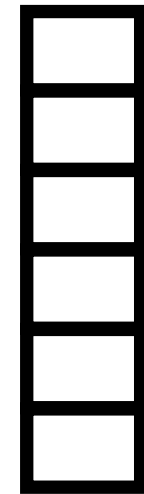
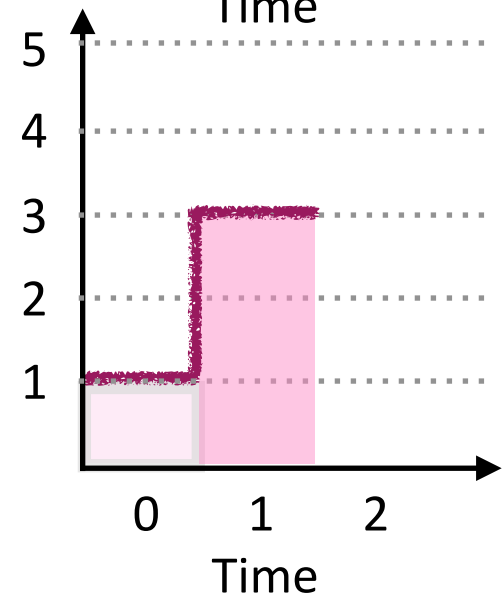
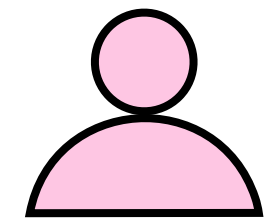
Max-min fairness
applied periodically

Max-min fairness under dynamic demands: loses one or more of its properties 13

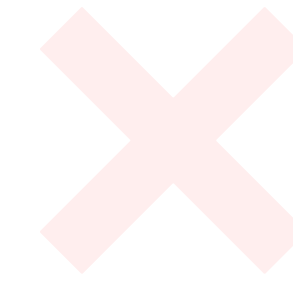
Running Example



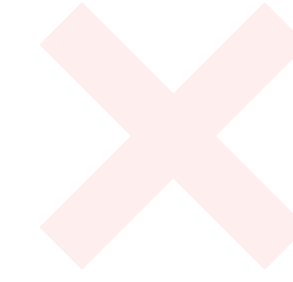
Resource Pool



Pareto efficiency



Strategy-proofness



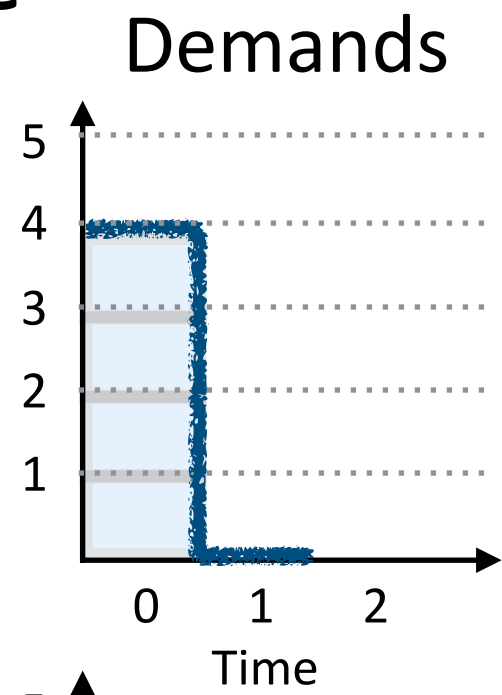
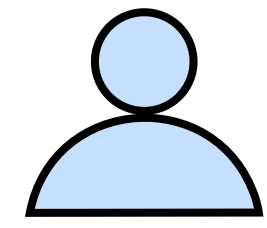
Fairness

Max-min fairness
based on demands at $t=0$

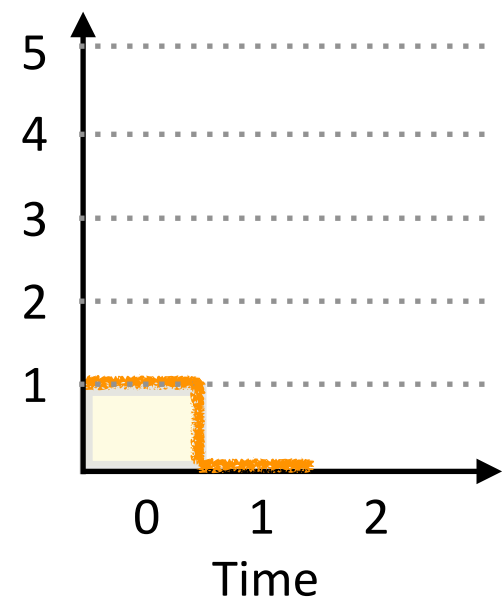
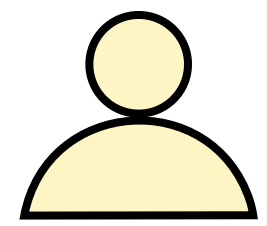
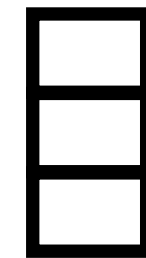
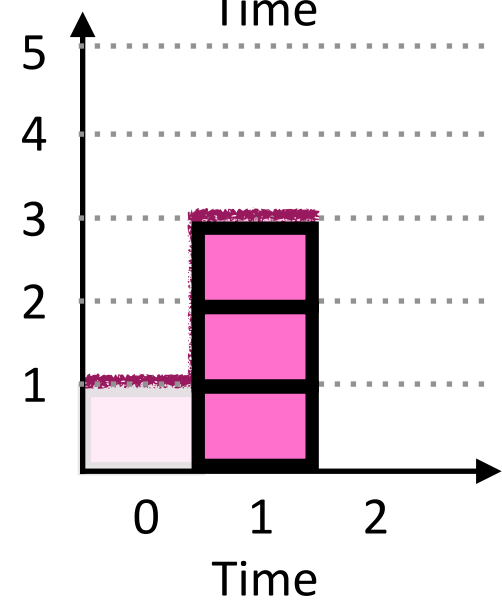
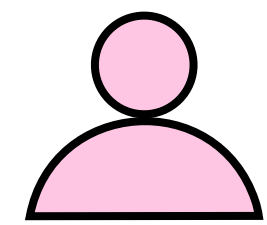
Max-min fairness
applied periodically

Max-min fairness under dynamic demands: loses one or more of its properties 14

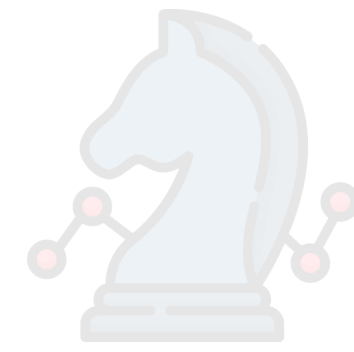
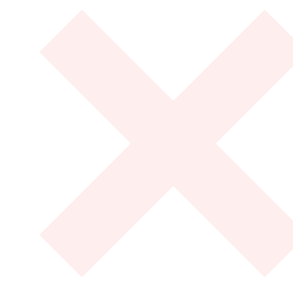
Running Example



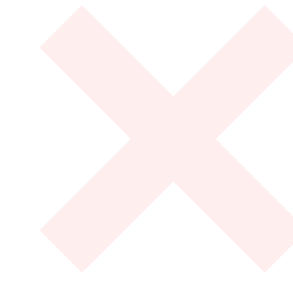
Resource Pool



Pareto efficiency



Strategy-proofness



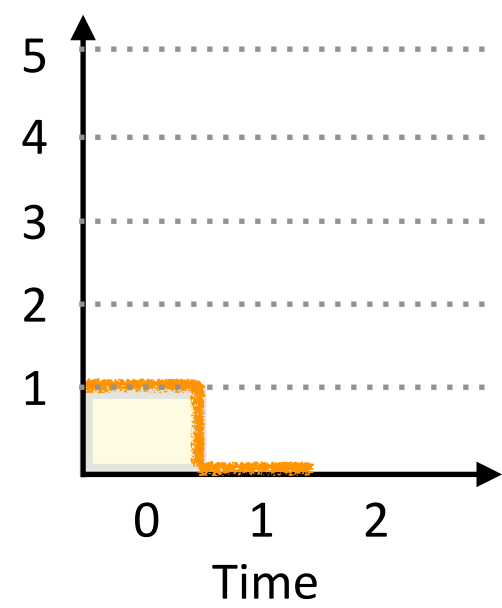
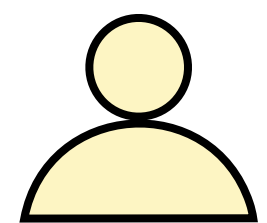
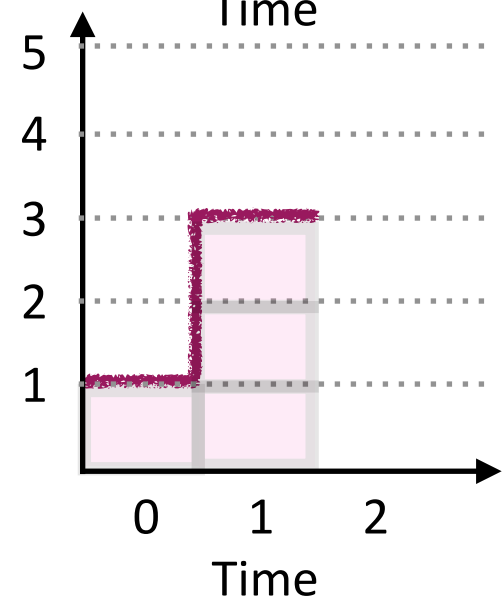
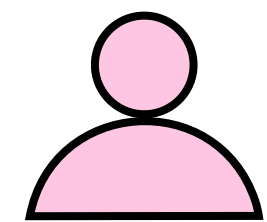
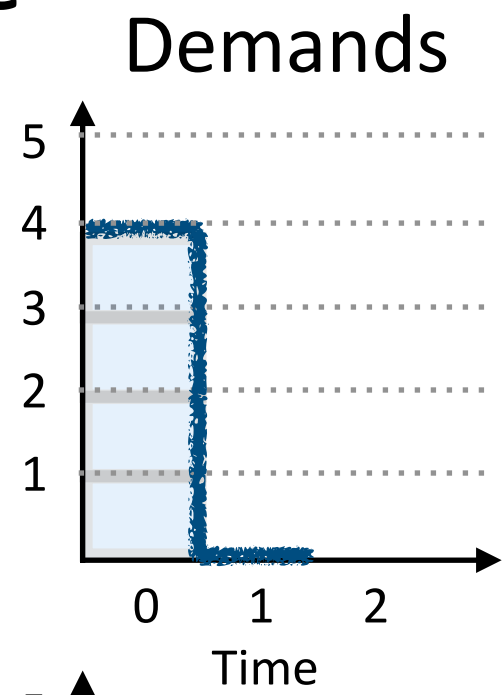
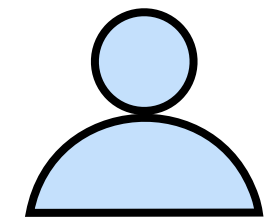
Fairness

Max-min fairness applied periodically

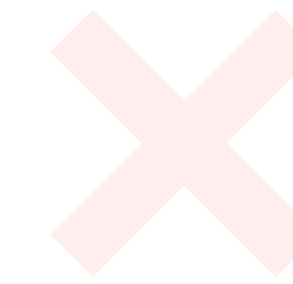
Max-min fairness based on demands at $t=0$

Max-min fairness under dynamic demands: loses one or more of its properties 15

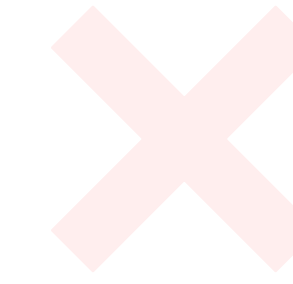
Running Example



Pareto efficiency



Strategy-proofness

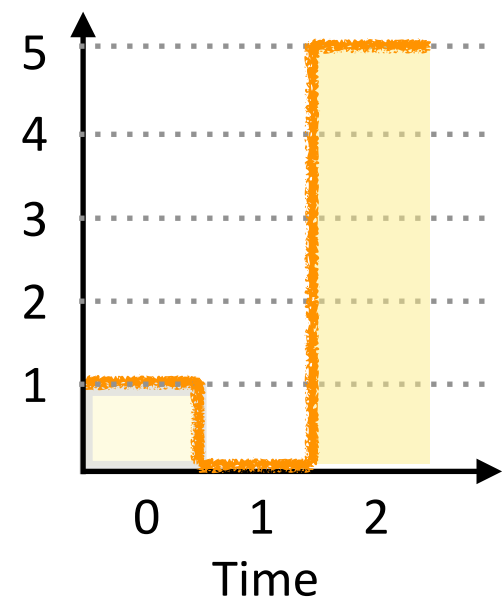
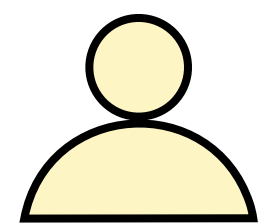
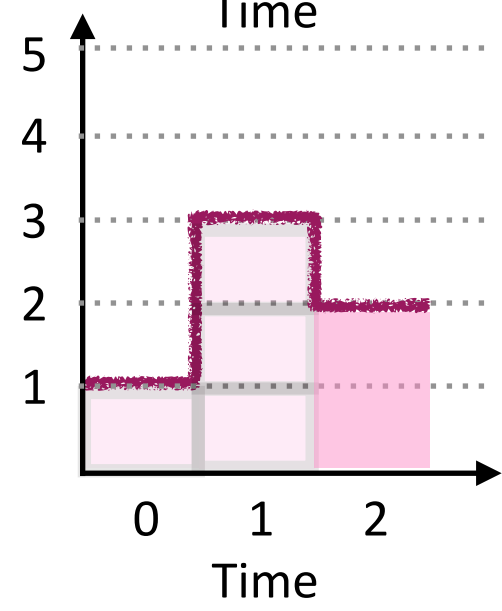
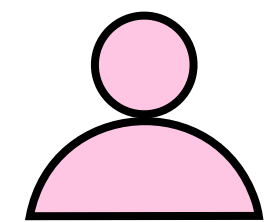
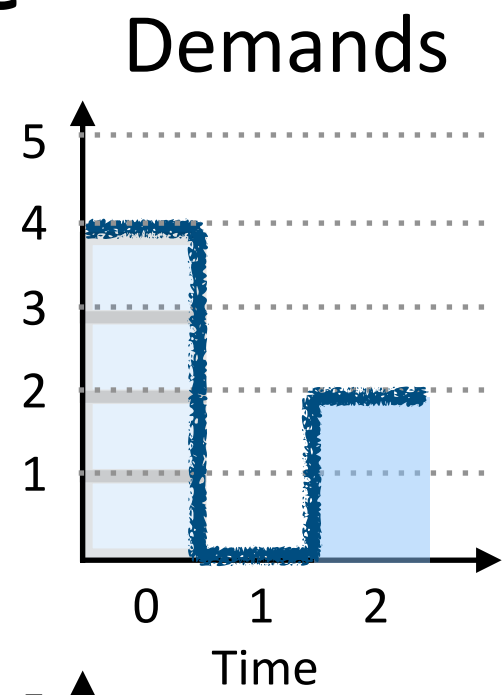
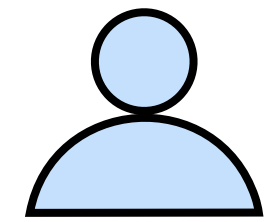


Fairness

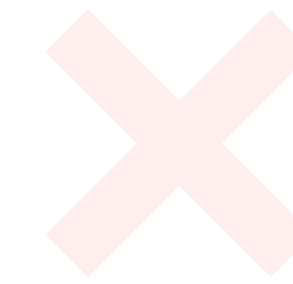
Max-min fairness applied periodically

Max-min fairness under dynamic demands: loses one or more of its properties 15

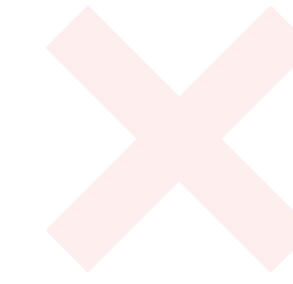
Running Example



Pareto efficiency



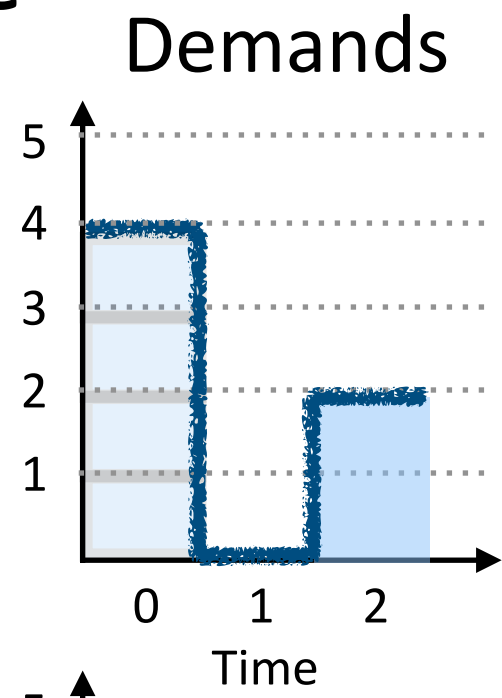
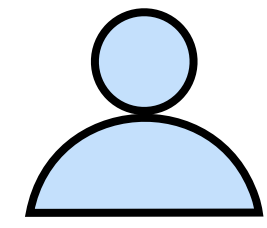
Strategy-proofness



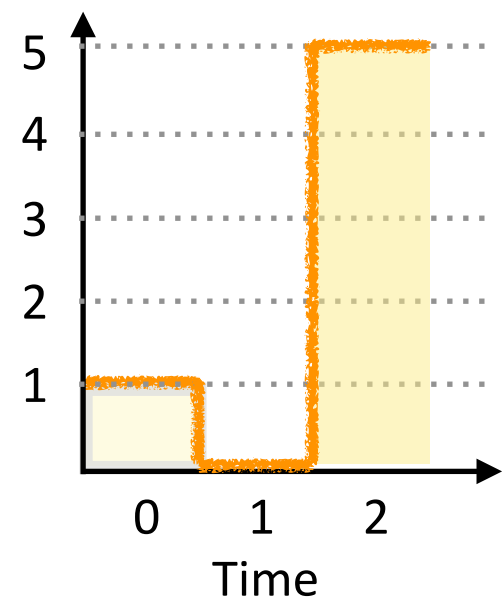
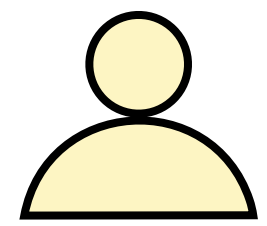
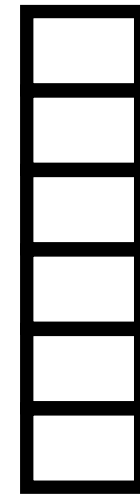
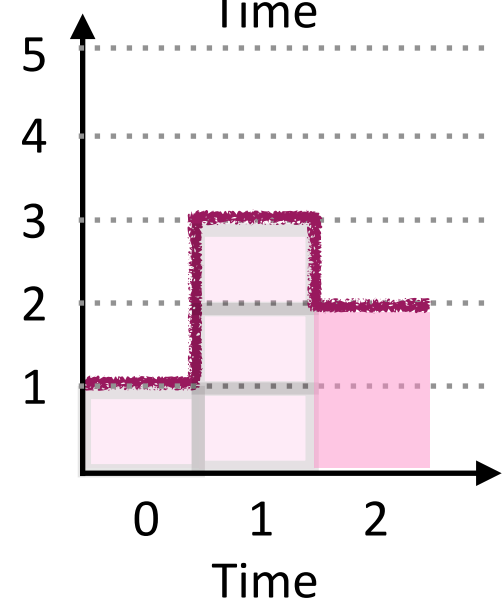
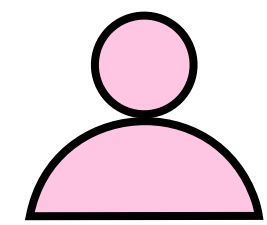
Fairness

Max-min fairness under dynamic demands: loses one or more of its properties 15

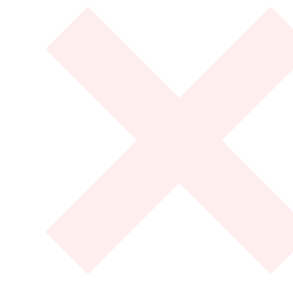
Running Example



Resource Pool



Pareto efficiency



Strategy-proofness



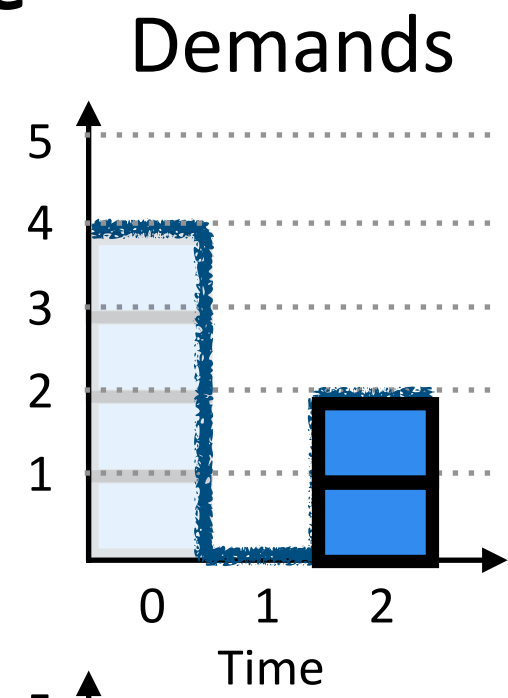
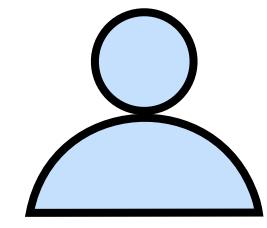
Fairness

Max-min fairness
based on demands at $t=0$

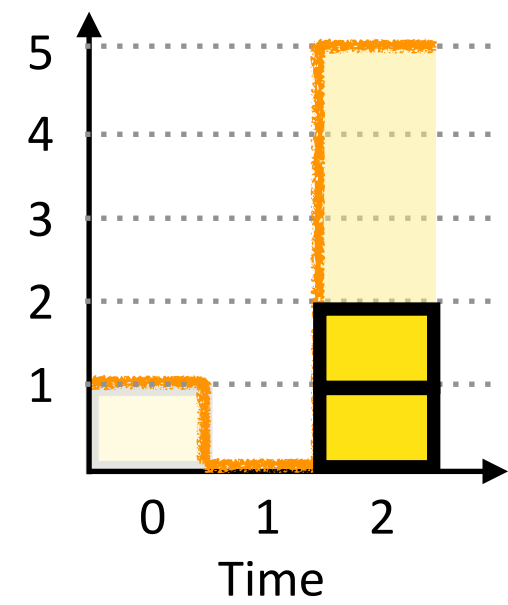
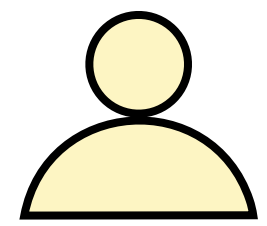
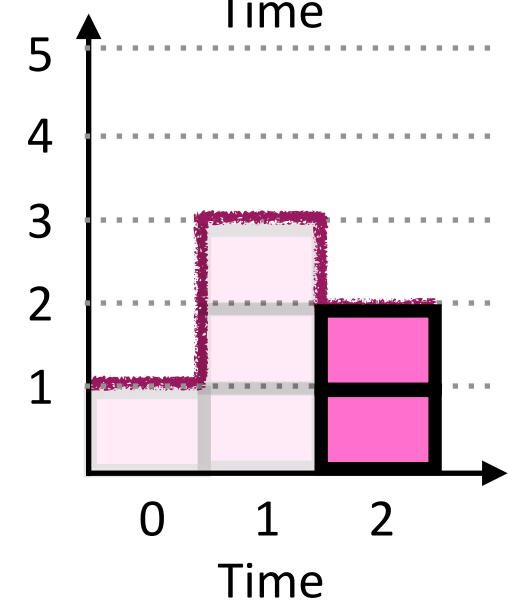
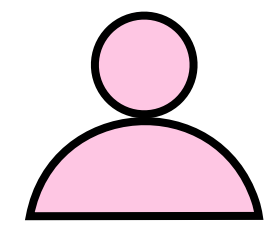
Max-min fairness
applied periodically

Max-min fairness under dynamic demands: loses one or more of its properties 16

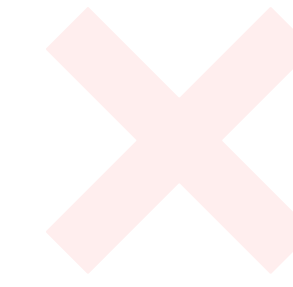
Running Example



Resource Pool



Pareto efficiency



Strategy-proofness



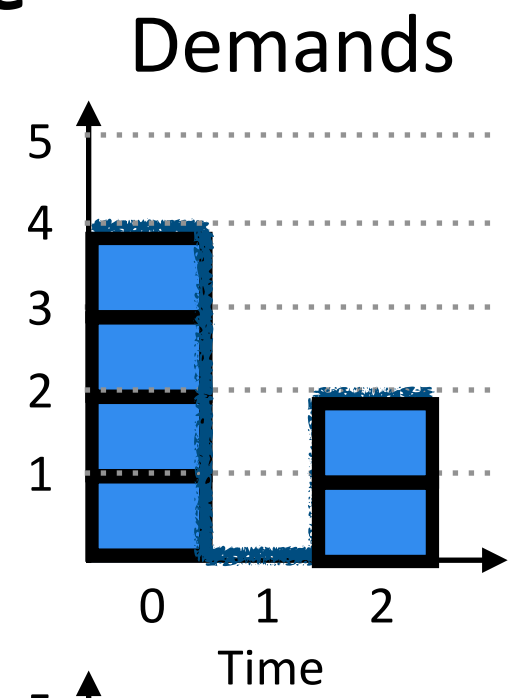
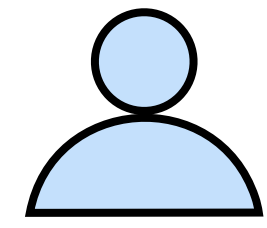
Fairness

Max-min fairness
based on demands at $t=0$

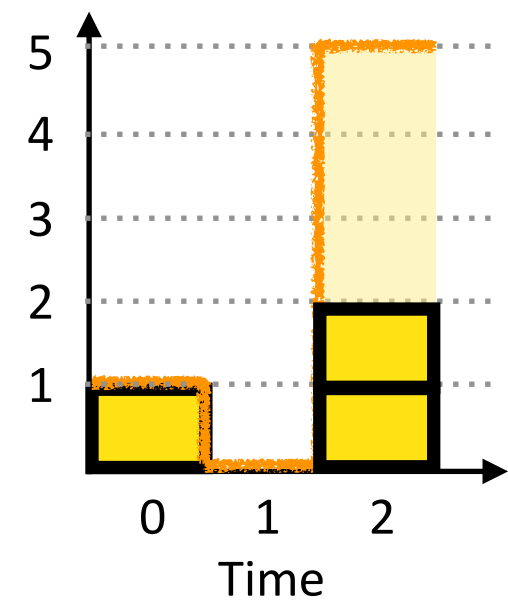
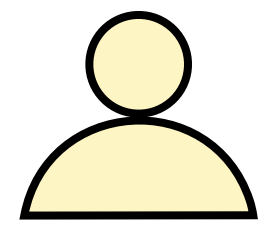
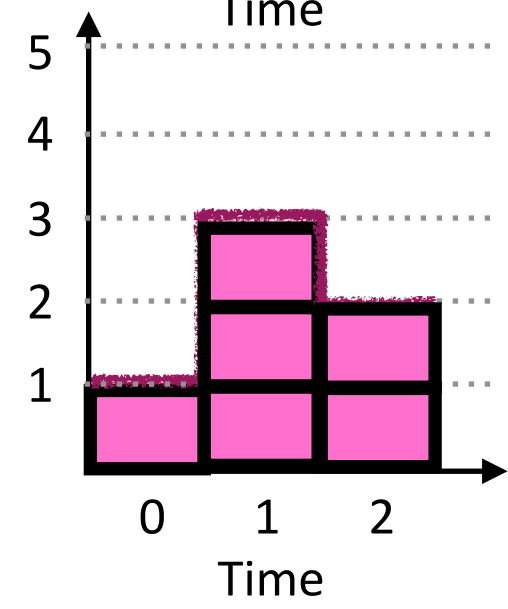
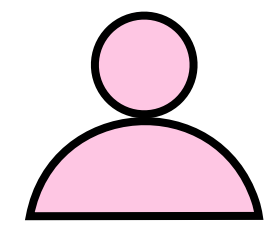
Max-min fairness
applied periodically

Max-min fairness under dynamic demands: loses one or more of its properties 17

Running Example



Resource Pool



Pareto efficiency



Strategy-proofness



Fairness

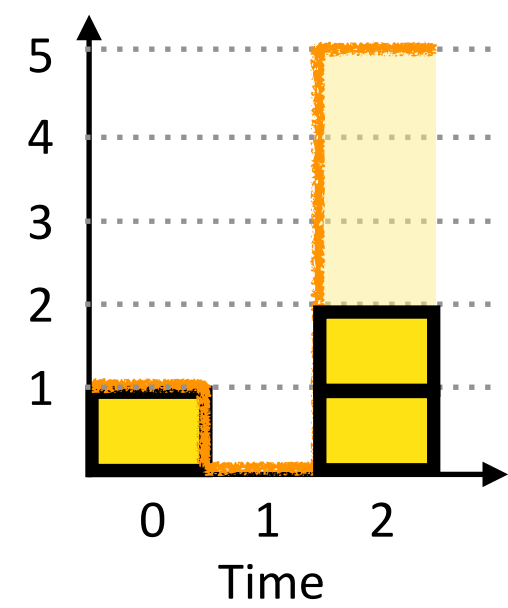
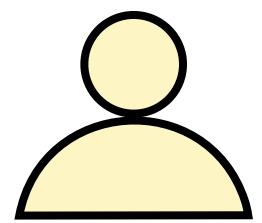
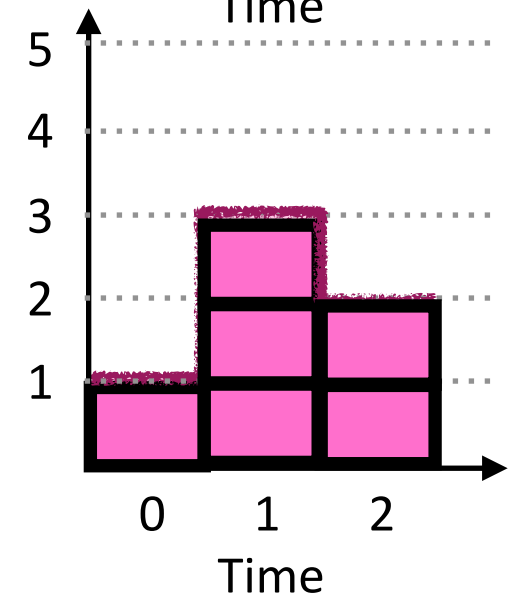
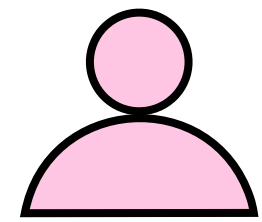
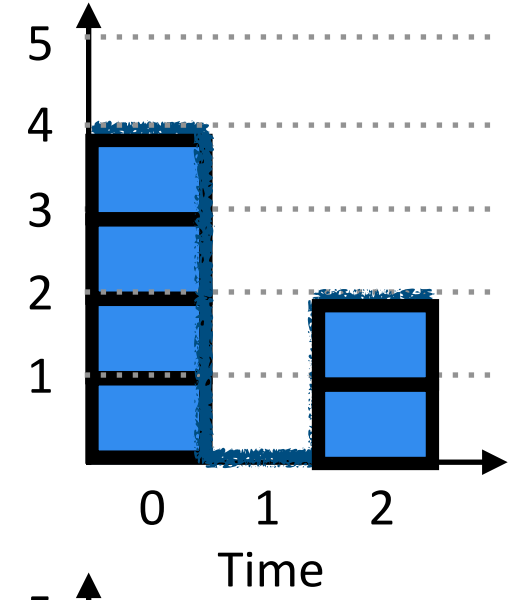
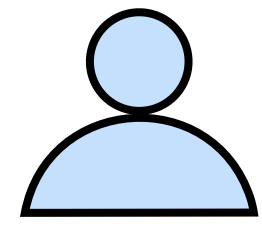
Max-min fairness
based on demands at $t=0$

Max-min fairness
applied periodically

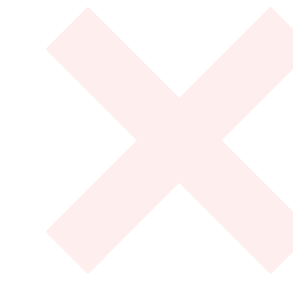
Max-min fairness under dynamic demands: loses one or more of its properties 18

Running Example

Demands Total Allocation



Pareto efficiency



Strategy-proofness



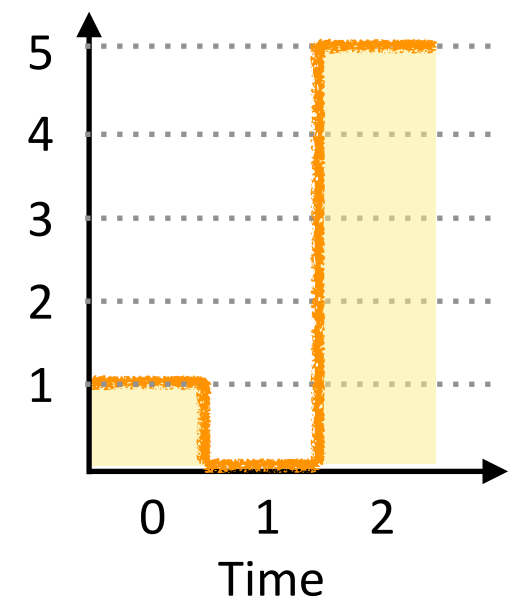
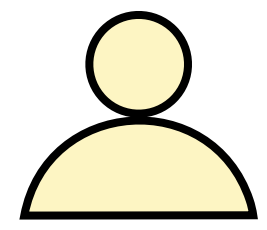
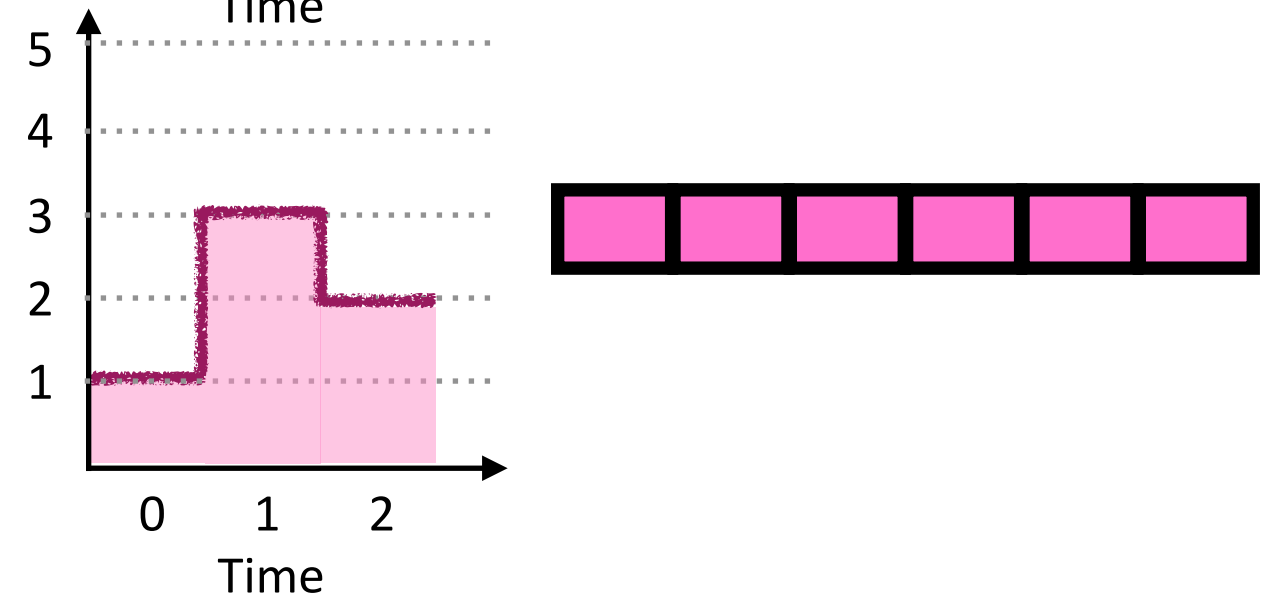
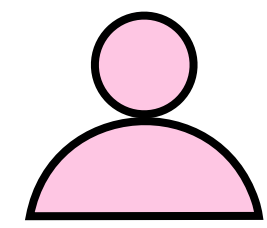
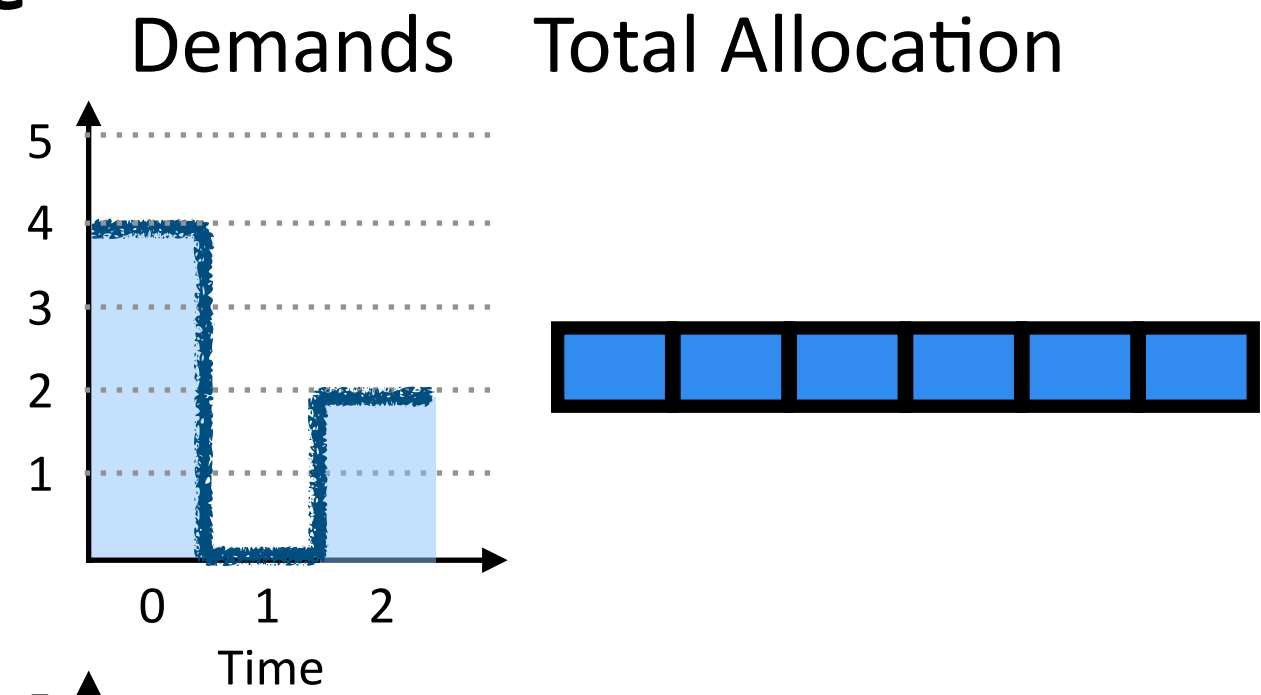
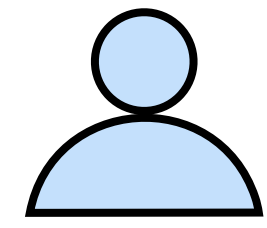
Fairness

Max-min fairness based on demands at $t=0$

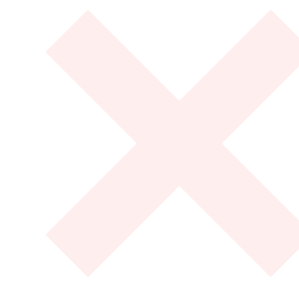
Max-min fairness applied periodically

Max-min fairness under dynamic demands: loses one or more of its properties 19

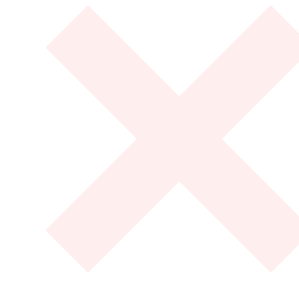
Running Example



Pareto efficiency



Strategy-proofness



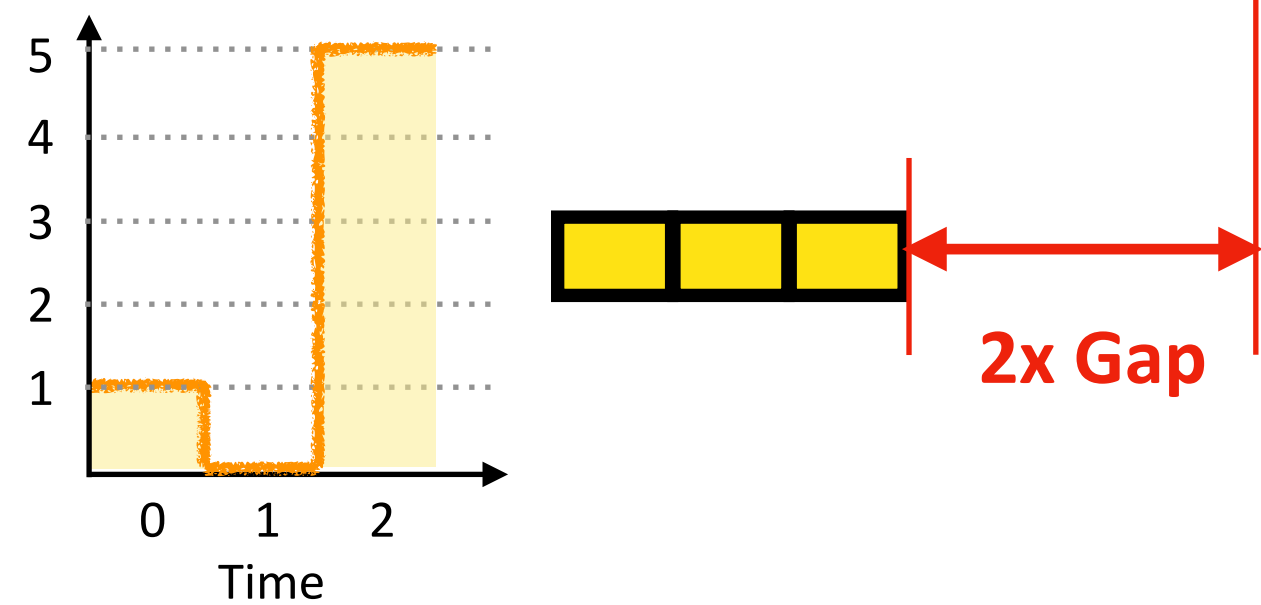
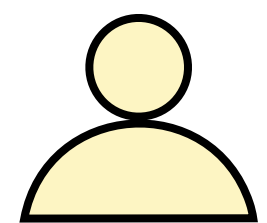
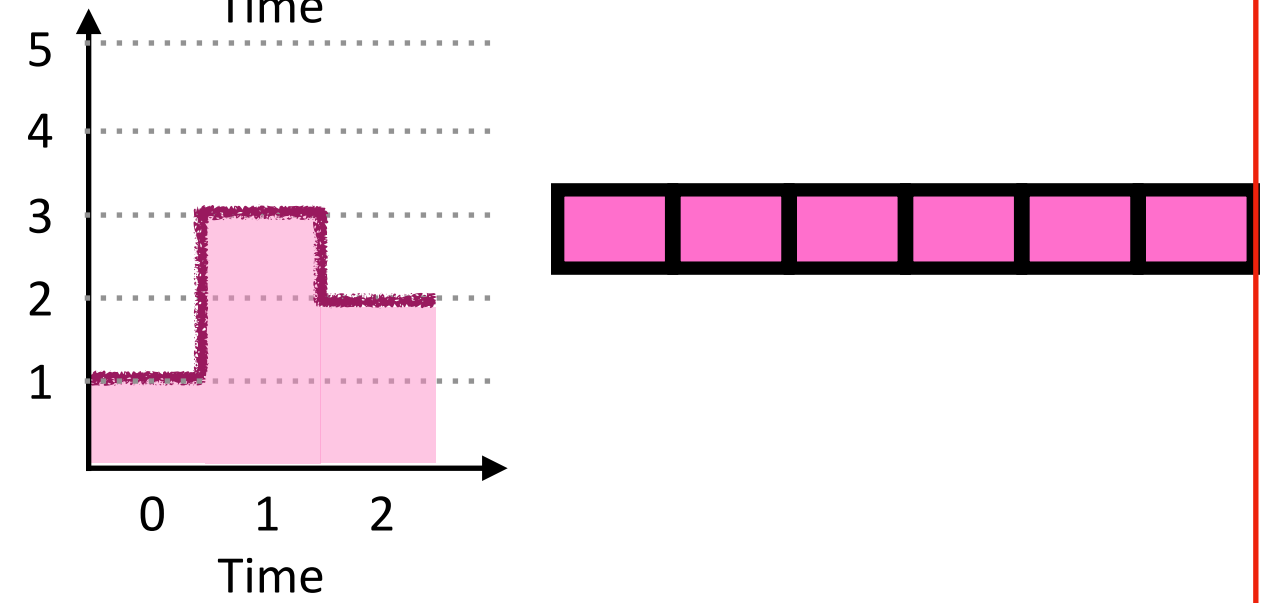
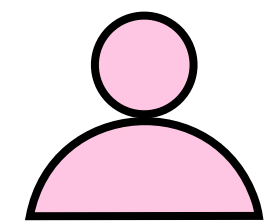
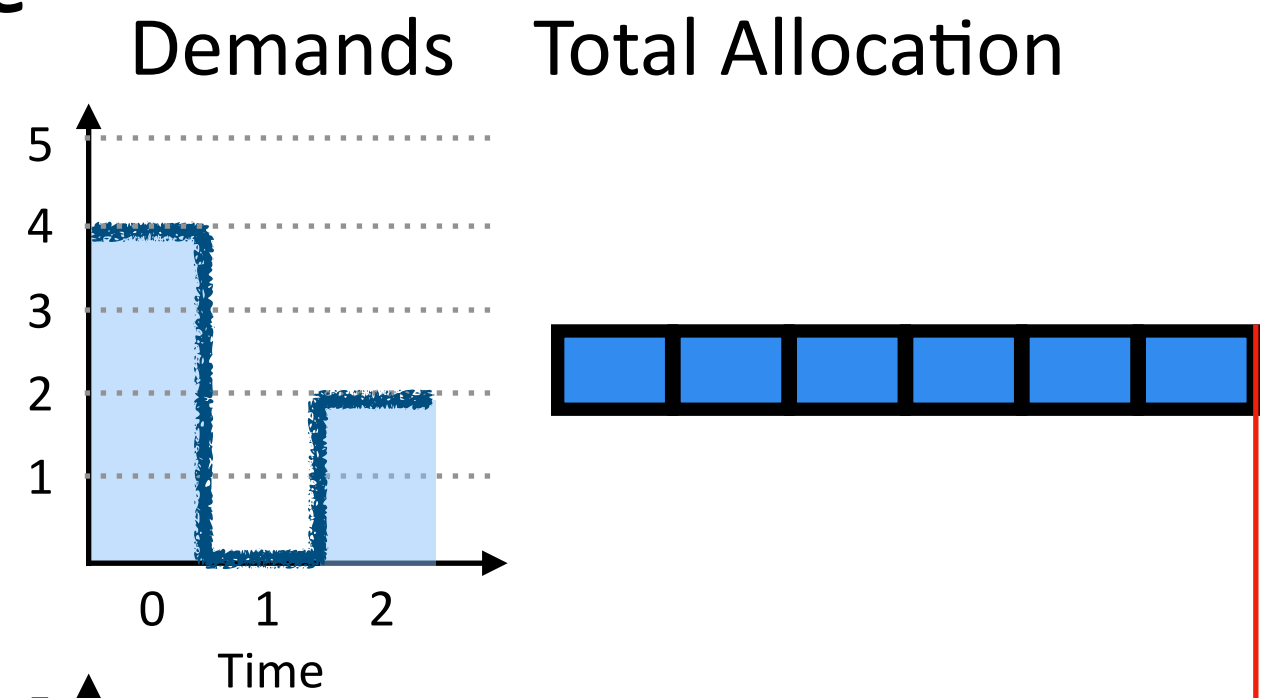
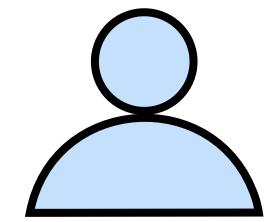
Fairness

Max-min fairness
based on demands at $t=0$

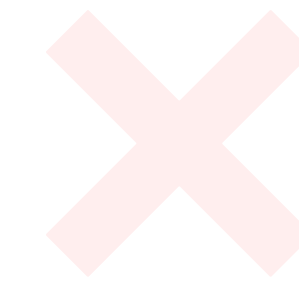
Max-min fairness
applied periodically

Max-min fairness under dynamic demands: loses one or more of its properties 19

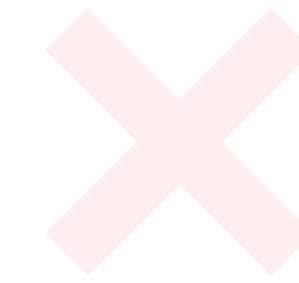
Running Example



Pareto efficiency



Strategy-proofness



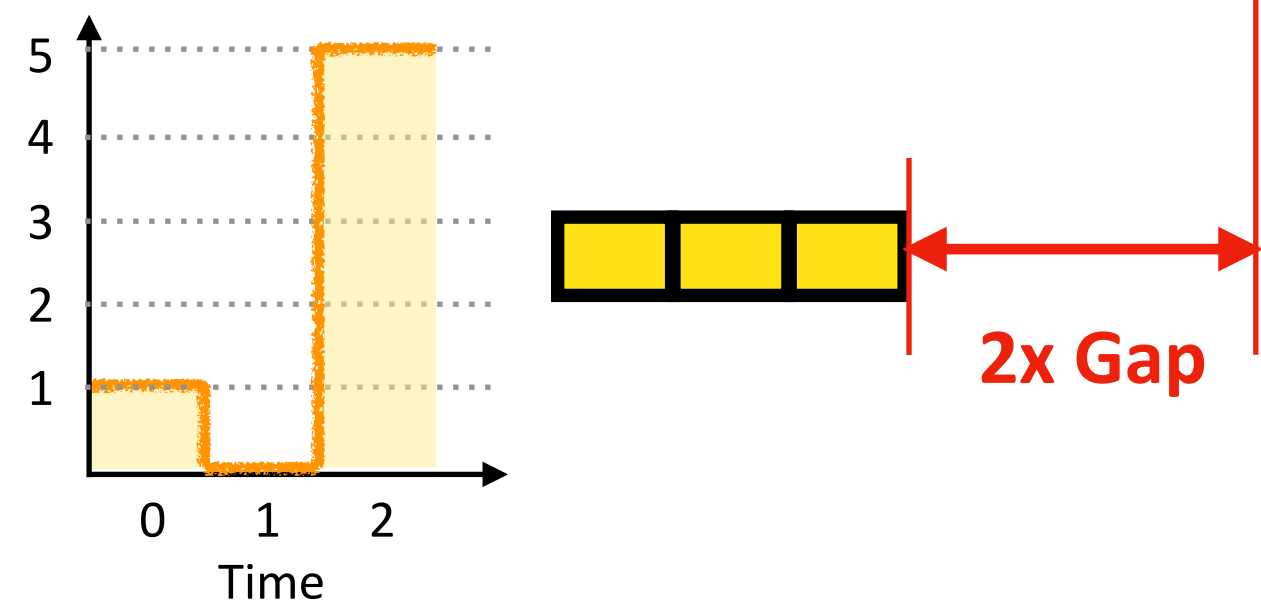
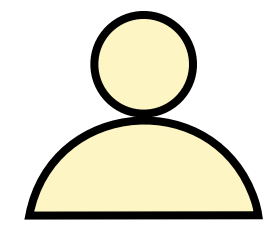
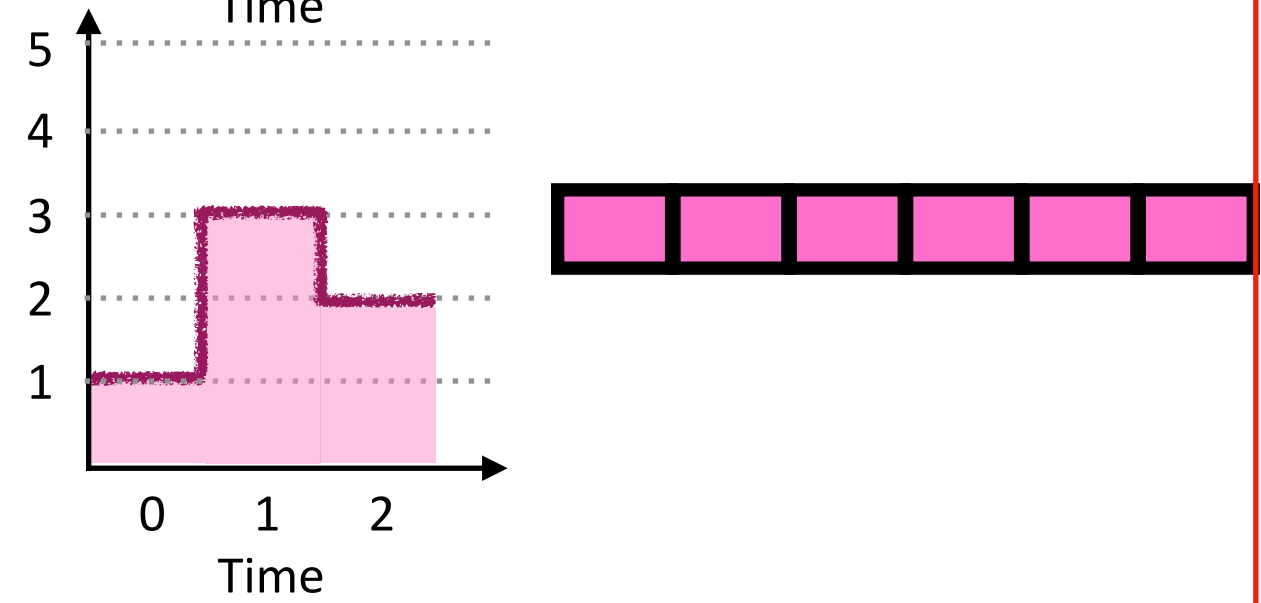
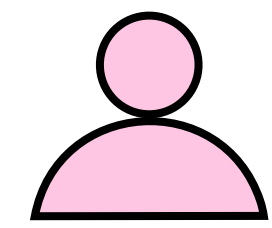
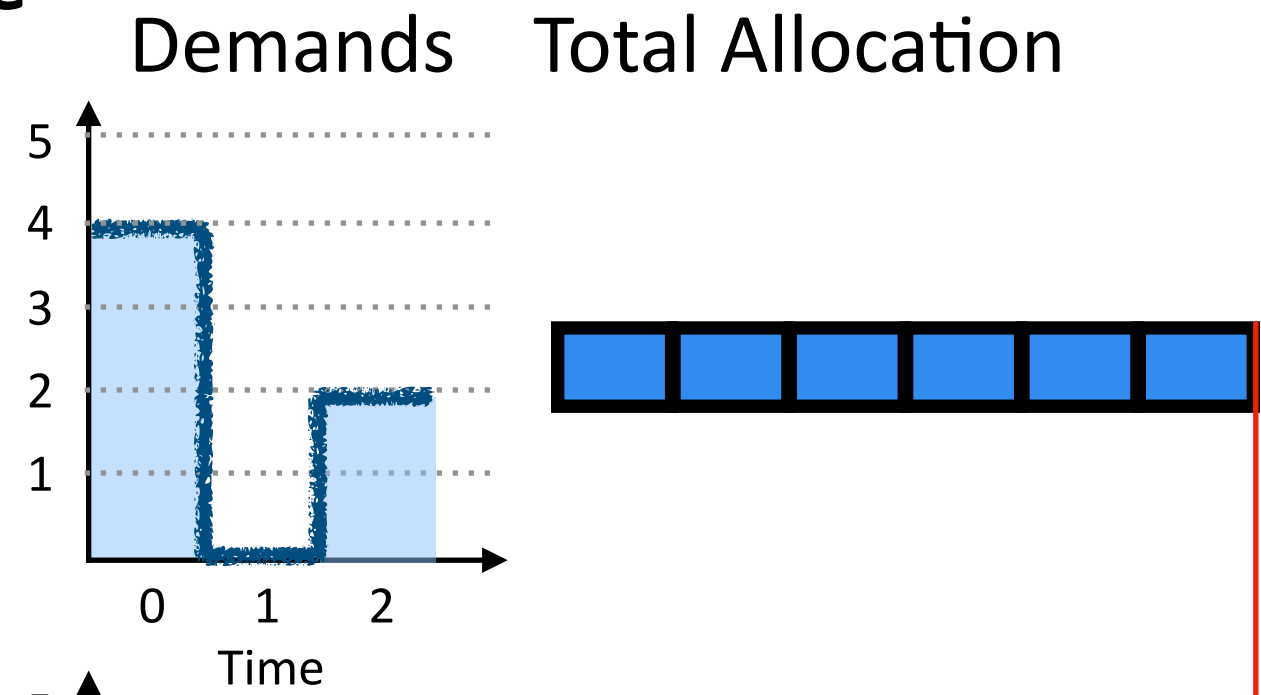
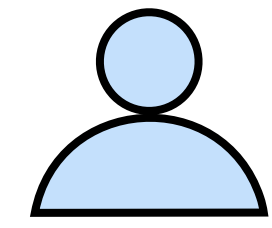
Fairness

Max-min fairness
based on demands at $t=0$

Max-min fairness
applied periodically

Max-min fairness under dynamic demands: loses one or more of its properties 19

Running Example

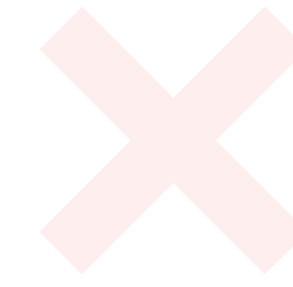


Max-min fairness
based on demands at t=0

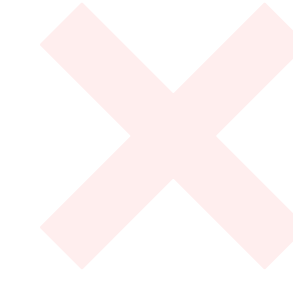
Max-min fairness
applied periodically



Pareto efficiency



Strategy-proofness

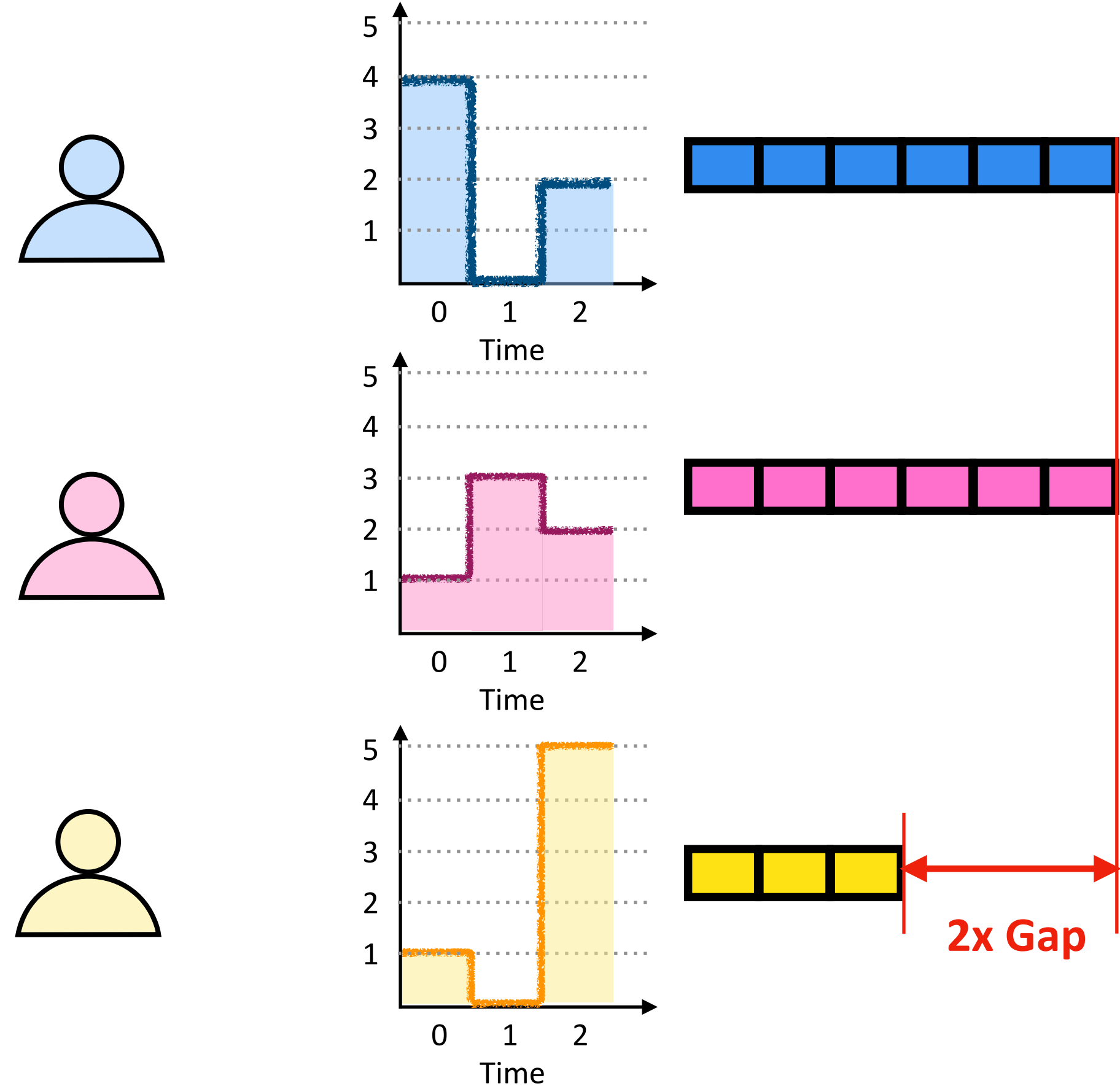


Fairness

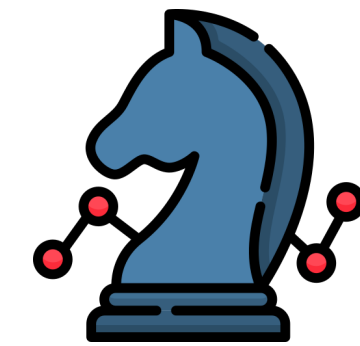
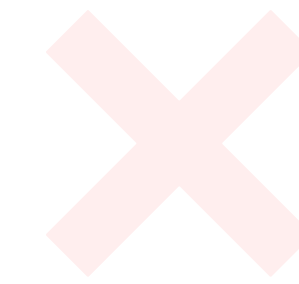
For n users, a user can get $\Omega(n)$ more allocation than others

Max-min fairness under dynamic demands: loses one or more of its properties 19

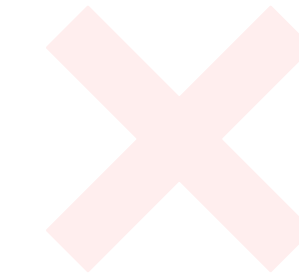
Running Example



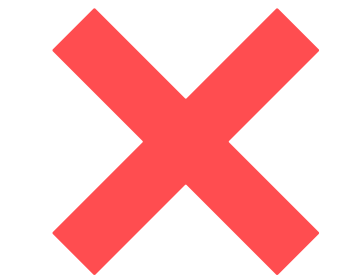
Pareto efficiency



Strategy-proofness



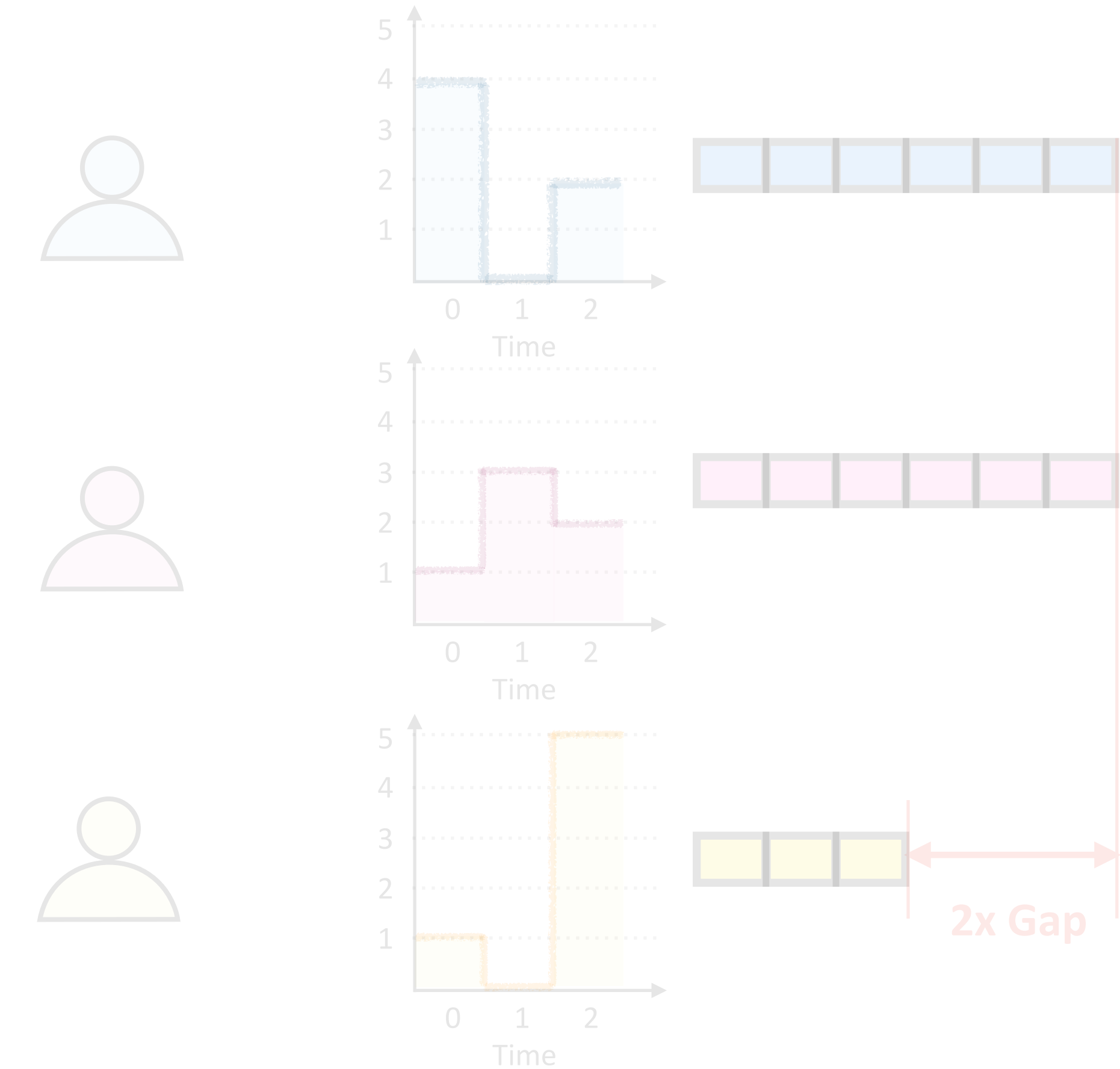
Fairness



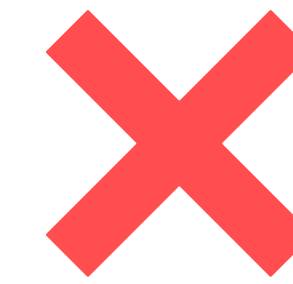
For n users, a user can get $\Omega(n)$ more allocation than others

Max-min fairness under dynamic demands: loses one or more of its properties 19

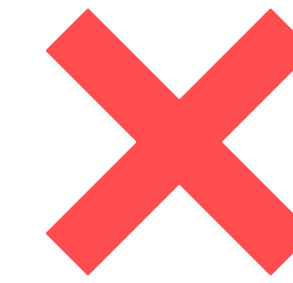
Running Example



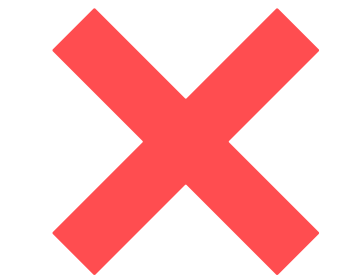
Pareto efficiency



Strategy-proofness



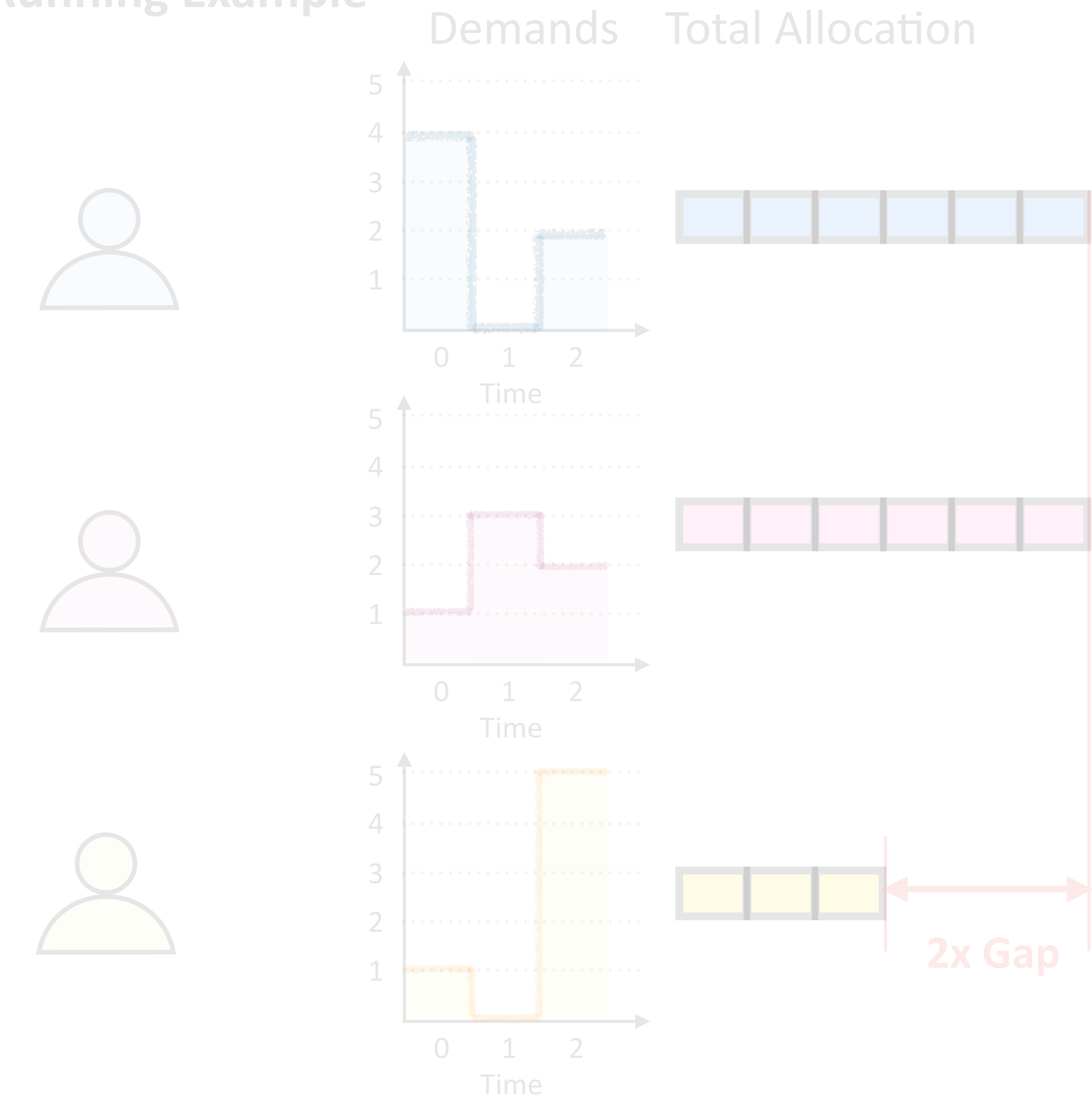
Fairness



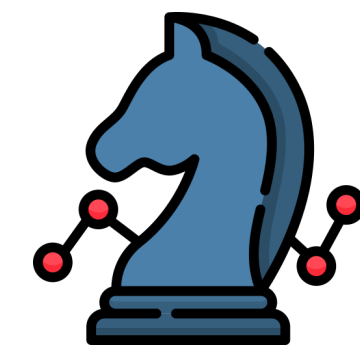
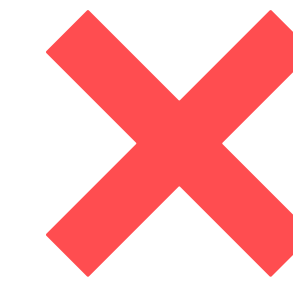
For n users, a user can get $\Omega(n)$ more allocation than others

Max-min fairness under dynamic demands: loses one or more of its properties 19

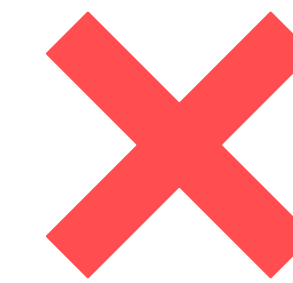
Running Example



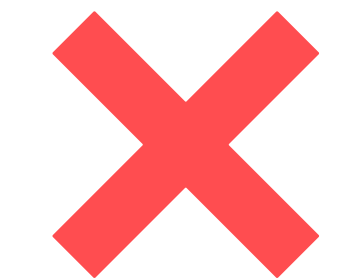
Pareto efficiency



Strategy-proofness



Fairness

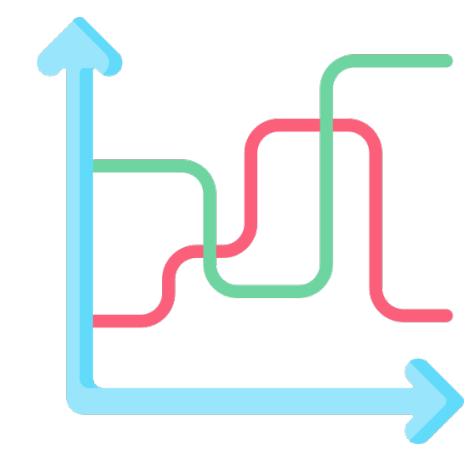


For n users, a user can get $\Omega(n)$ more allocation than others

Need to revisit classical resource allocation problem under dynamic demands

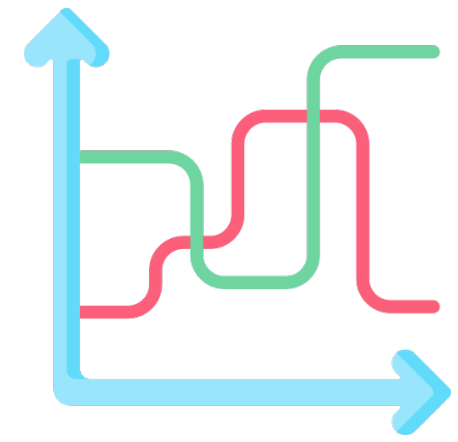
Karma: Revisiting the classical resource allocation problem under dynamic demands

Karma: Revisiting the classical resource allocation problem under dynamic demands

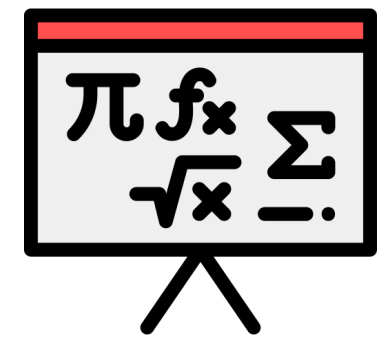


New resource allocation algorithm for dynamic demands

Karma: Revisiting the classical resource allocation problem under dynamic demands



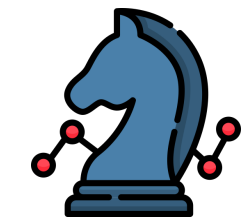
New resource allocation algorithm for dynamic demands



Theoretical guarantees



Pareto efficiency

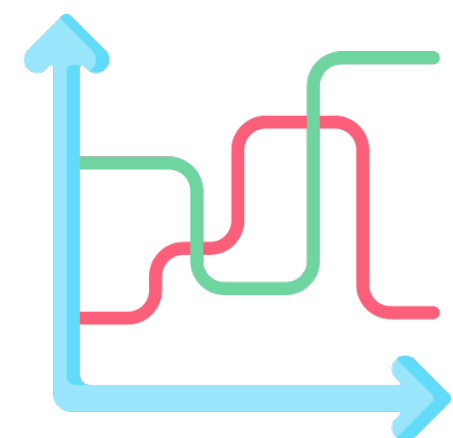


Strategy-proofness

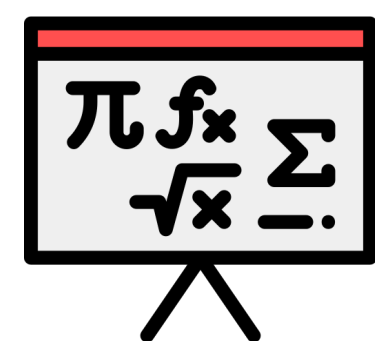


Fairness

Karma: Revisiting the classical resource allocation problem under dynamic demands



New resource allocation algorithm for dynamic demands



Theoretical guarantees



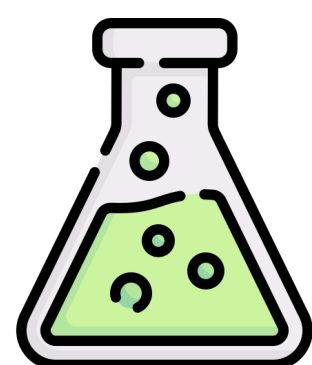
Pareto efficiency



Strategy-proofness

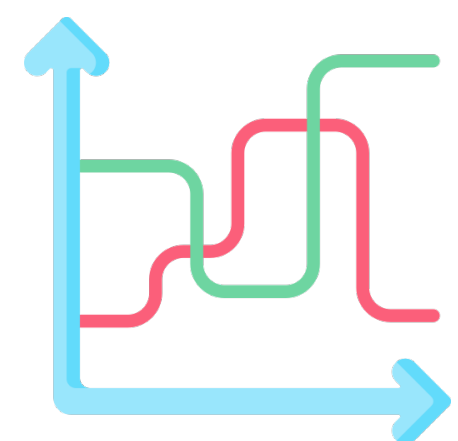


Fairness

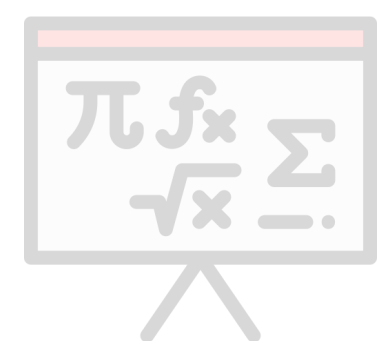


Prototype implementation and evaluation

Karma: Revisiting the classical resource allocation problem under dynamic demands



New resource allocation algorithm for dynamic demands



Theoretical guarantees



Pareto efficiency



Strategy-proofness

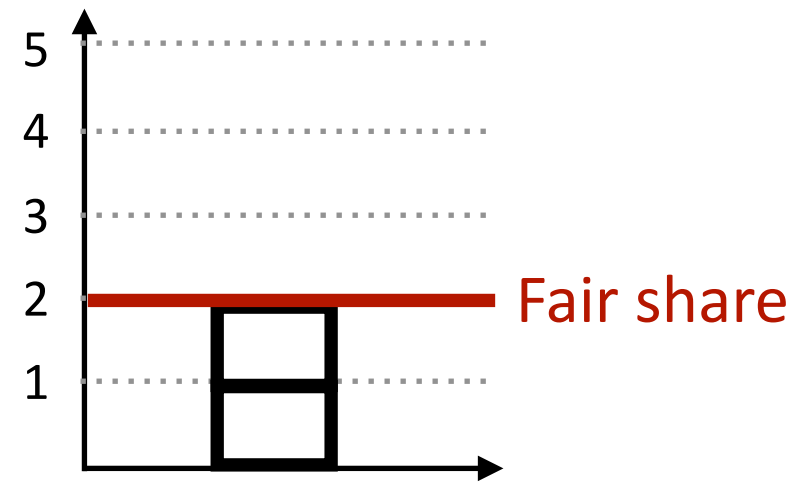
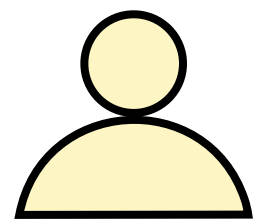
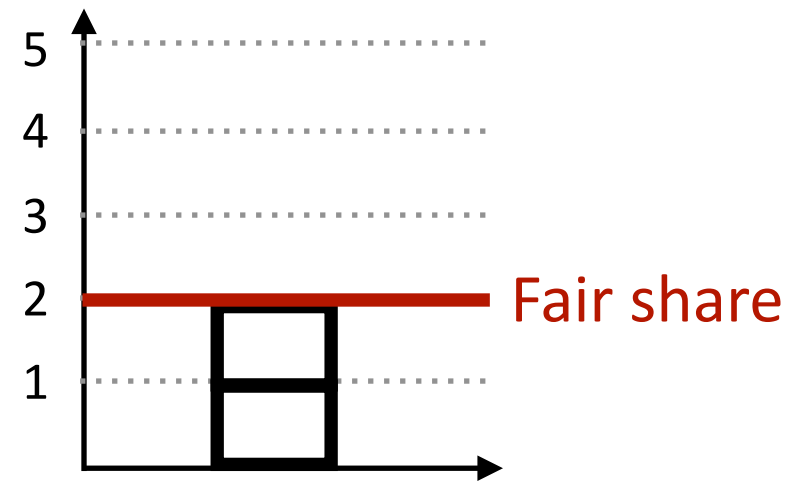
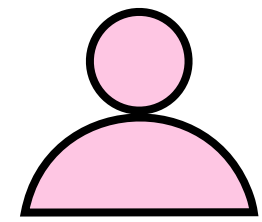
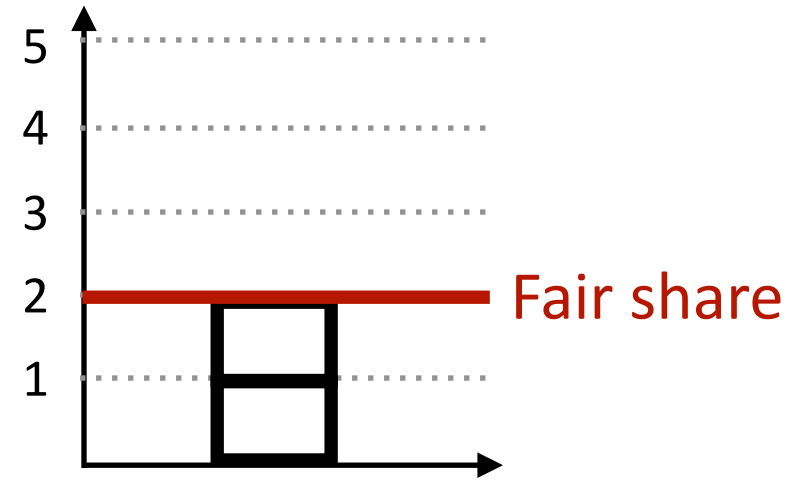
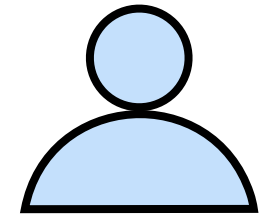


Fairness

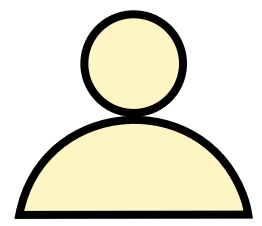
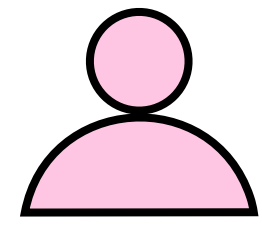
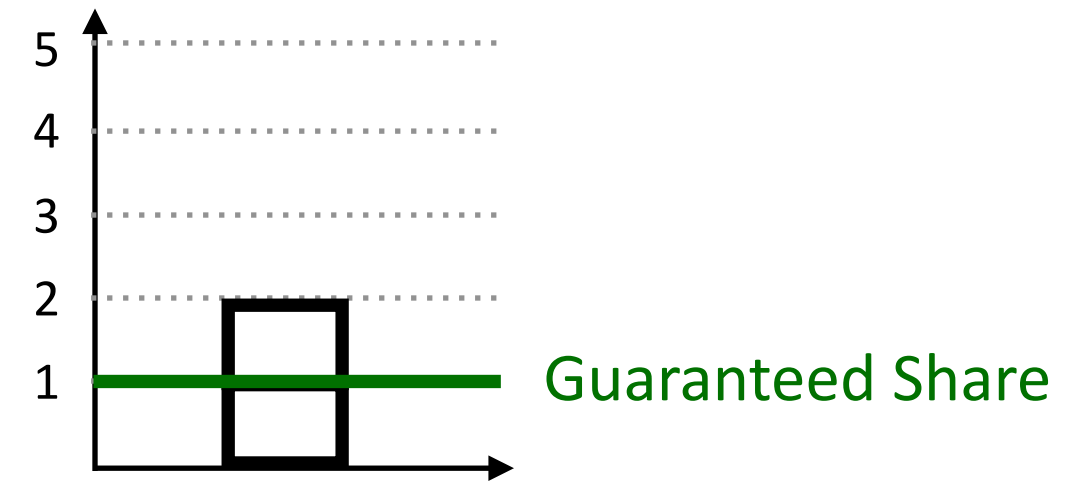
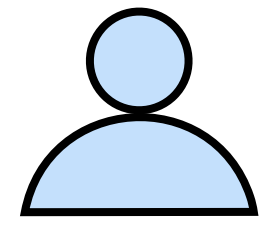


Prototype implementation and evaluation

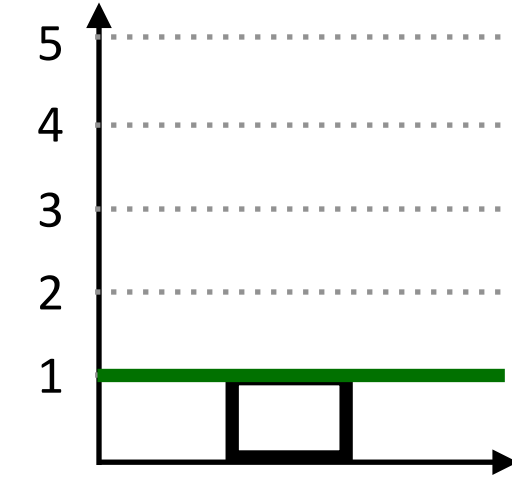
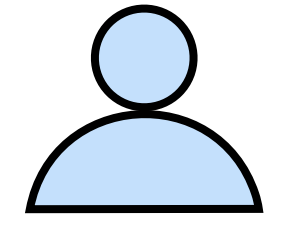
Karma key idea #1: *donated slices* and *shared slices*



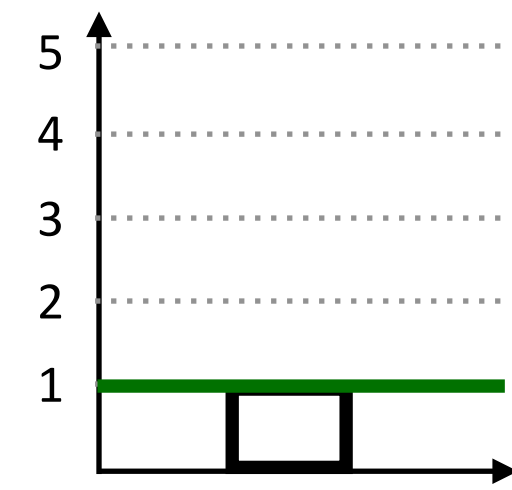
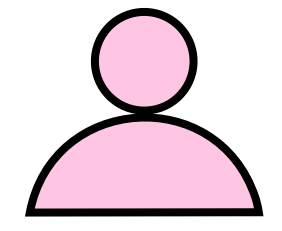
Karma key idea #1: *donated slices* and *shared slices*



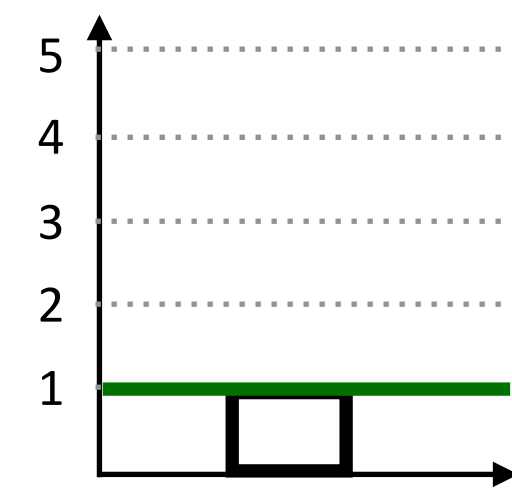
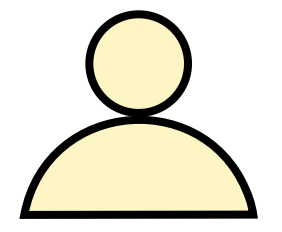
Karma key idea #1: *donated slices* and *shared slices*



Guaranteed Share

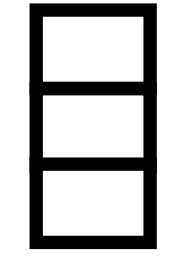


Guaranteed Share

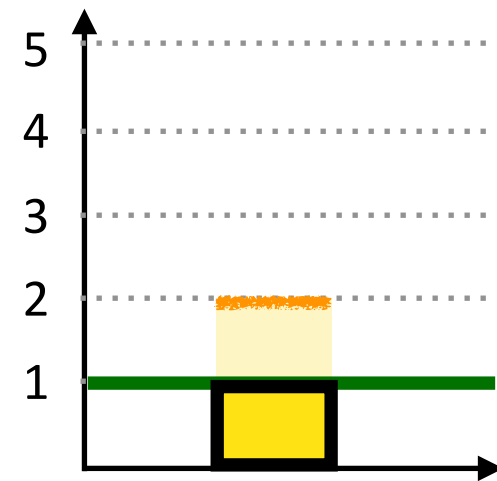
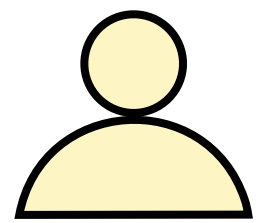
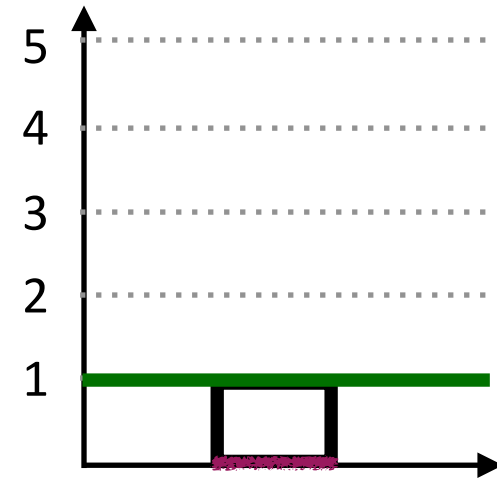
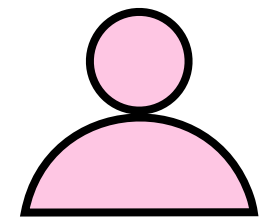
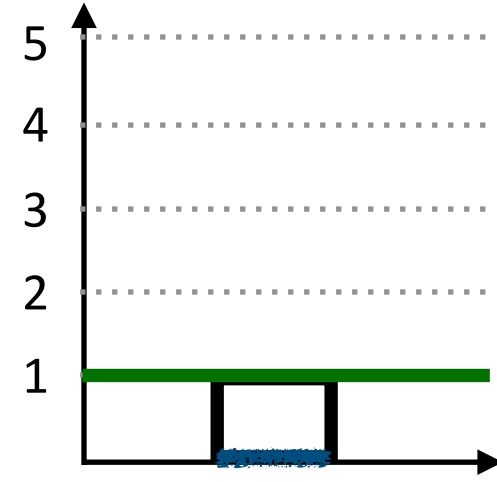
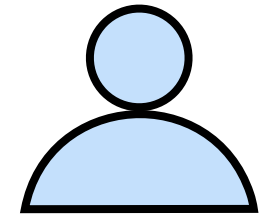


Guaranteed Share

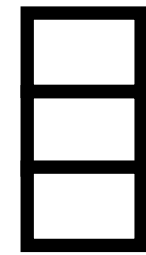
Shared Slices



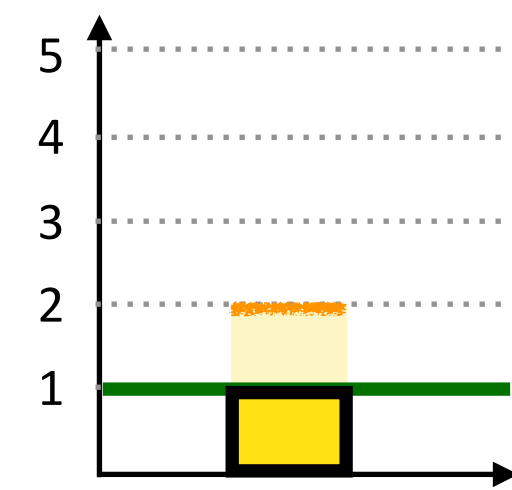
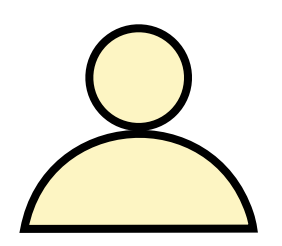
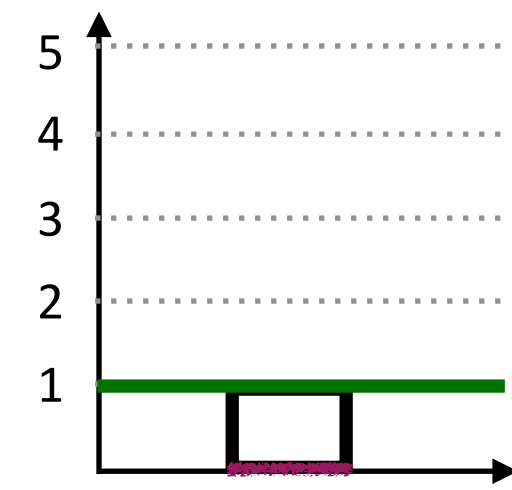
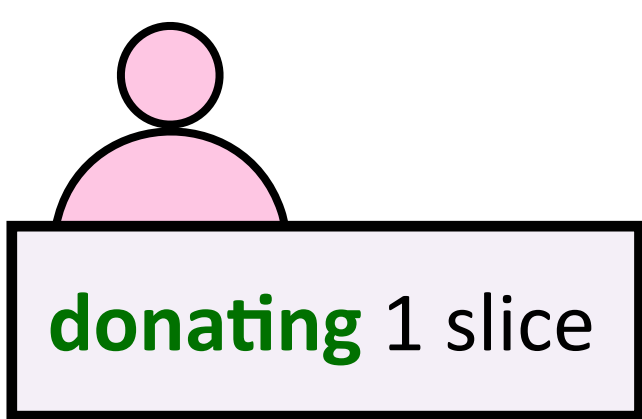
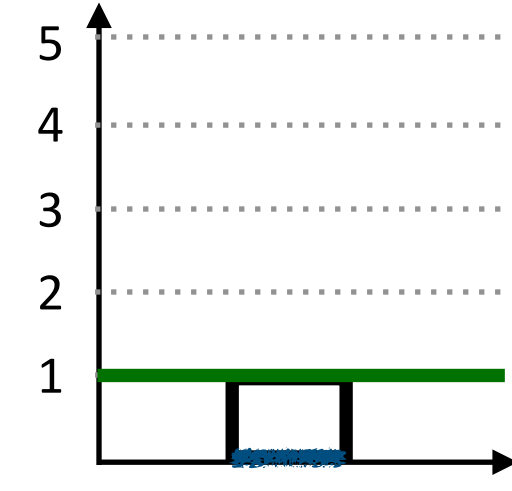
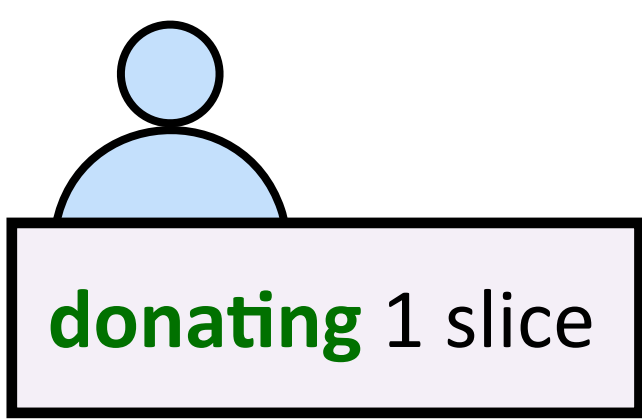
Karma key idea #1: *donated slices* and *shared slices*



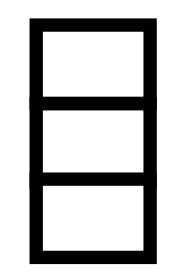
Shared Slices



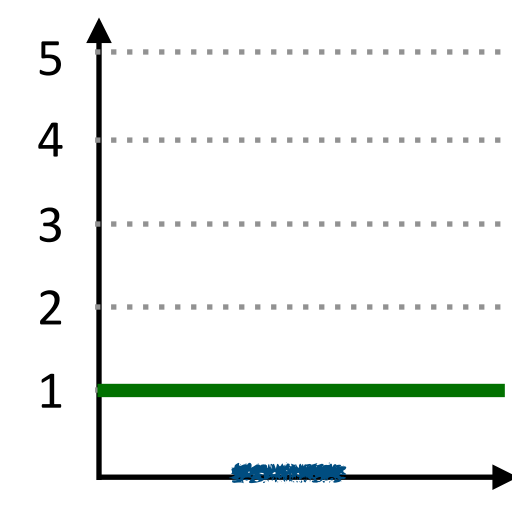
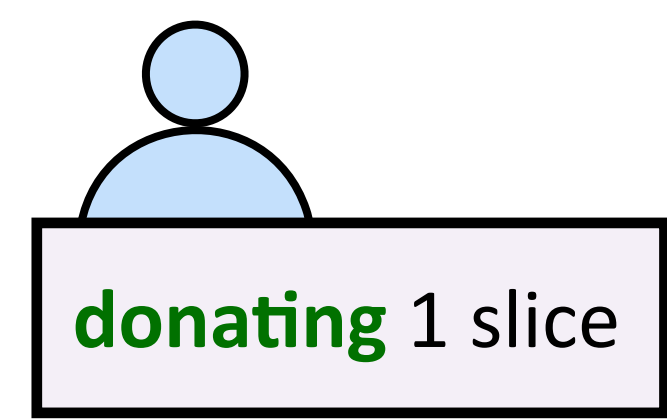
Karma key idea #1: *donated slices* and *shared slices*



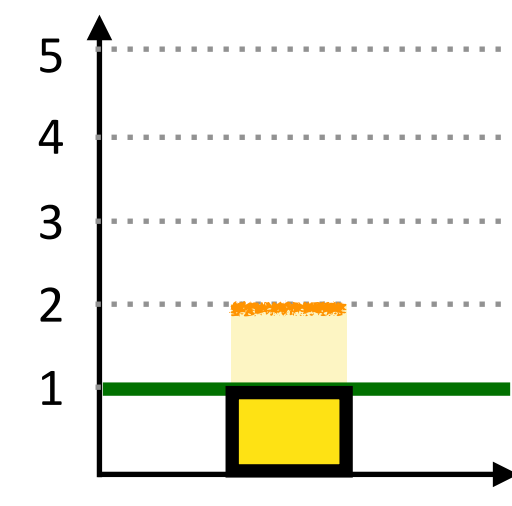
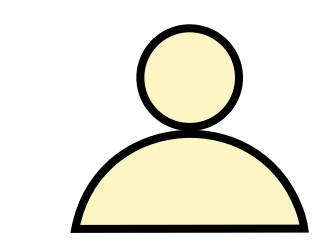
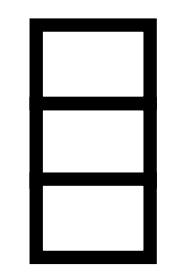
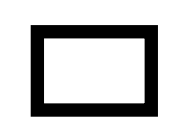
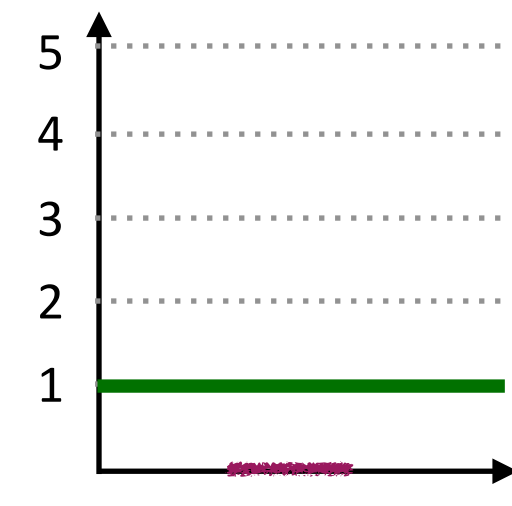
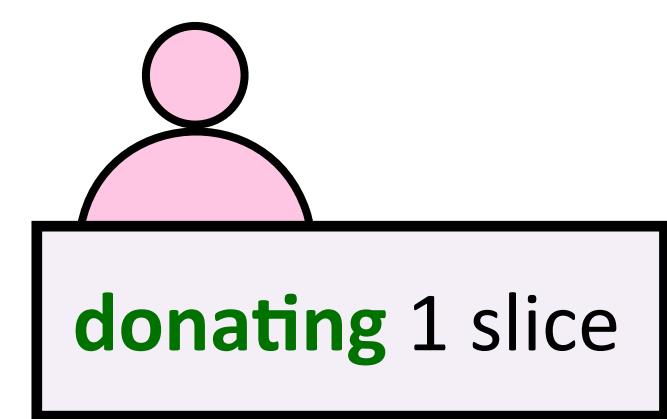
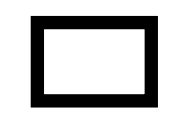
Shared Slices



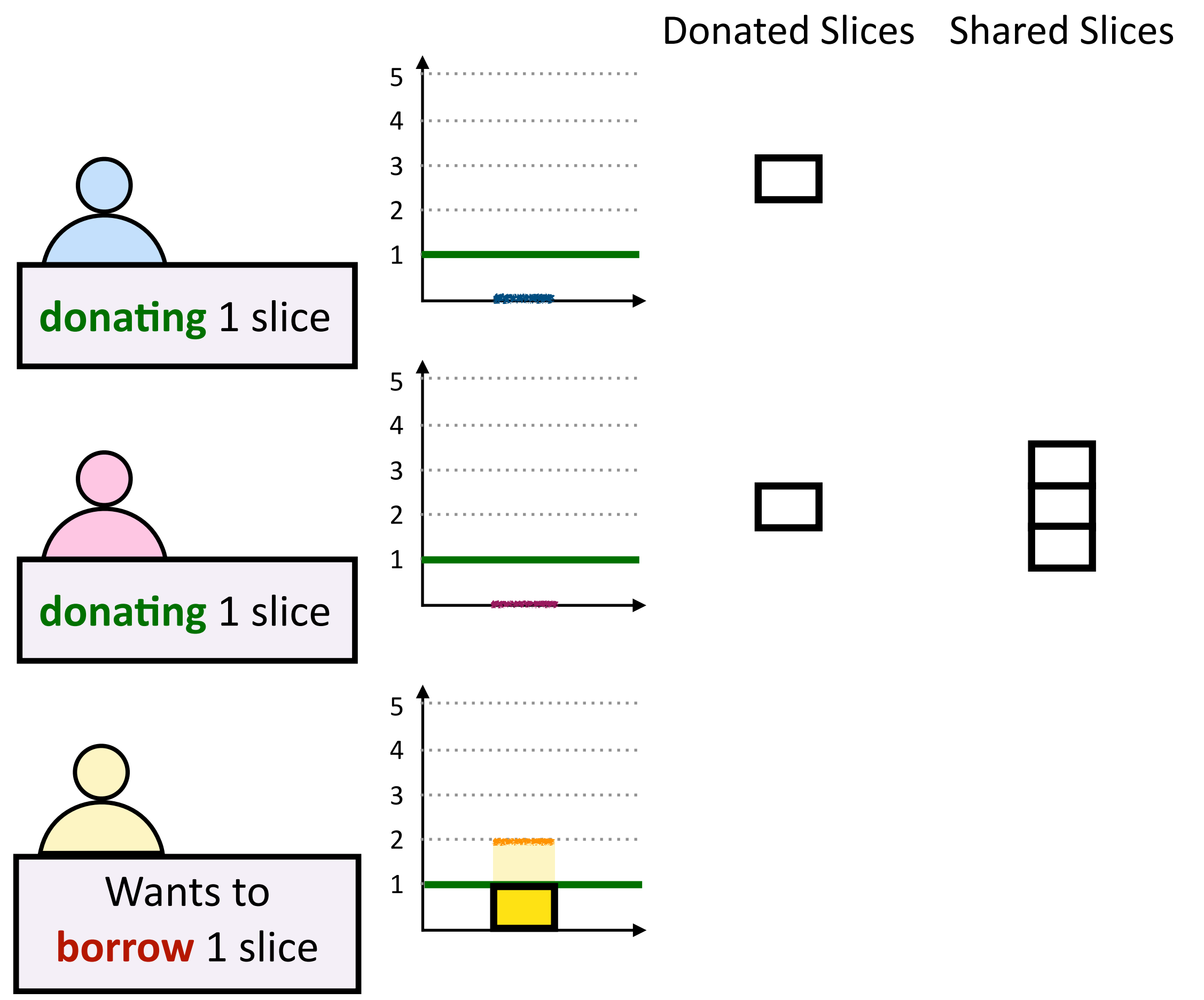
Karma key idea #1: *donated slices* and *shared slices*



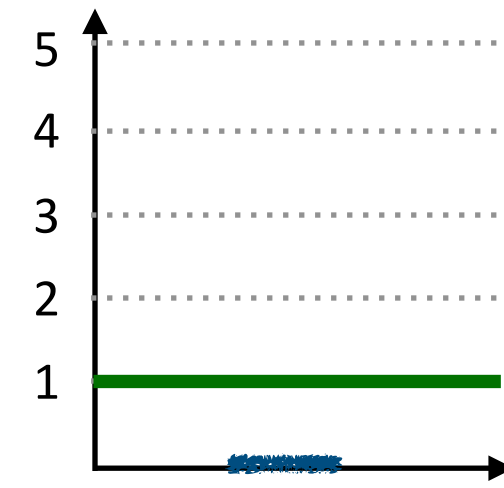
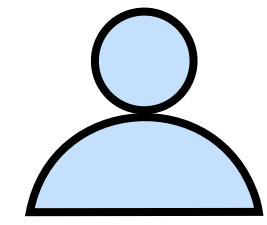
Donated Slices Shared Slices



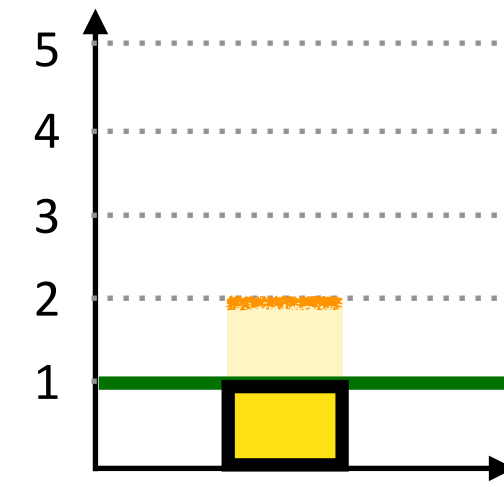
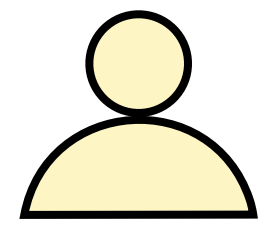
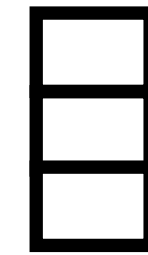
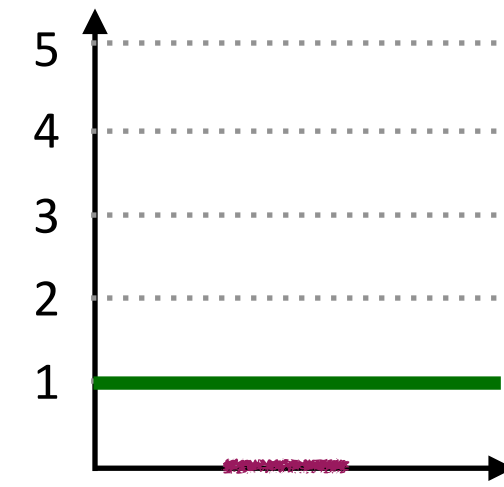
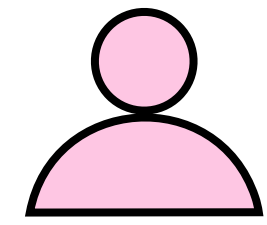
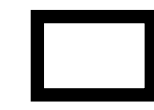
Karma key idea #1: *donated slices* and *shared slices*



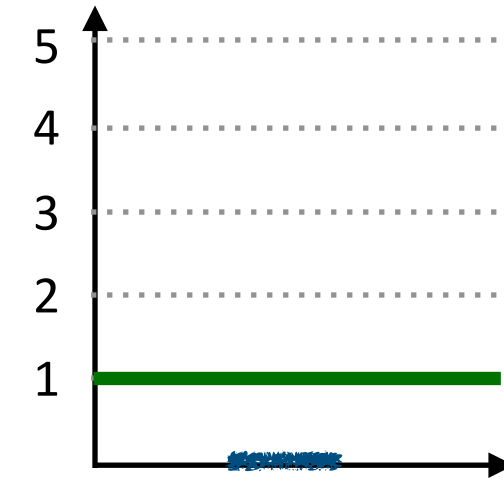
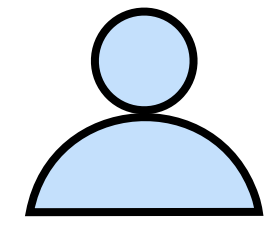
Karma key idea #2: "credits" for resource allocation



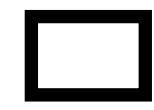
Donated Slices Shared Slices



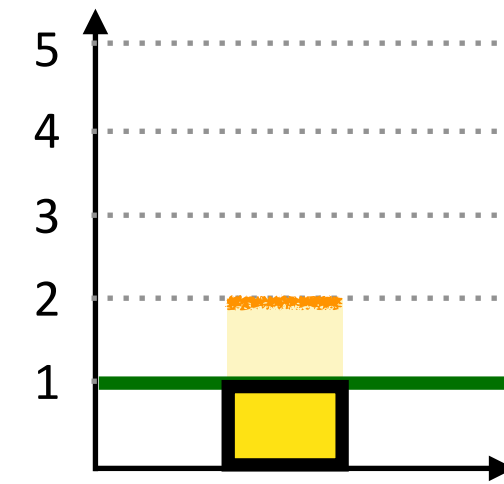
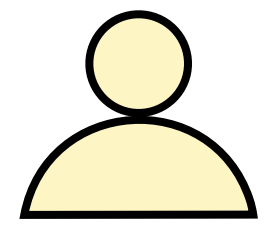
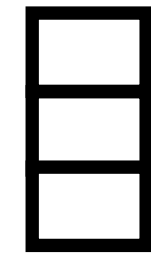
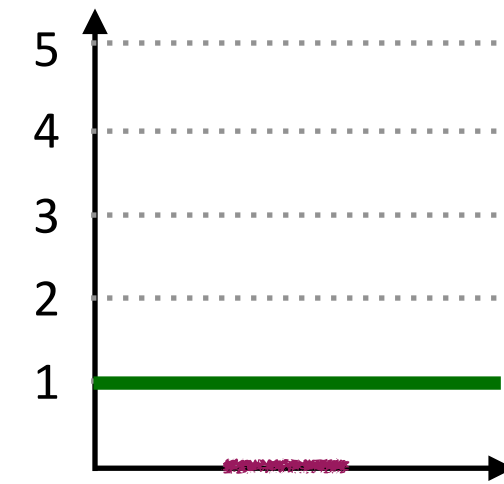
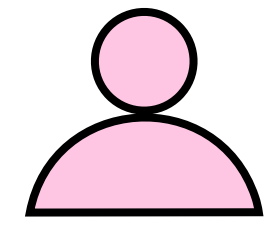
Karma key idea #2: "credits" for resource allocation



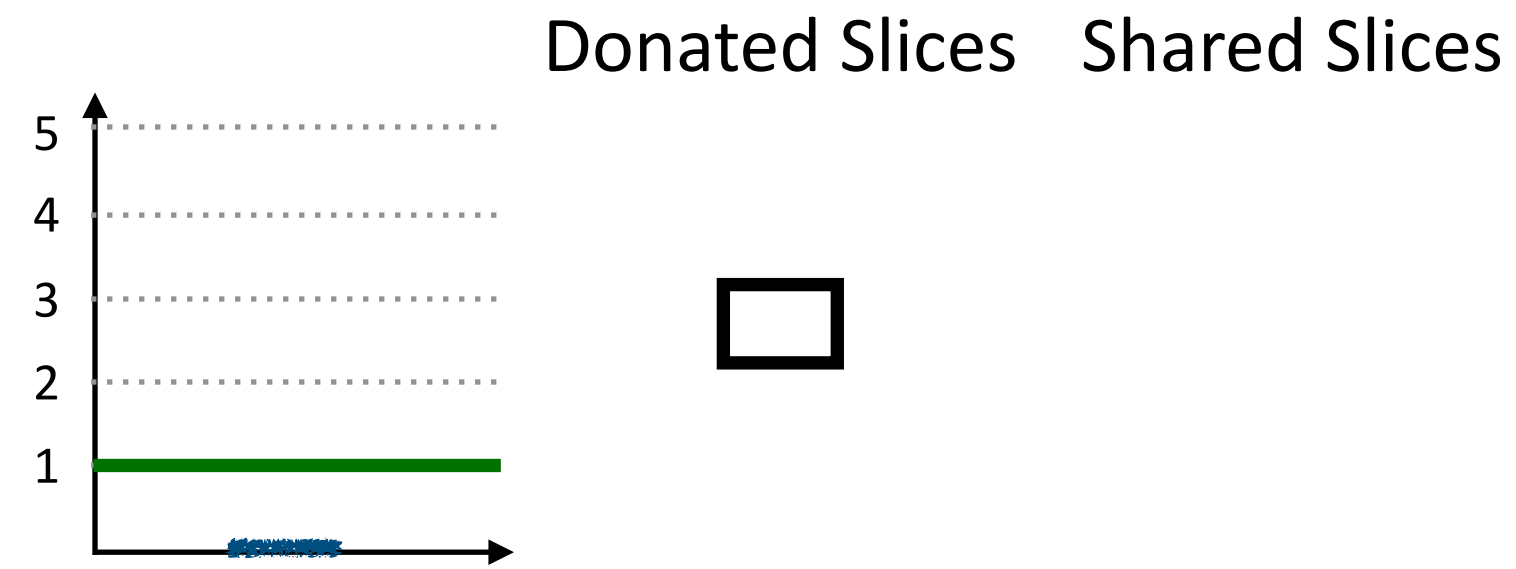
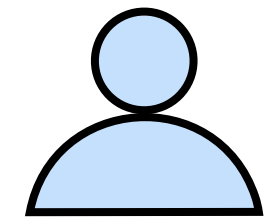
Donated Slices Shared Slices



-1 credit for **borrowing** a slice

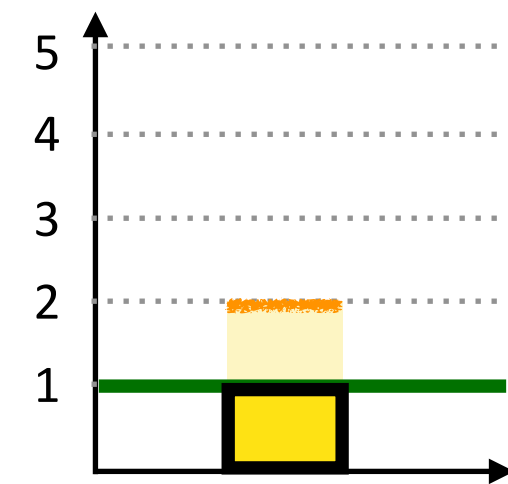
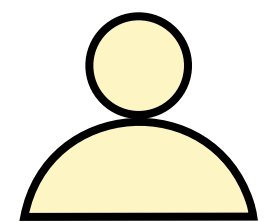
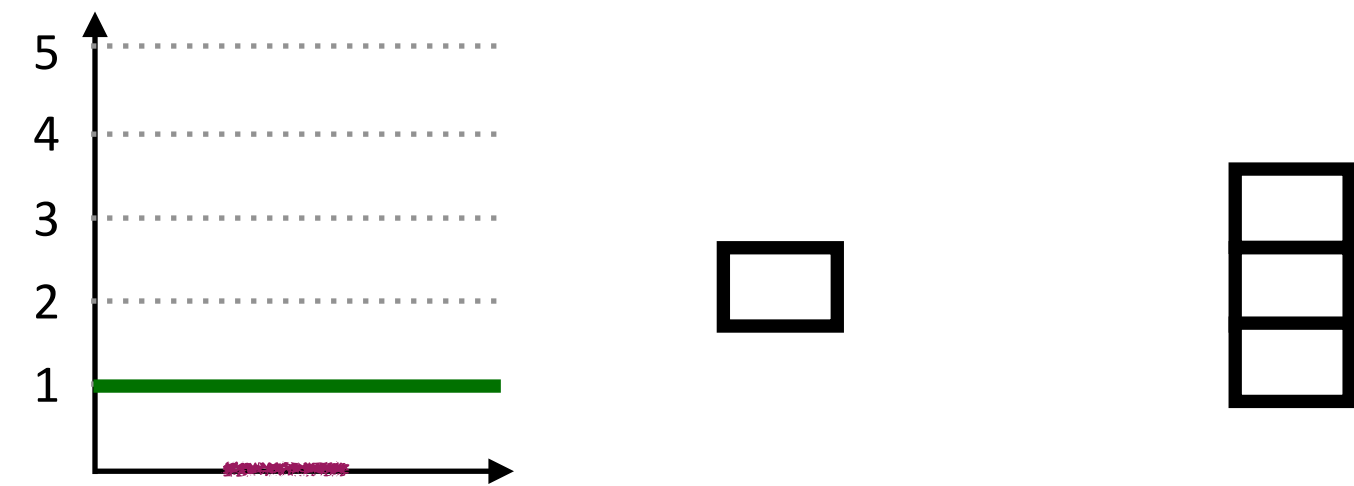
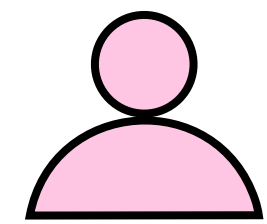


Karma key idea #2: "credits" for resource allocation

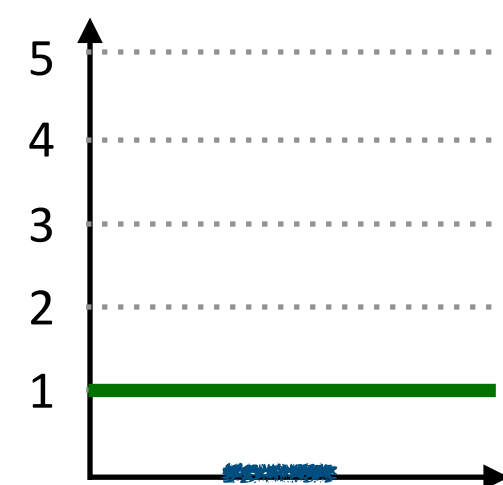
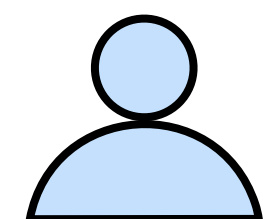


-1 credit for **borrowing** a slice

+1 credit if a **donated** slice is borrowed



Karma key idea #2: “credits” for resource allocation



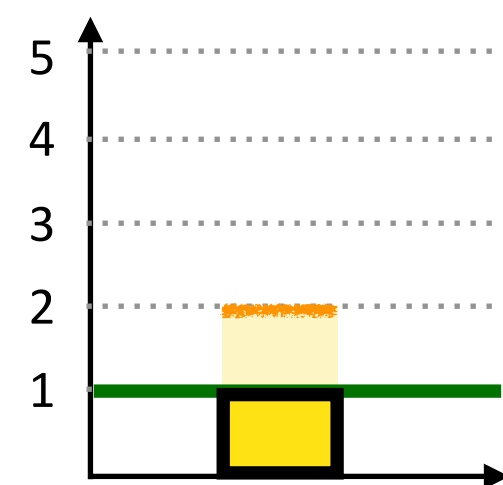
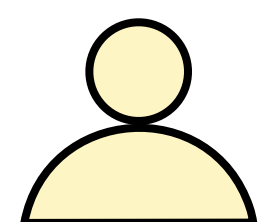
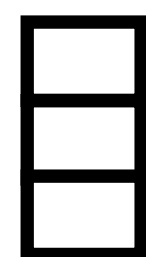
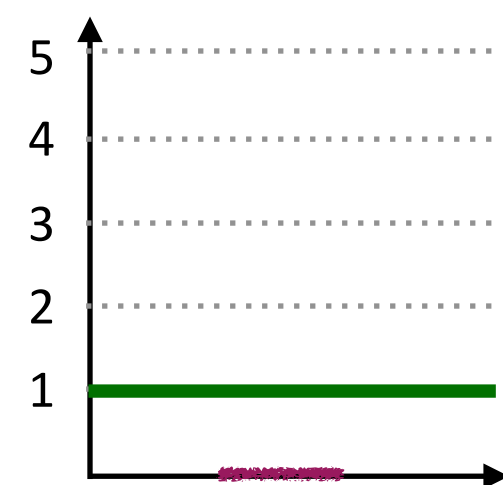
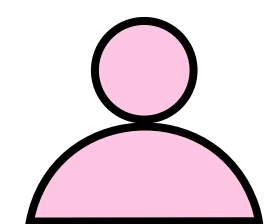
Donated Slices Shared Slices



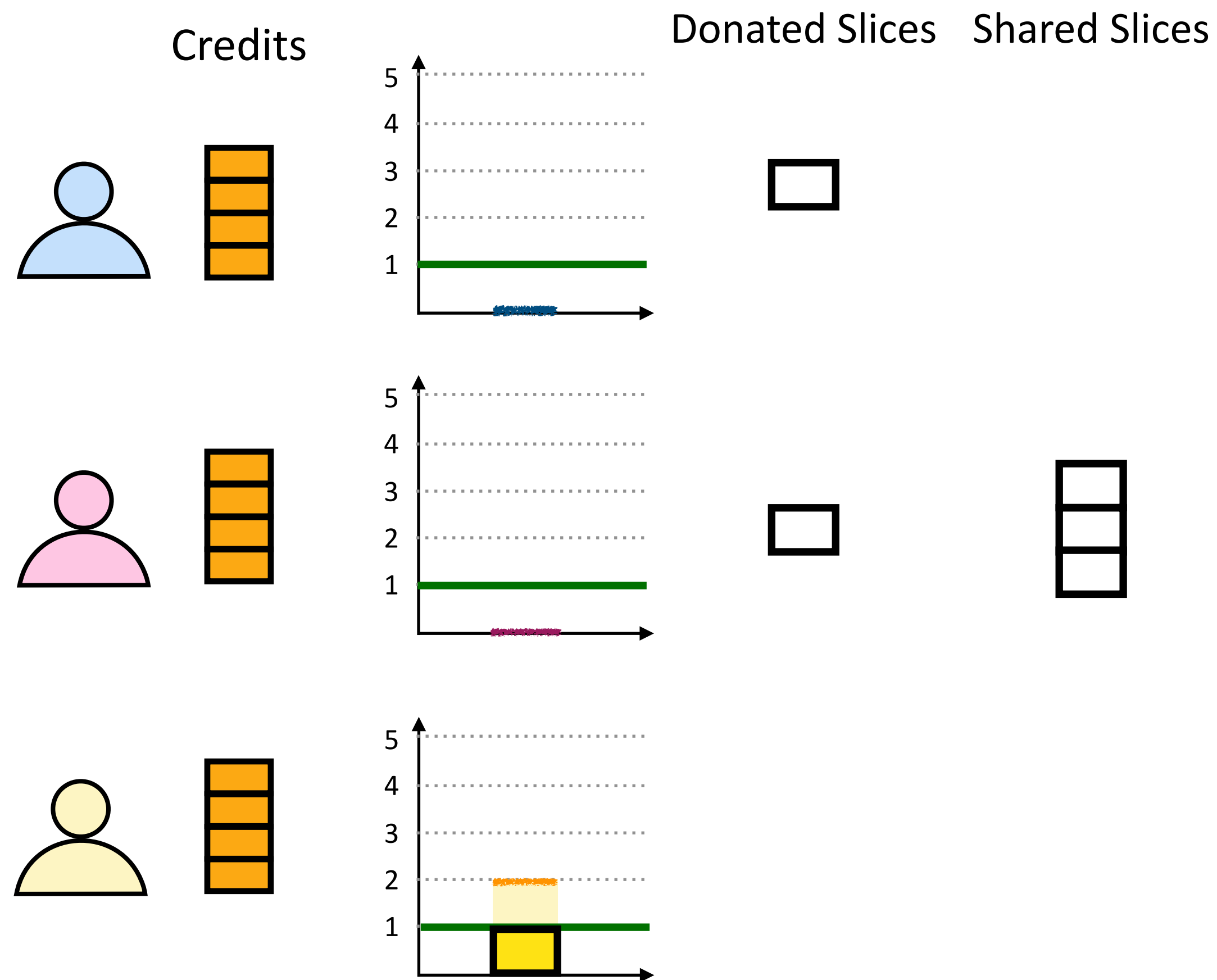
-1 credit for **borrowing** a slice

+1 credit if a **donated** slice is borrowed

(Every user is given initial credits at t=0)



Karma key idea #2: “credits” for resource allocation

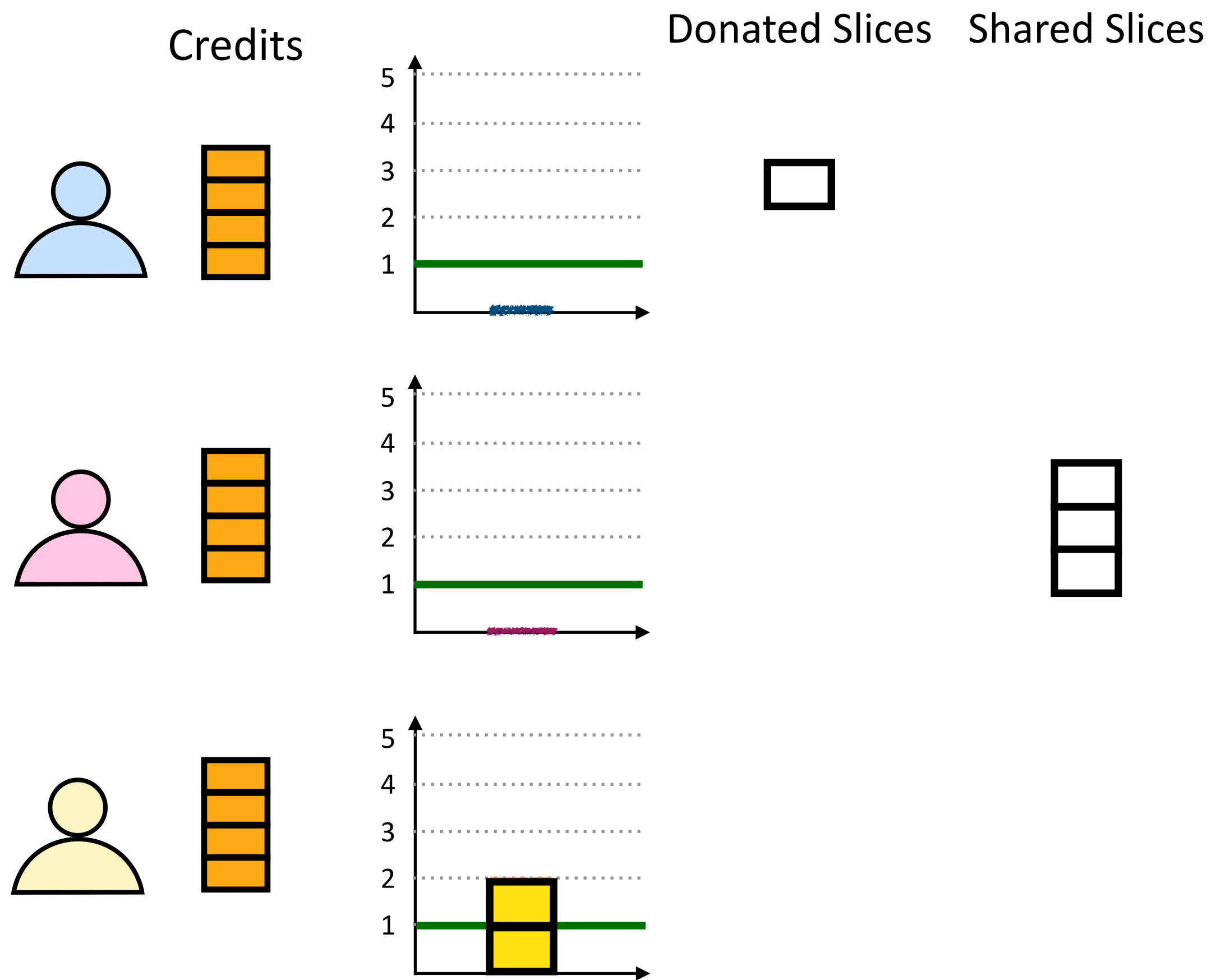


-1 credit for **borrowing** a slice

+1 credit if a **donated** slice is borrowed

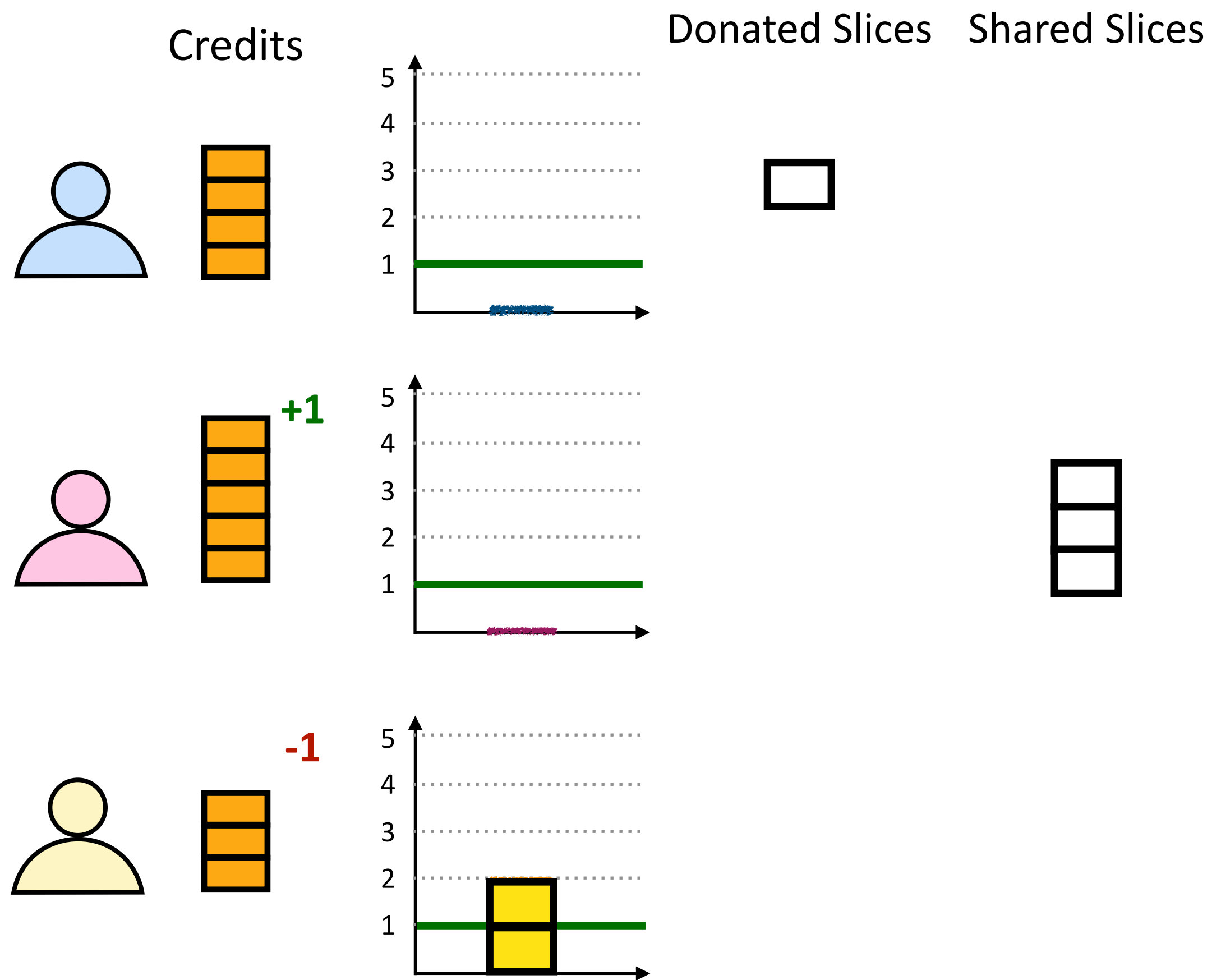
(Every user is given initial credits at $t=0$)

Karma key idea #2: "credits" for resource allocation



-1 credit for **borrowing** a slice
+1 credit if a **donated** slice is borrowed
(Every user is given initial credits at t=0)

Karma key idea #2: "credits" for resource allocation



-1 credit for **borrowing** a slice
+1 credit if a **donated** slice is borrowed
(Every user is given initial credits at t=0)


Karma allocation algorithm

Karma allocation algorithm

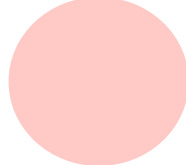

 Pick **borrower** with **maximum** credits

Karma allocation algorithm

 Pick **borrower** with **maximum** credits

 Pick **donor** with **minimum** credits

Karma allocation algorithm

-  Pick **borrower** with **maximum** credits
-  Pick **donor** with **minimum** credits
If no donors, then use a shared slice

Karma allocation algorithm

- Pick **borrower** with **maximum** credits
 - Pick **donor** with **minimum** credits
 - If no donors, then use a shared slice
- Allocate slice to borrower

Karma allocation algorithm

 Pick **borrower** with **maximum** credits

 Pick **donor** with **minimum** credits

If no donors, then use a shared slice

Allocate slice to borrower

-1 credit for borrower, **+1** credit for donor

Karma allocation algorithm

 Pick **borrower** with **maximum** credits

 Pick **donor** with **minimum** credits

If no donors, then use a shared slice

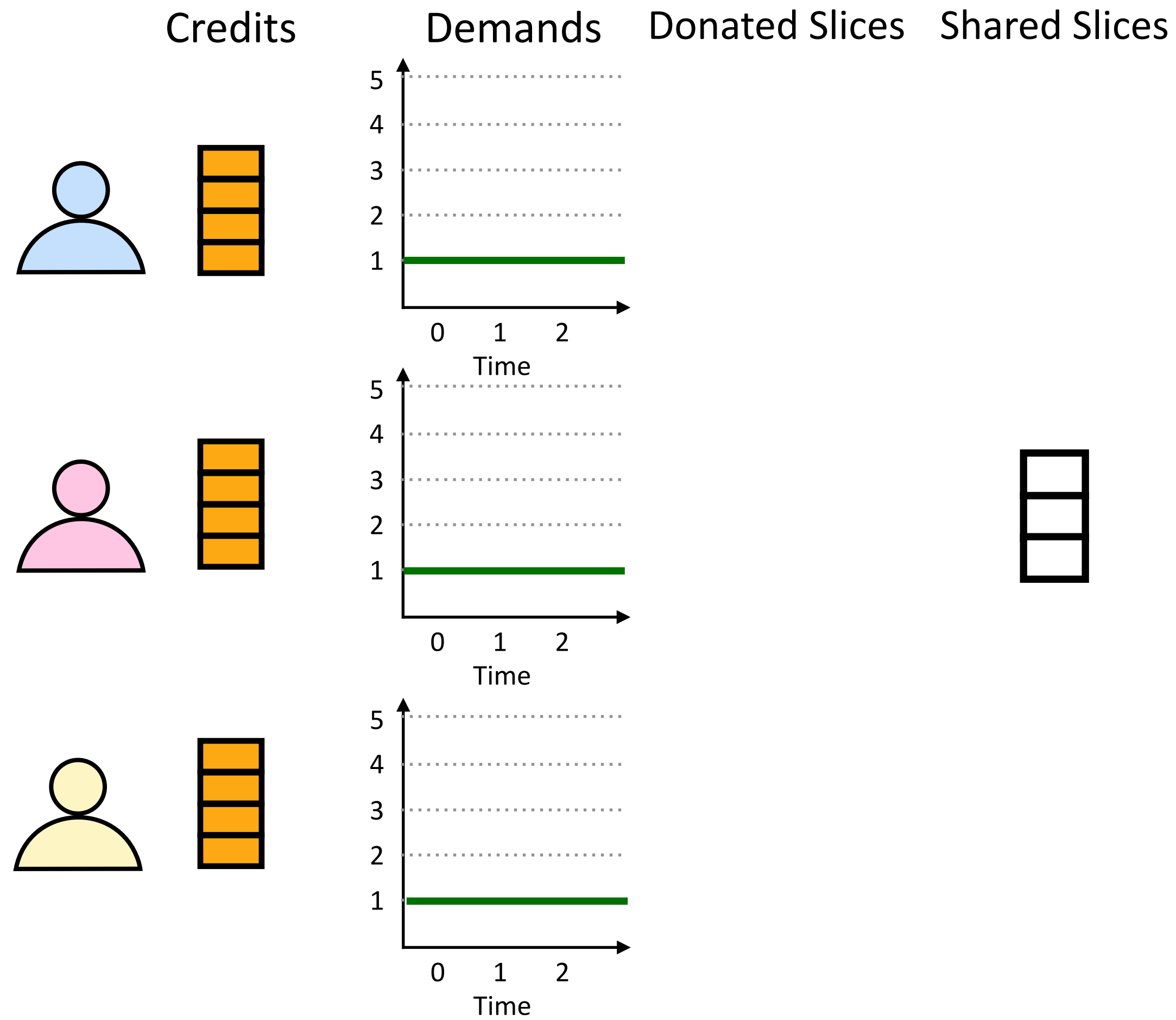
Allocate slice to borrower

-1 credit for borrower, **+1** credit for donor

(Repeat until demands satisfied or resources exhausted)

Karma allocation algorithm

Running Example



 Pick **borrower** with **maximum** credits

 Pick **donor** with **minimum** credits

If no donors, then use a shared slice

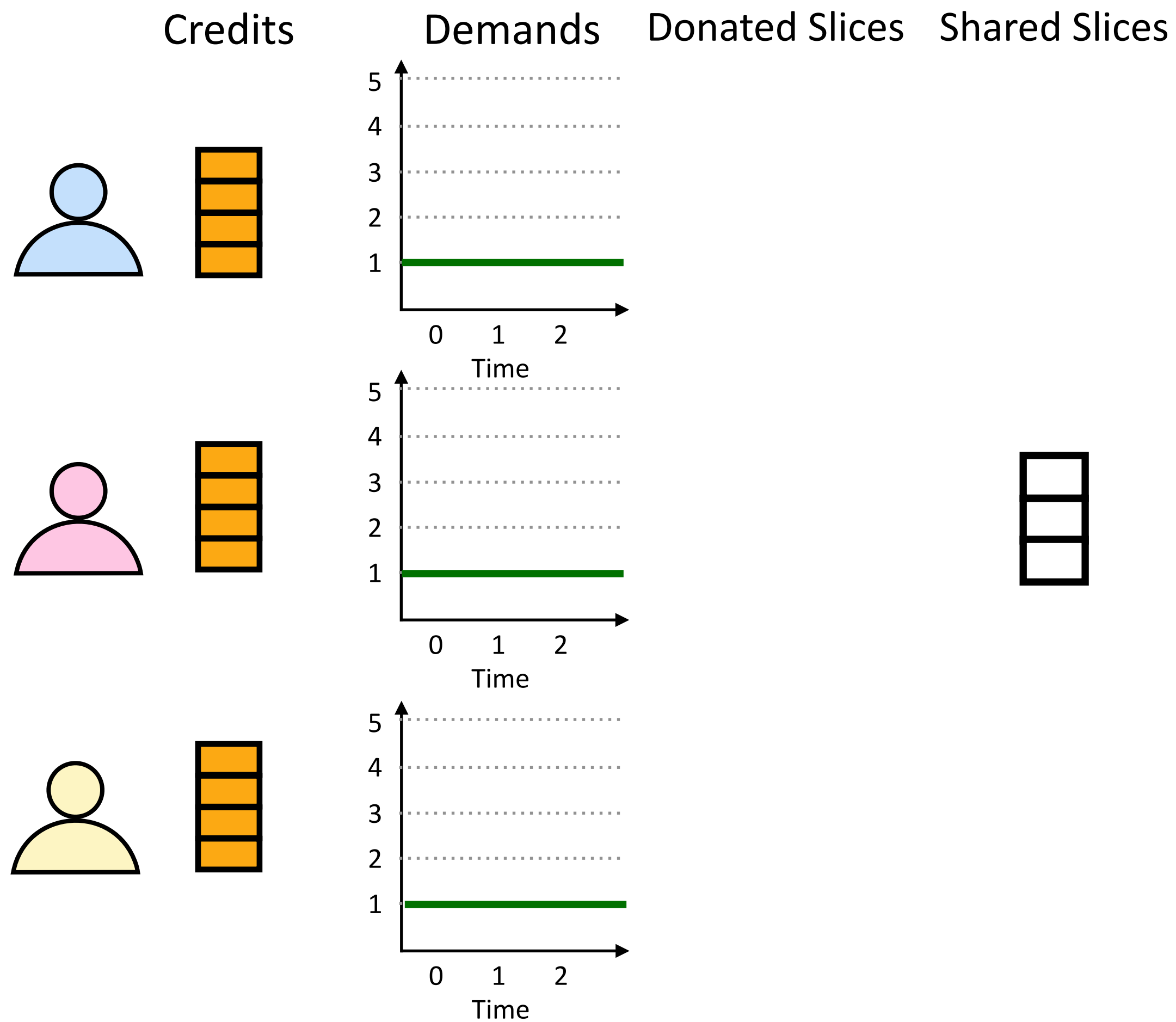
Allocate slice to borrower

-1 credit for borrower, **+1** credit for donor

(Repeat until demands satisfied or resources exhausted)

Karma allocation algorithm

Running Example



- Pick **borrower** with **maximum** credits
- Pick **donor** with **minimum** credits
- If no donors, then use a shared slice

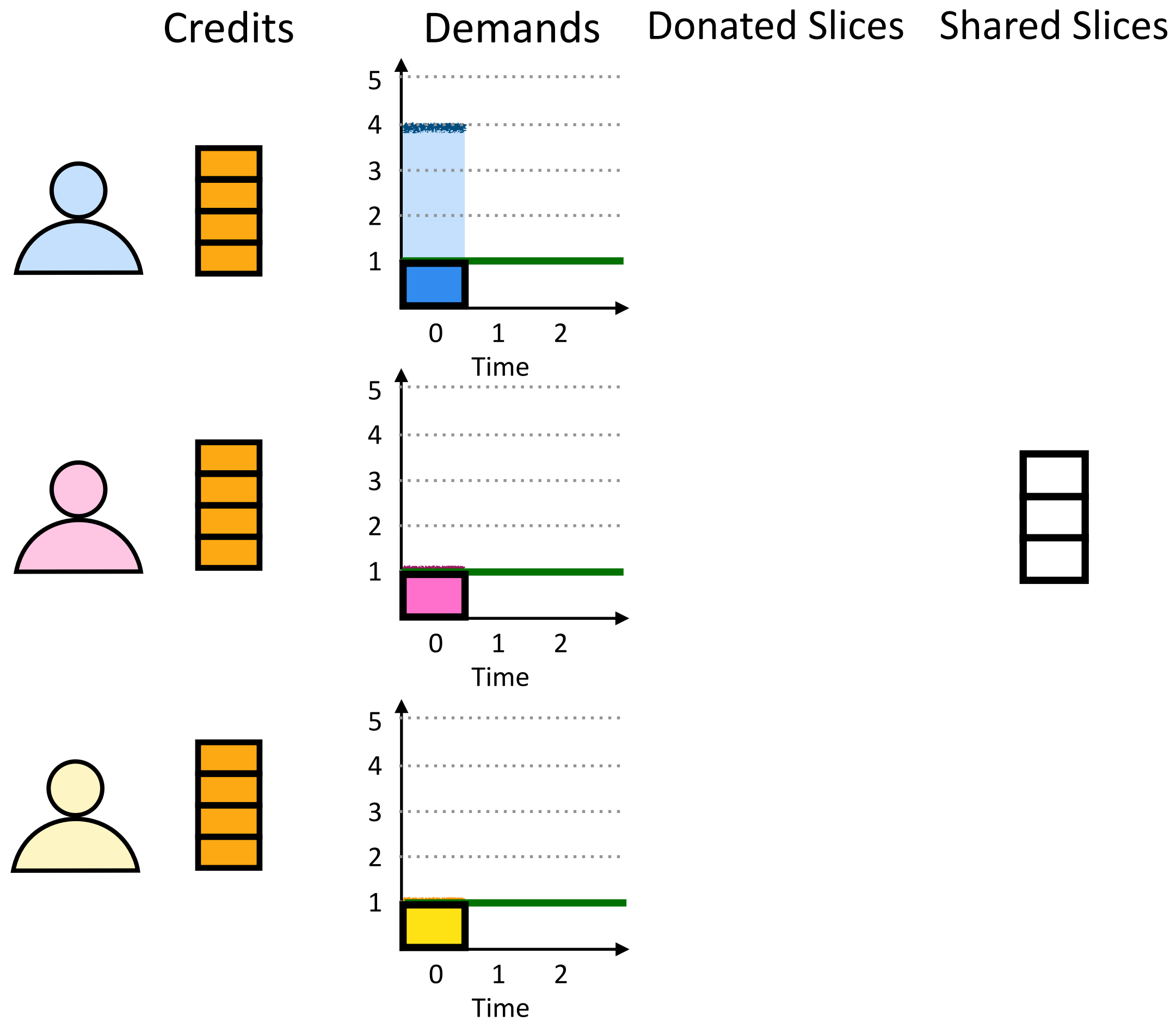
Allocate slice to borrower

-1 credit for borrower, +1 credit for donor

(Repeat until demands satisfied or resources exhausted)

Karma allocation algorithm

Running Example



 Pick **borrower** with **maximum** credits

 Pick **donor** with **minimum** credits

If no donors, then use a shared slice

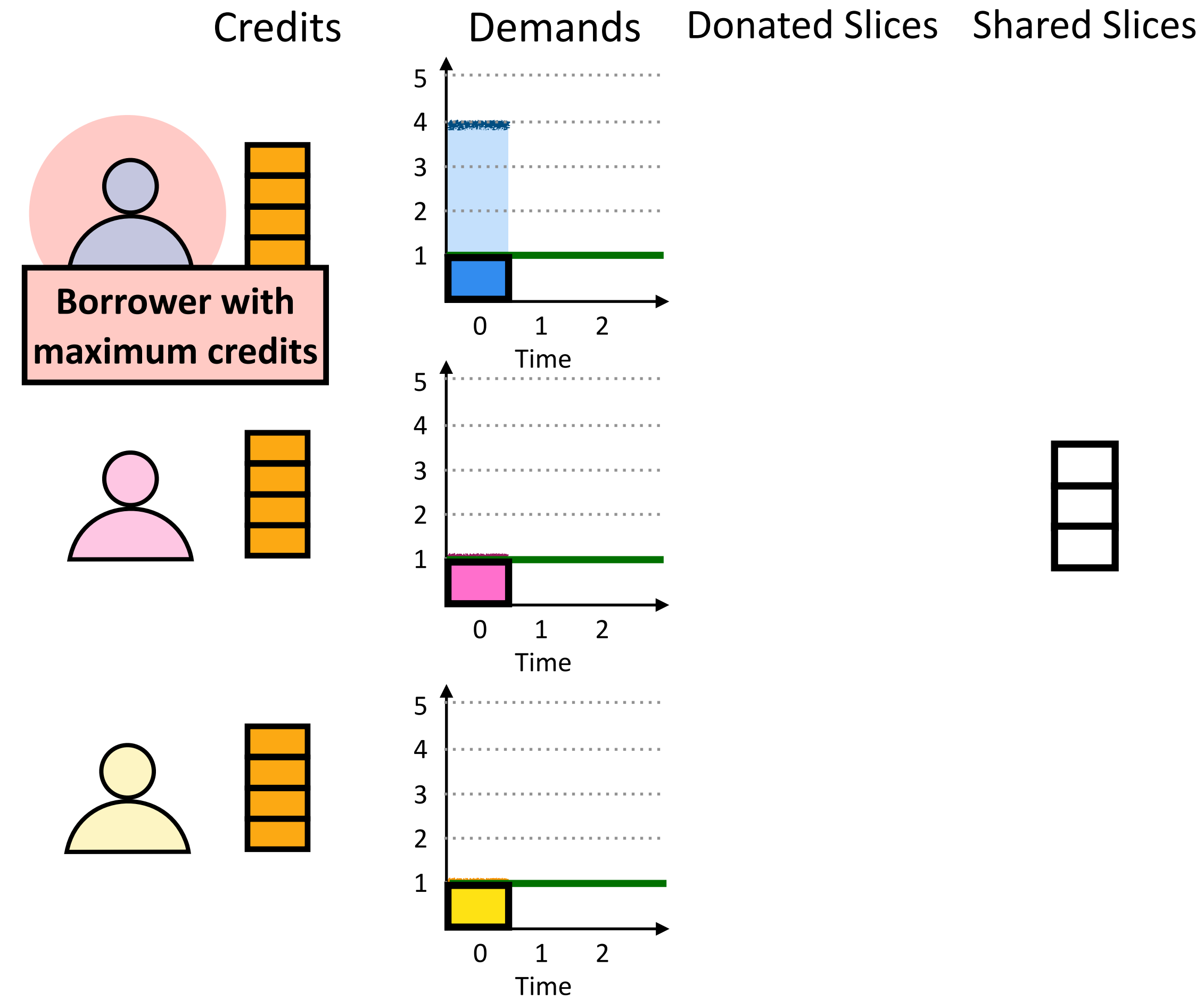
Allocate slice to borrower

-1 credit for borrower, +1 credit for donor

(Repeat until demands satisfied or resources exhausted)

Karma allocation algorithm

Running Example



● Pick **borrower** with **maximum** credits

● Pick **donor** with **minimum** credits

If no donors, then use a shared slice

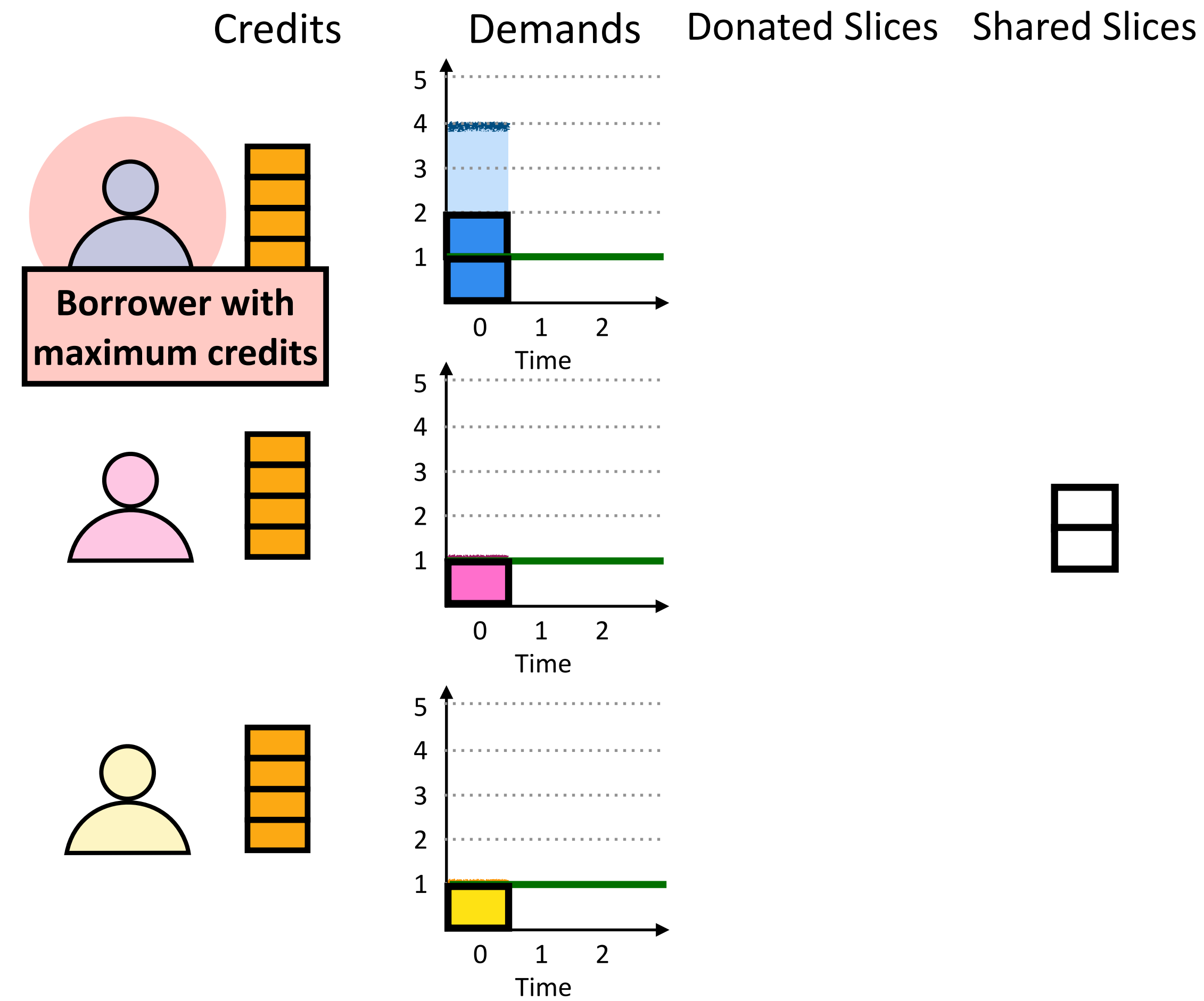
Allocate slice to borrower

-1 credit for borrower, +1 credit for donor

(Repeat until demands satisfied or resources exhausted)

Karma allocation algorithm

Running Example



● Pick **borrower** with **maximum** credits

● Pick **donor** with **minimum** credits

If no donors, then use a shared slice

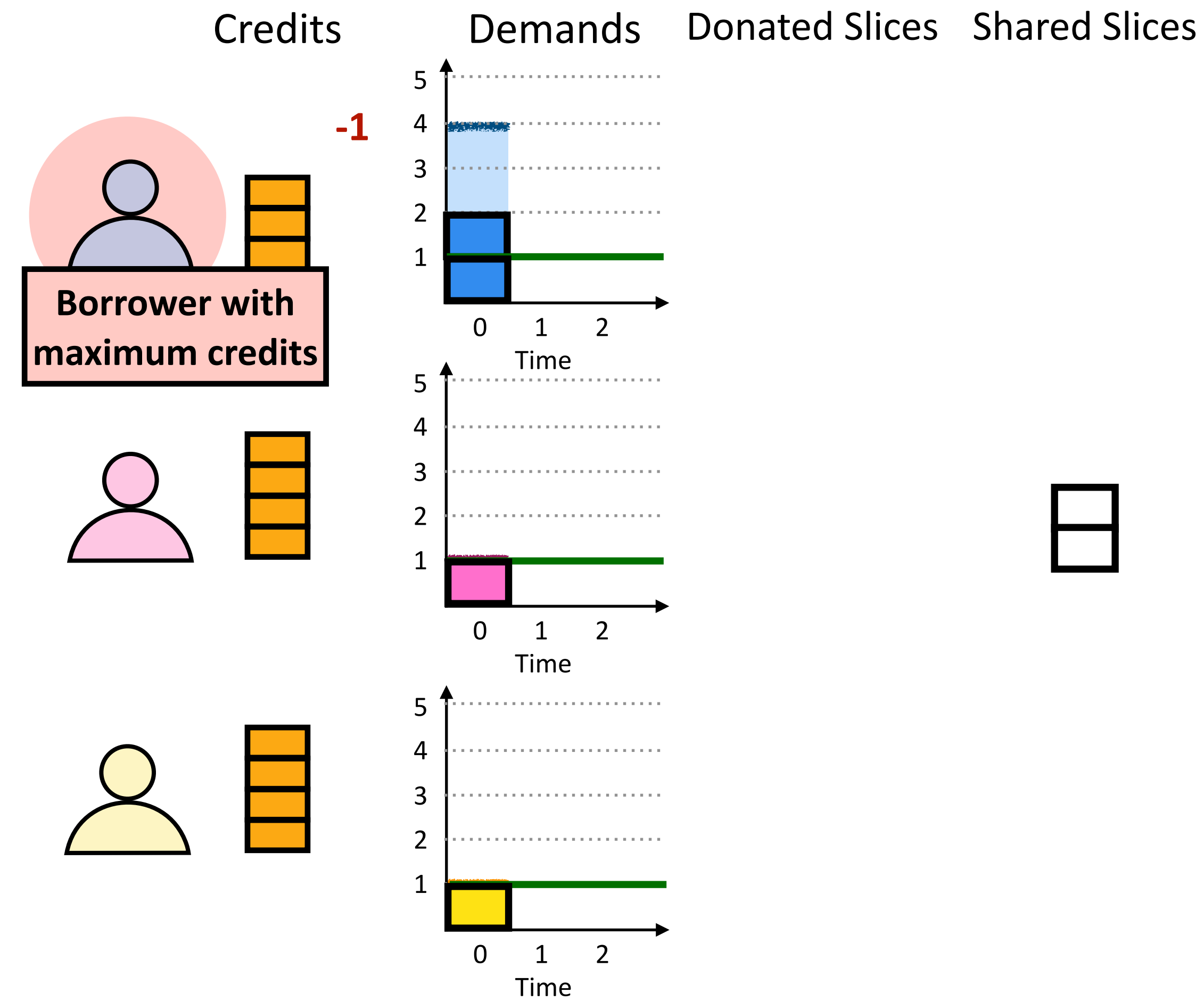
Allocate slice to borrower

-1 credit for borrower, +1 credit for donor

(Repeat until demands satisfied or resources exhausted)

Karma allocation algorithm

Running Example



● Pick **borrower** with **maximum** credits

● Pick **donor** with **minimum** credits

If no donors, then use a shared slice

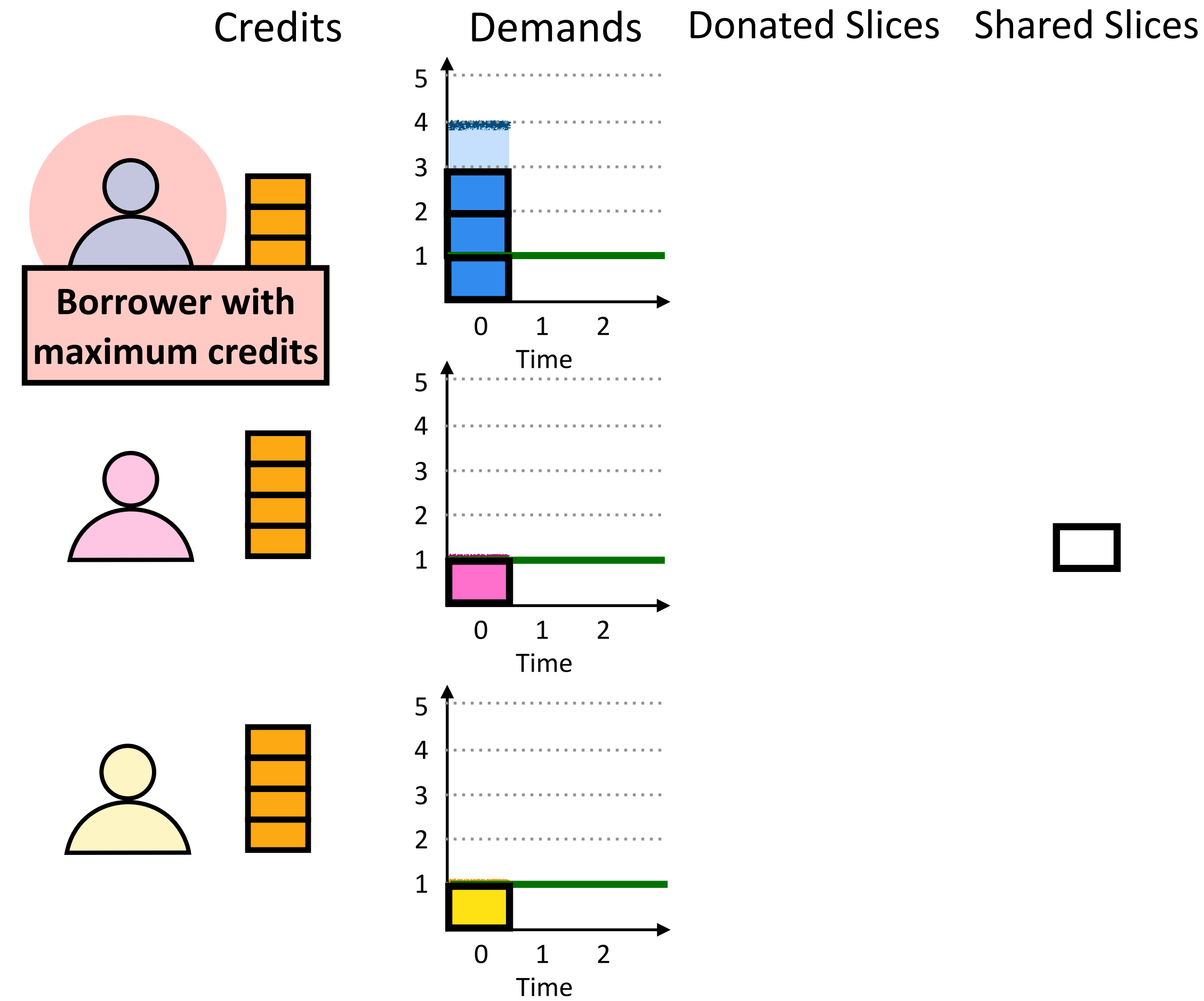
Allocate slice to borrower

-1 credit for borrower, +1 credit for donor

(Repeat until demands satisfied or resources exhausted)

Karma allocation algorithm

Running Example



● Pick **borrower** with **maximum** credits

● Pick **donor** with **minimum** credits

If no donors, then use a shared slice

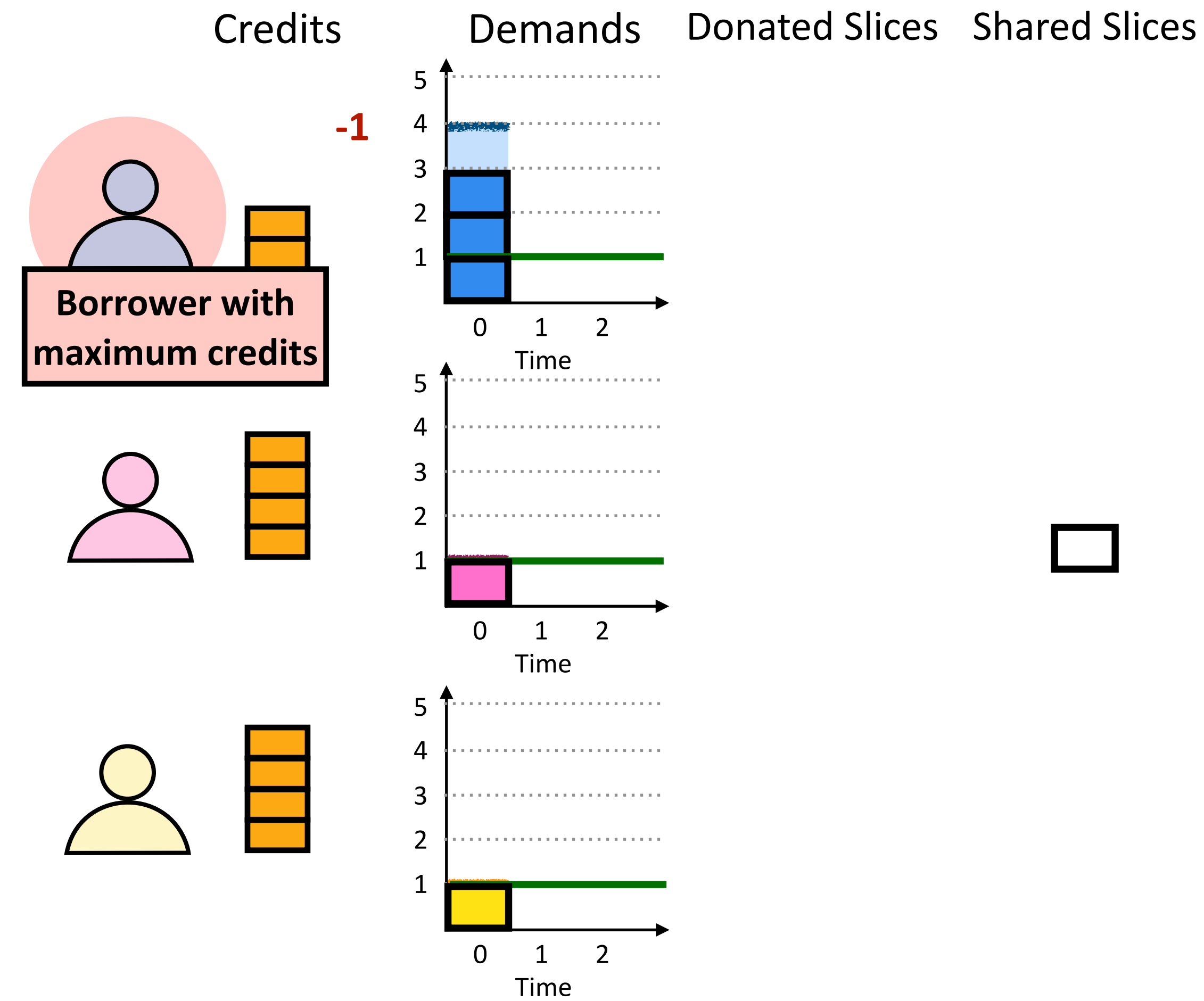
Allocate slice to borrower

-1 credit for borrower, +1 credit for donor

(Repeat until demands satisfied or resources exhausted)

Karma allocation algorithm

Running Example



● Pick **borrower** with **maximum** credits

● Pick **donor** with **minimum** credits

If no donors, then use a shared slice

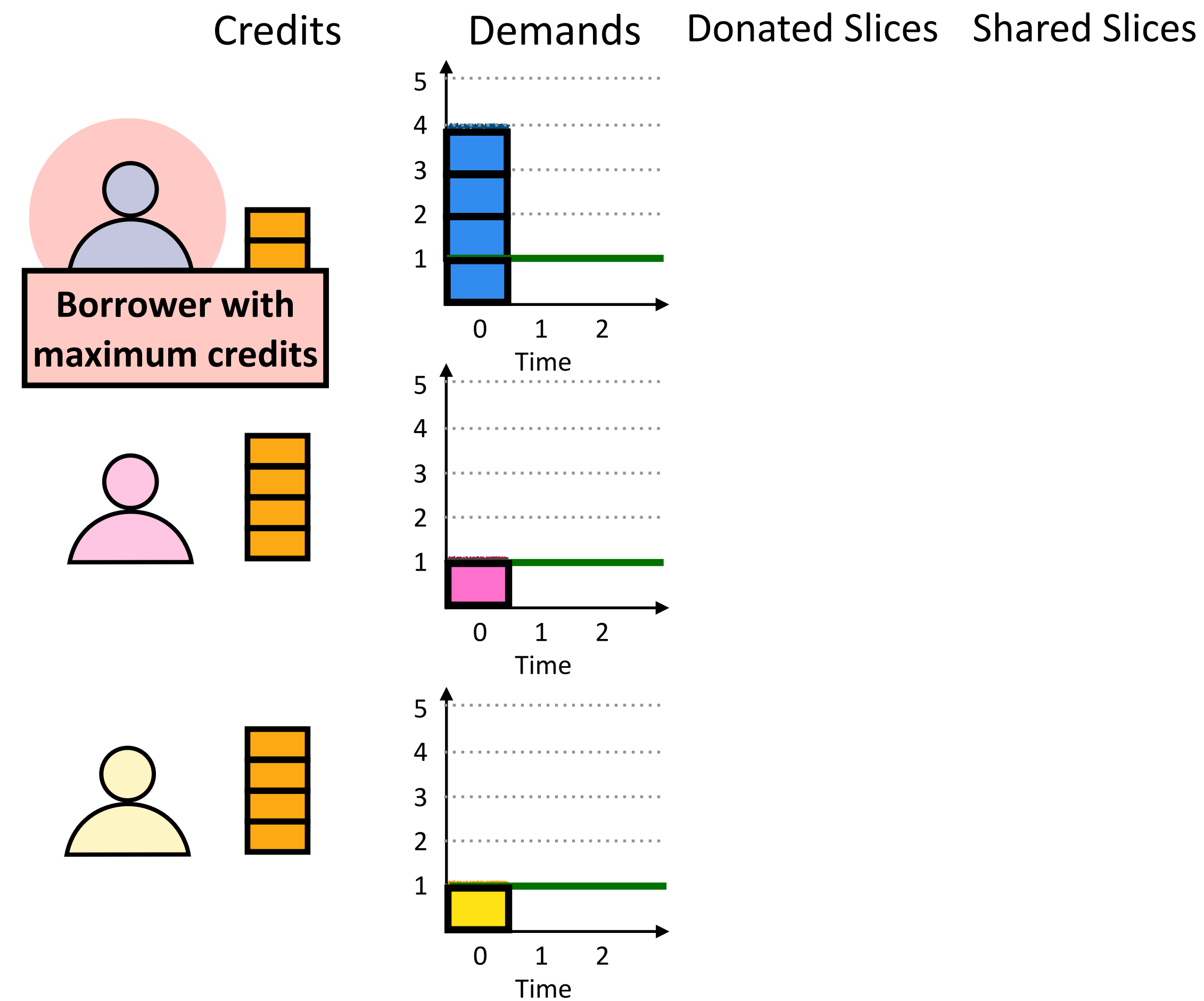
Allocate slice to borrower

-1 credit for borrower, +1 credit for donor

(Repeat until demands satisfied or resources exhausted)

Karma allocation algorithm

Running Example



- Pick **borrower** with **maximum** credits
- Pick **donor** with **minimum** credits
- If no donors, then use a shared slice

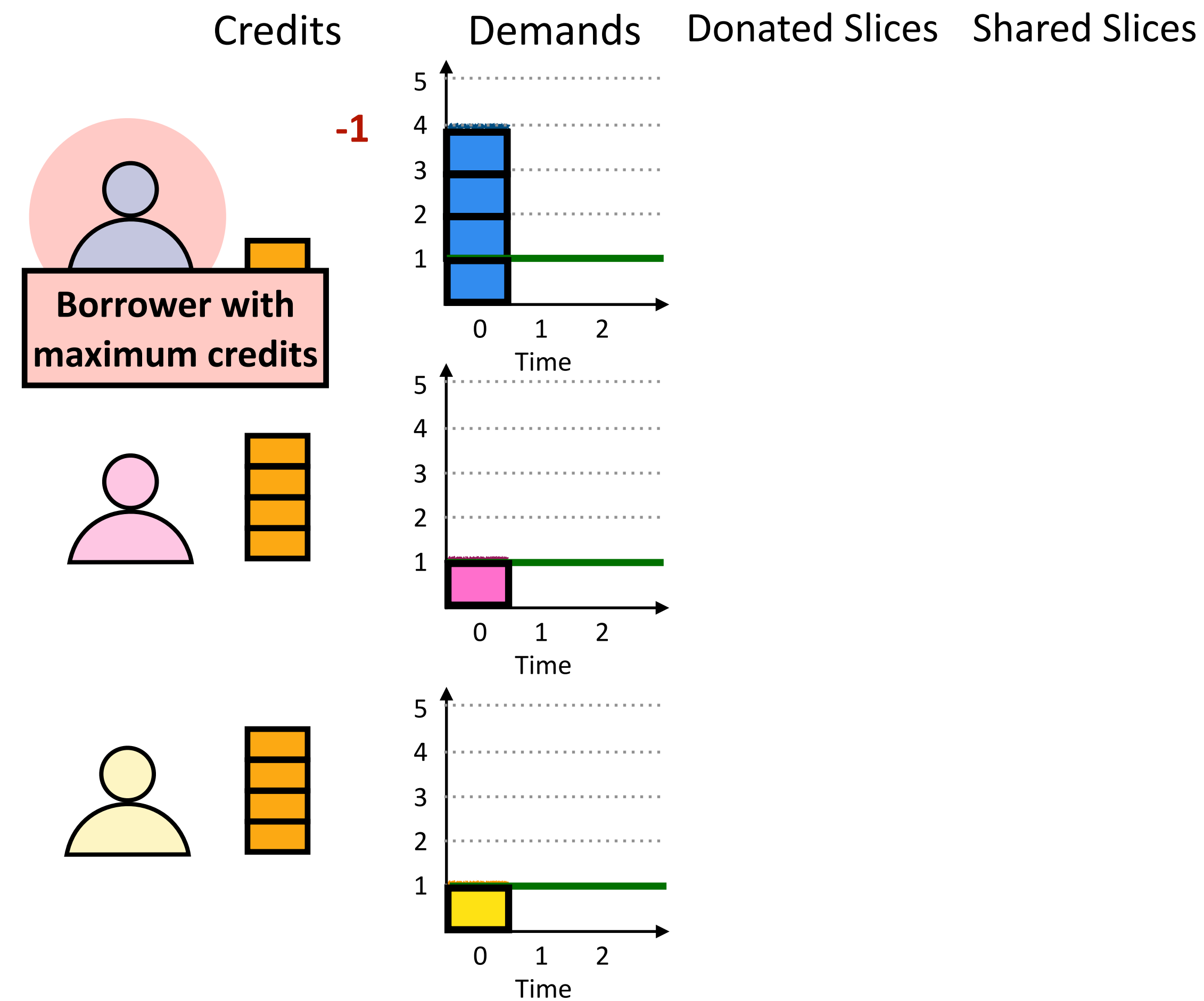
Allocate slice to borrower

-1 credit for borrower, +1 credit for donor

(Repeat until demands satisfied or resources exhausted)

Karma allocation algorithm

Running Example



● Pick **borrower** with **maximum** credits

● Pick **donor** with **minimum** credits

If no donors, then use a shared slice

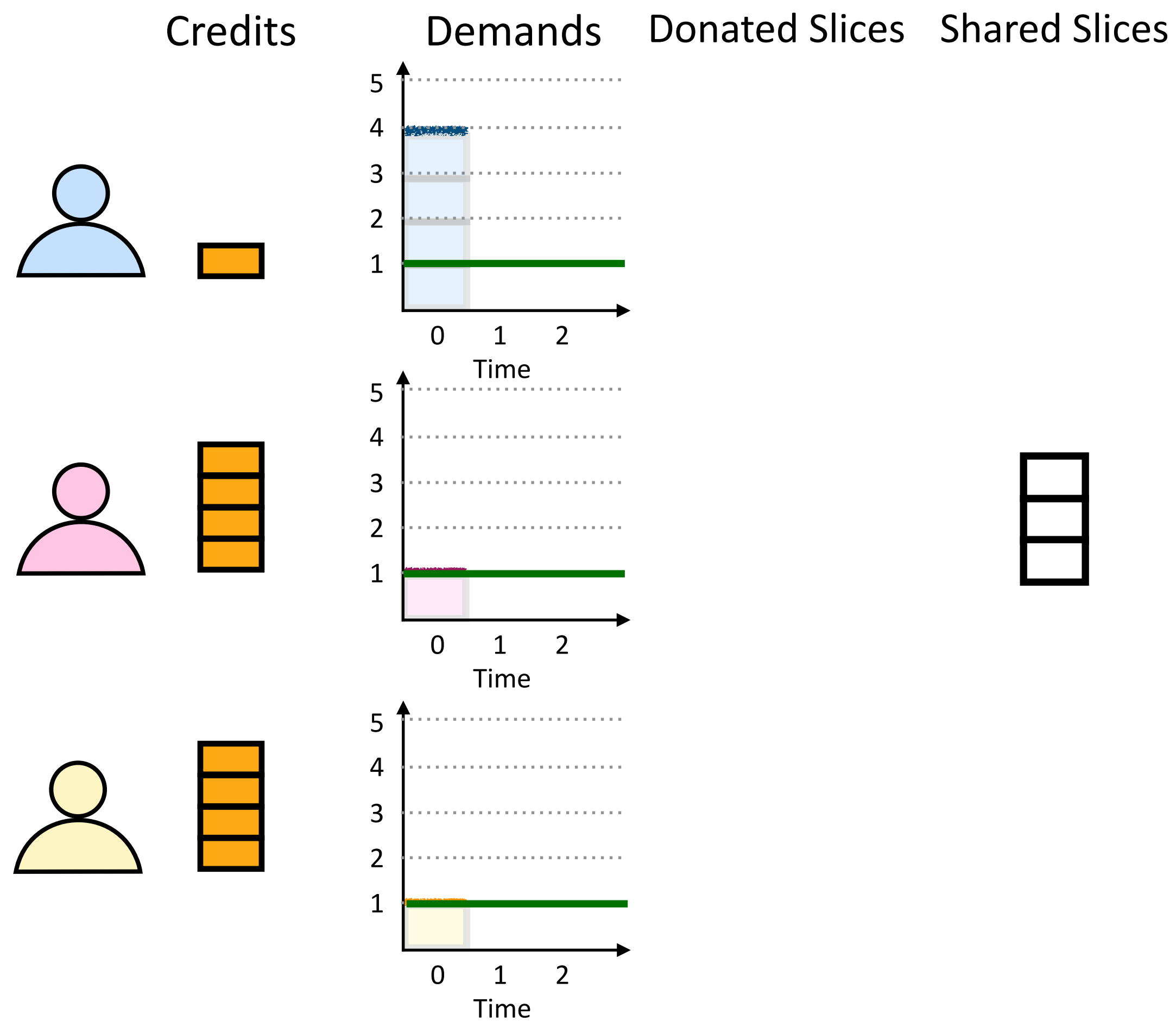
Allocate slice to borrower

-1 credit for borrower, +1 credit for donor

(Repeat until demands satisfied or resources exhausted)

Karma allocation algorithm

Running Example



- Pick **borrower** with **maximum** credits
- Pick **donor** with **minimum** credits
- If no donors, then use a shared slice

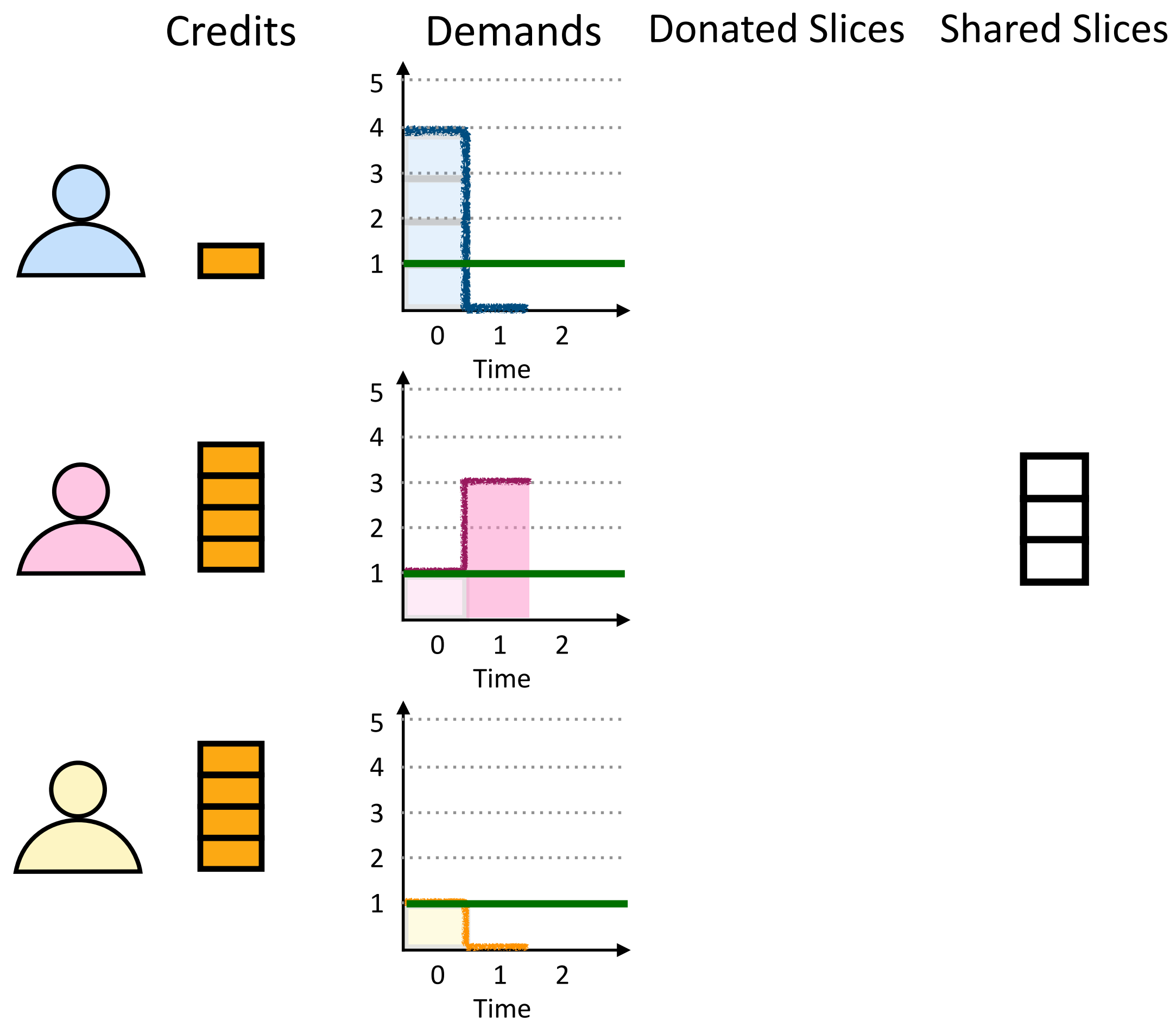
Allocate slice to borrower

-1 credit for borrower, +1 credit for donor

(Repeat until demands satisfied or resources exhausted)

Karma allocation algorithm

Running Example



- Pick **borrower** with **maximum** credits
- Pick **donor** with **minimum** credits
- If no donors, then use a shared slice

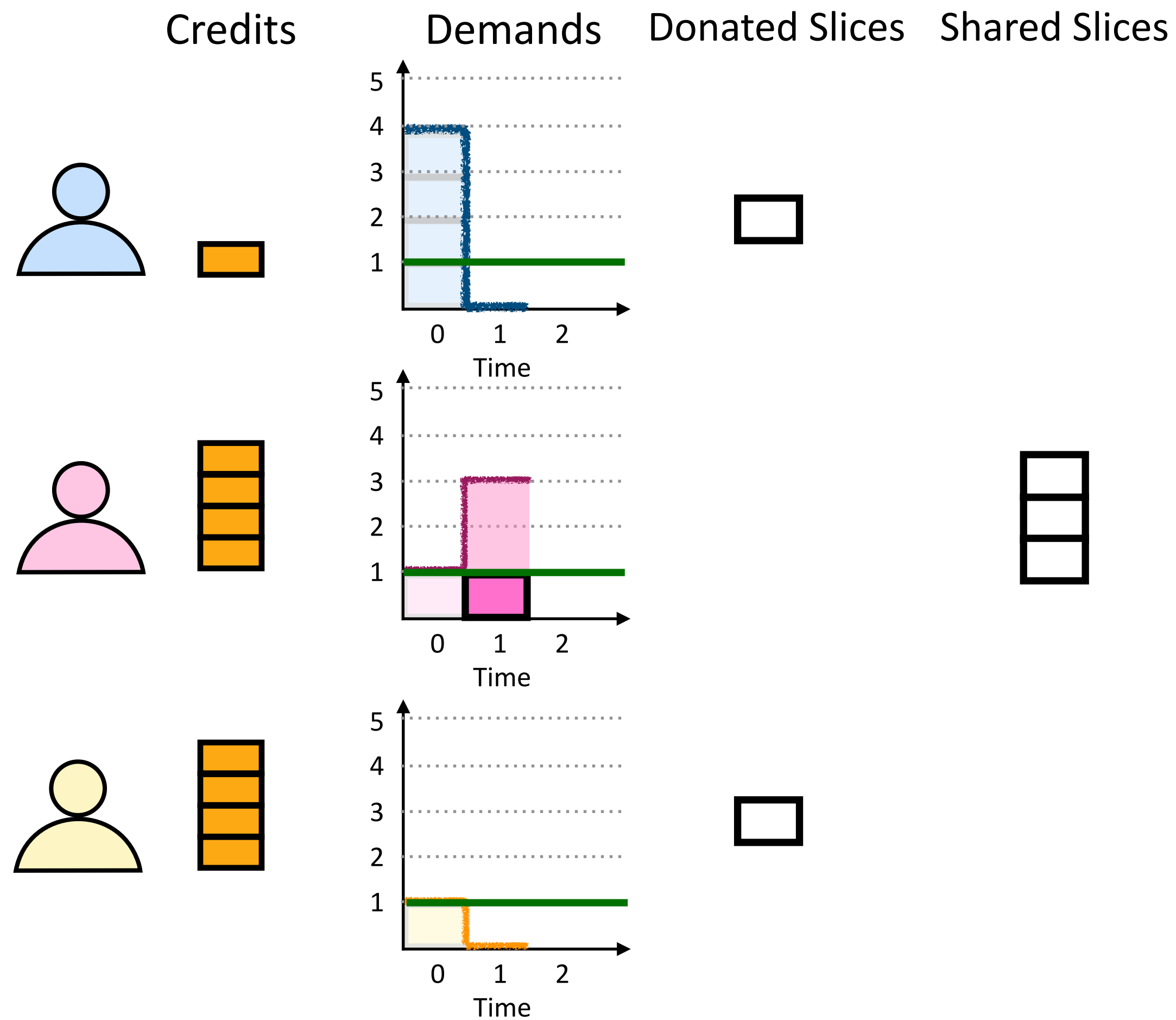
Allocate slice to borrower

-1 credit for borrower, +1 credit for donor

(Repeat until demands satisfied or resources exhausted)

Karma allocation algorithm

Running Example



 Pick **borrower** with **maximum** credits

 Pick **donor** with **minimum** credits

If no donors, then use a shared slice

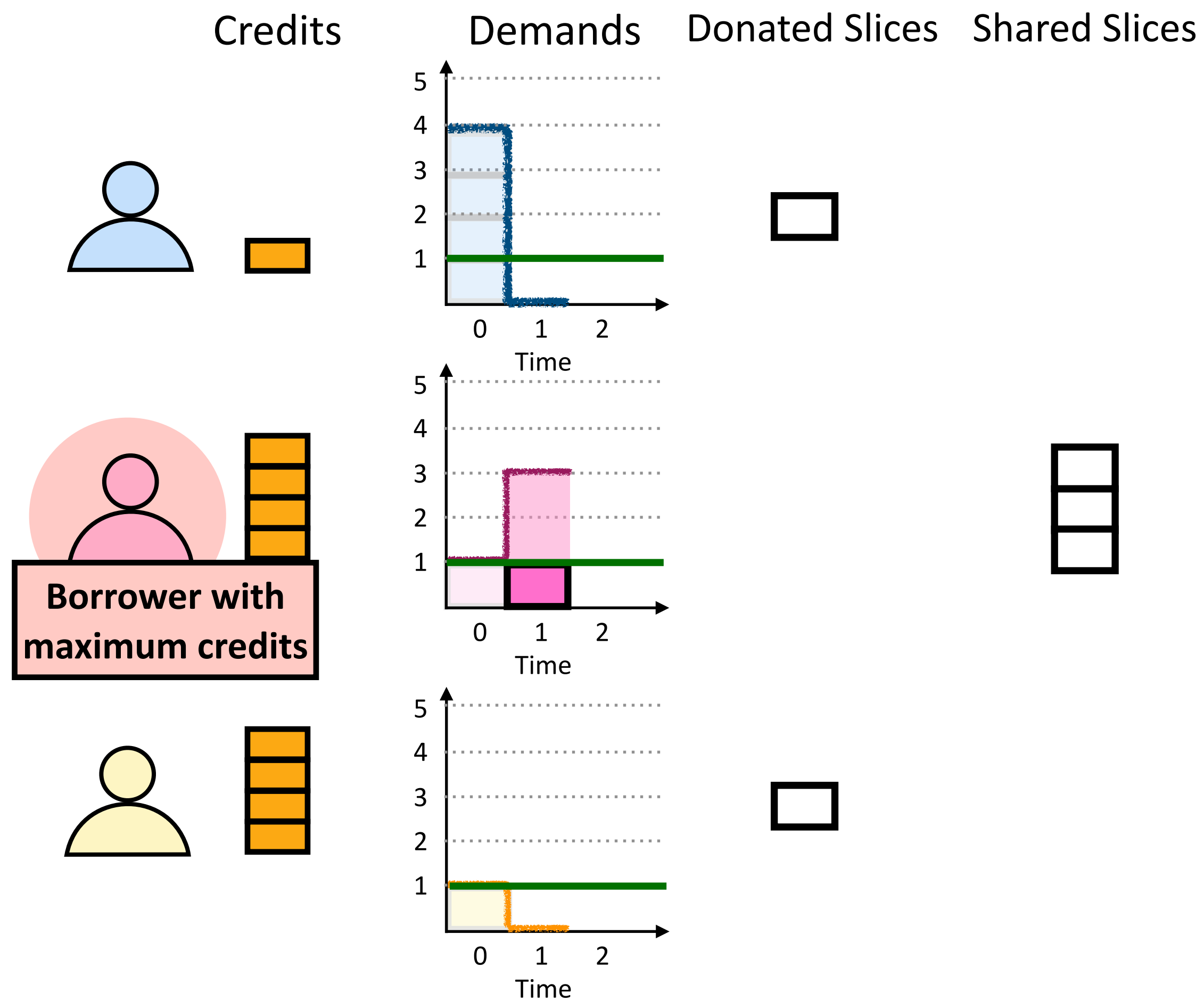
Allocate slice to borrower

-1 credit for borrower, **+1** credit for donor

(Repeat until demands satisfied or resources exhausted)

Karma allocation algorithm

Running Example



- Pick **borrower** with **maximum** credits
- Pick **donor** with **minimum** credits
- If no donors, then use a shared slice

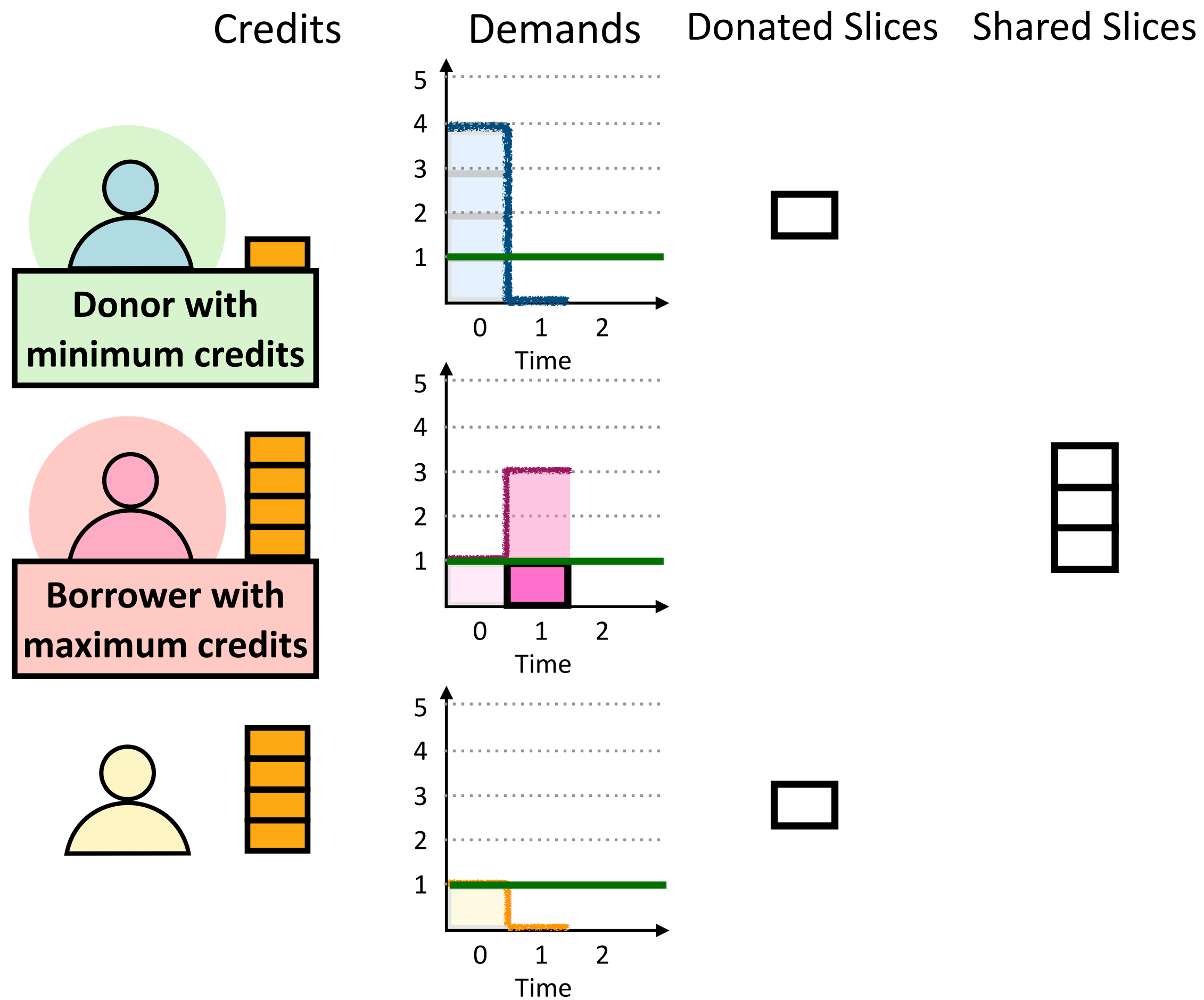
Allocate slice to borrower

-1 credit for borrower, +1 credit for donor

(Repeat until demands satisfied or resources exhausted)

Karma allocation algorithm

Running Example



● Pick **borrower** with **maximum** credits

● Pick **donor** with **minimum** credits

If no donors, then use a shared slice

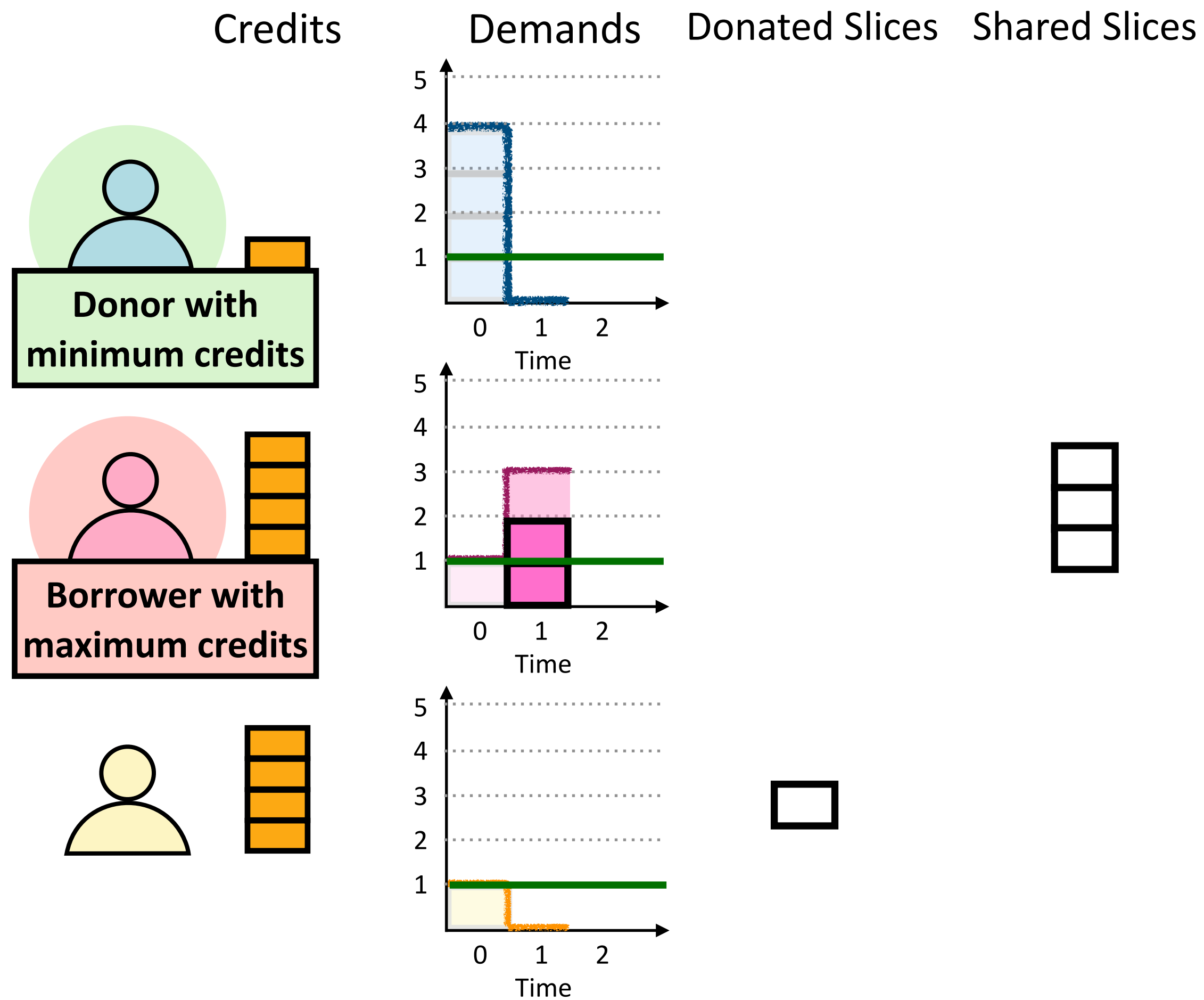
Allocate slice to borrower

-1 credit for borrower, +1 credit for donor

(Repeat until demands satisfied or resources exhausted)

Karma allocation algorithm

Running Example



● Pick **borrower** with **maximum** credits

● Pick **donor** with **minimum** credits

If no donors, then use a shared slice

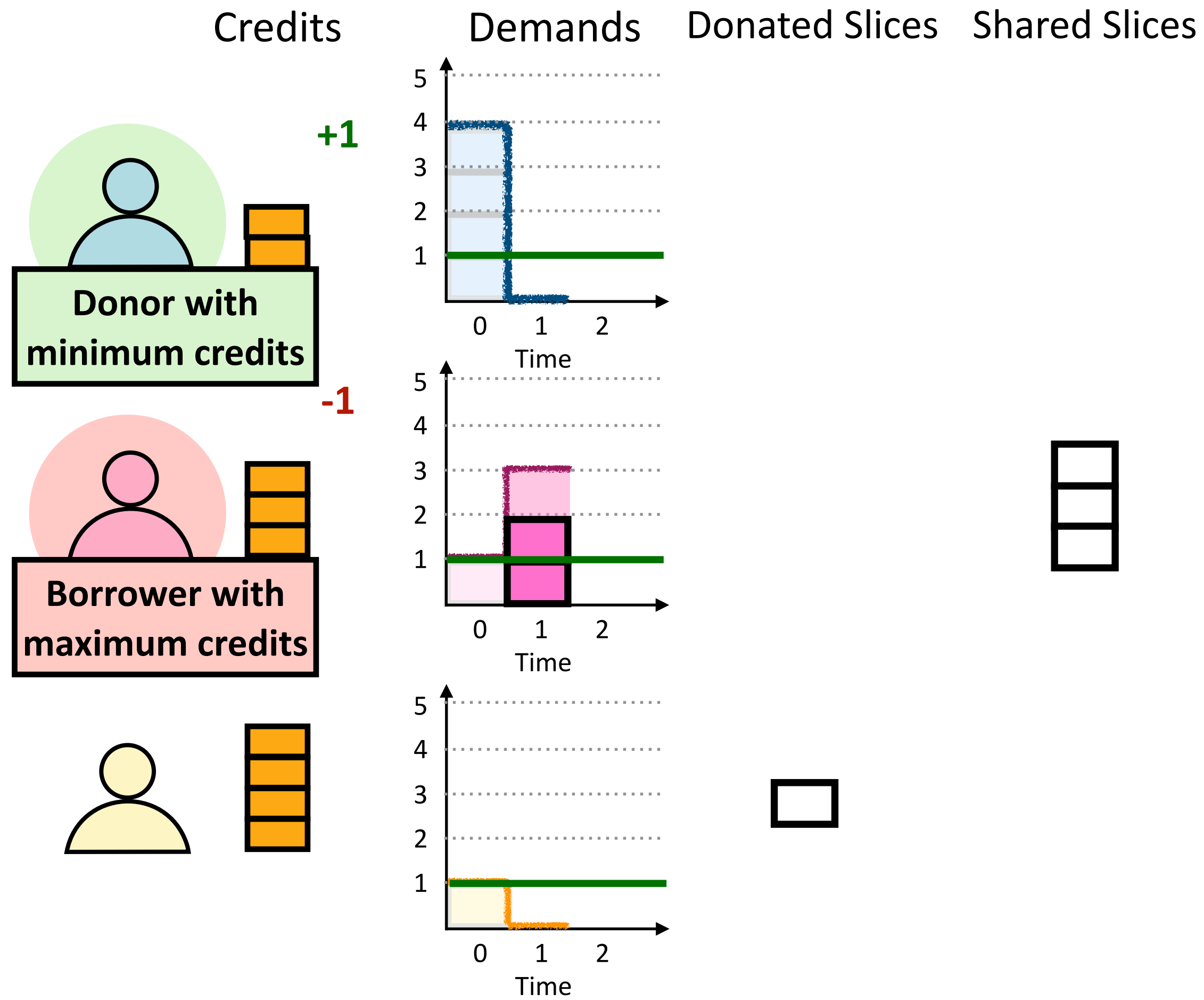
Allocate slice to borrower

-1 credit for borrower, +1 credit for donor

(Repeat until demands satisfied or resources exhausted)

Karma allocation algorithm

Running Example



● Pick **borrower** with **maximum** credits

● Pick **donor** with **minimum** credits

If no donors, then use a shared slice

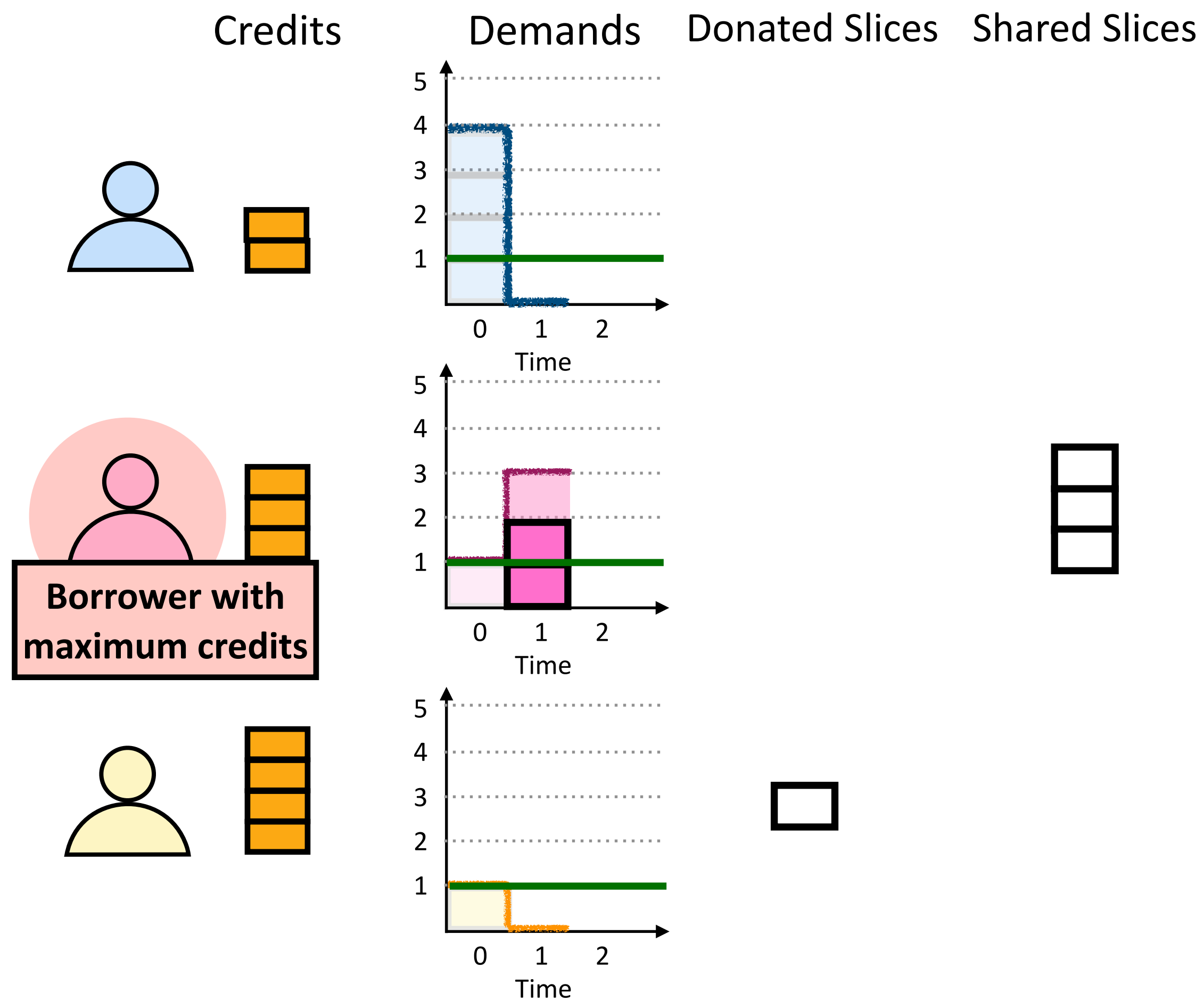
Allocate slice to borrower

-1 credit for borrower, +1 credit for donor

(Repeat until demands satisfied or resources exhausted)

Karma allocation algorithm

Running Example



- Pick **borrower** with **maximum** credits
- Pick **donor** with **minimum** credits
- If no donors, then use a shared slice

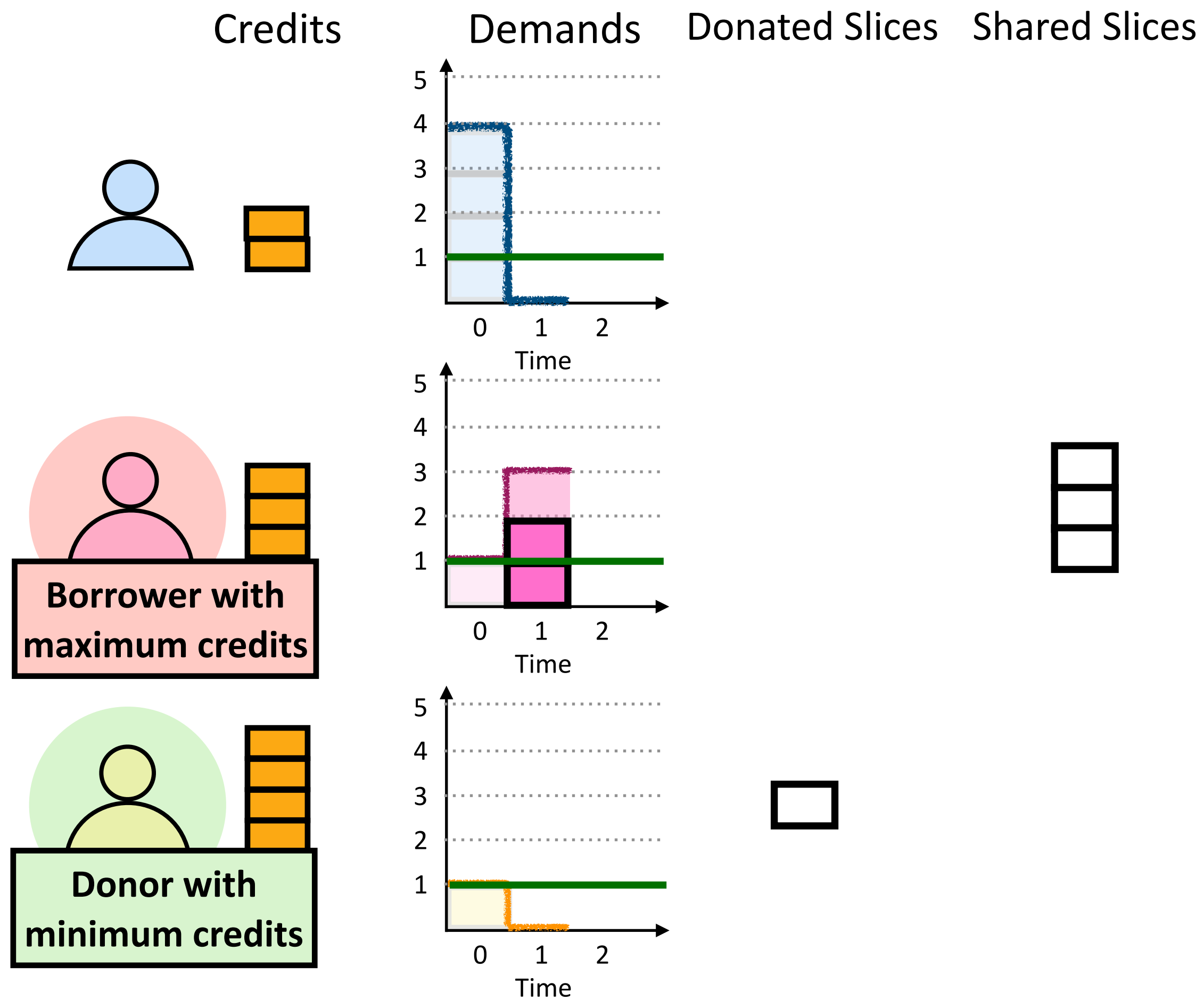
Allocate slice to borrower

-1 credit for borrower, +1 credit for donor

(Repeat until demands satisfied or resources exhausted)

Karma allocation algorithm

Running Example



● Pick **borrower** with **maximum** credits

● Pick **donor** with **minimum** credits

If no donors, then use a shared slice

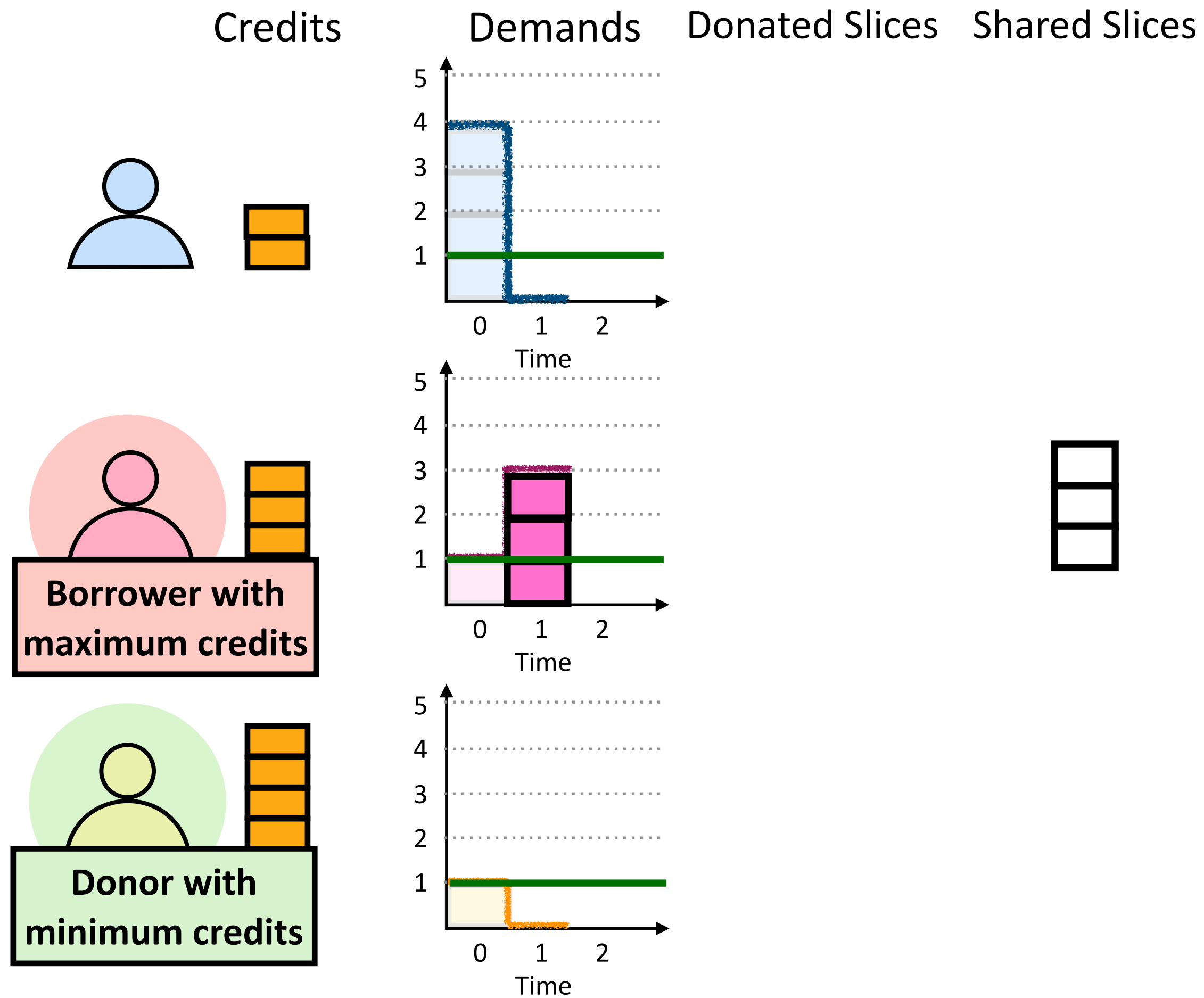
Allocate slice to borrower

-1 credit for borrower, +1 credit for donor

(Repeat until demands satisfied or resources exhausted)

Karma allocation algorithm

Running Example



● Pick **borrower** with **maximum** credits

● Pick **donor** with **minimum** credits

If no donors, then use a shared slice

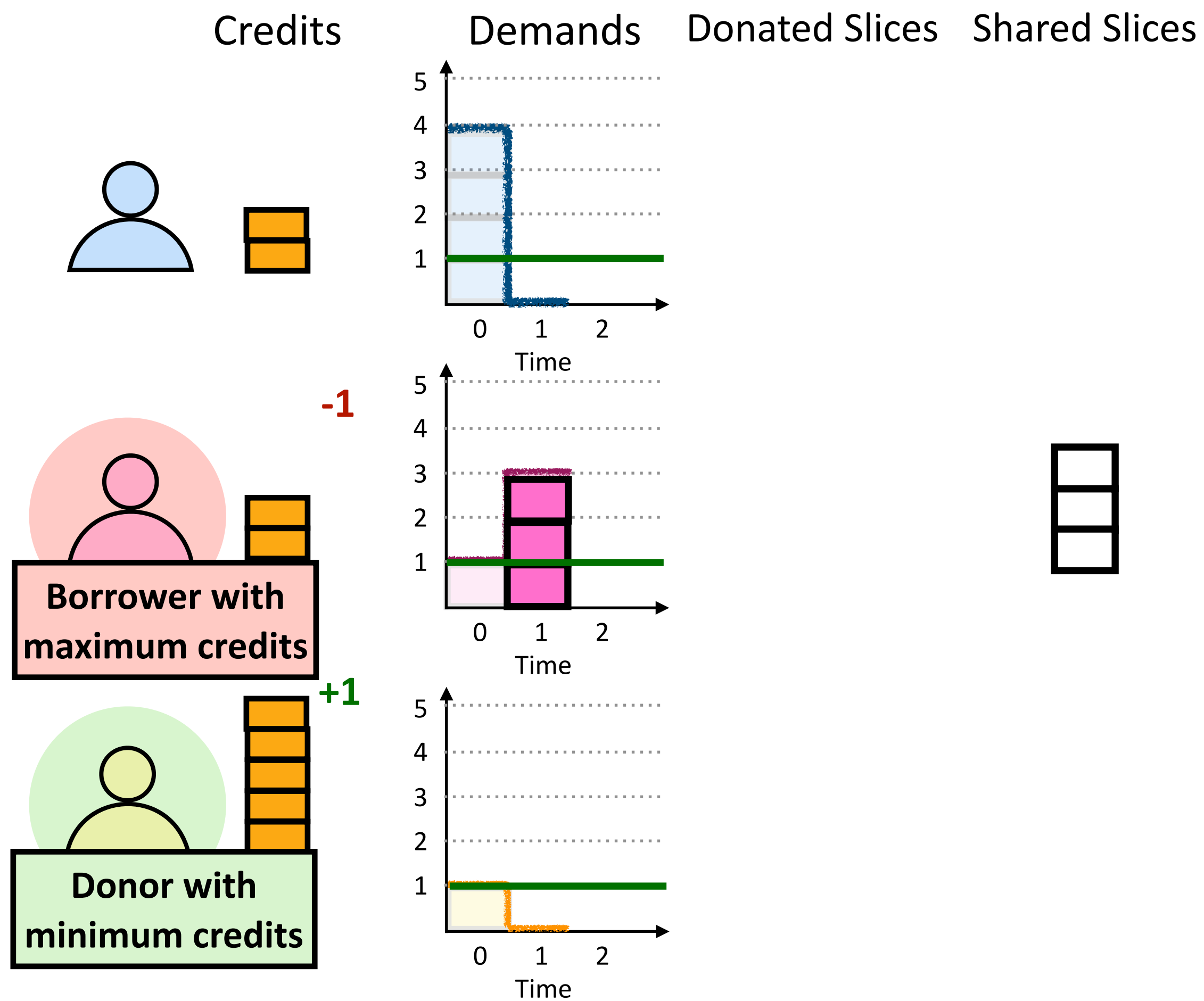
Allocate slice to borrower

-1 credit for borrower, +1 credit for donor

(Repeat until demands satisfied or resources exhausted)

Karma allocation algorithm

Running Example



- Pick **borrower** with **maximum** credits
- Pick **donor** with **minimum** credits
- If no donors, then use a shared slice

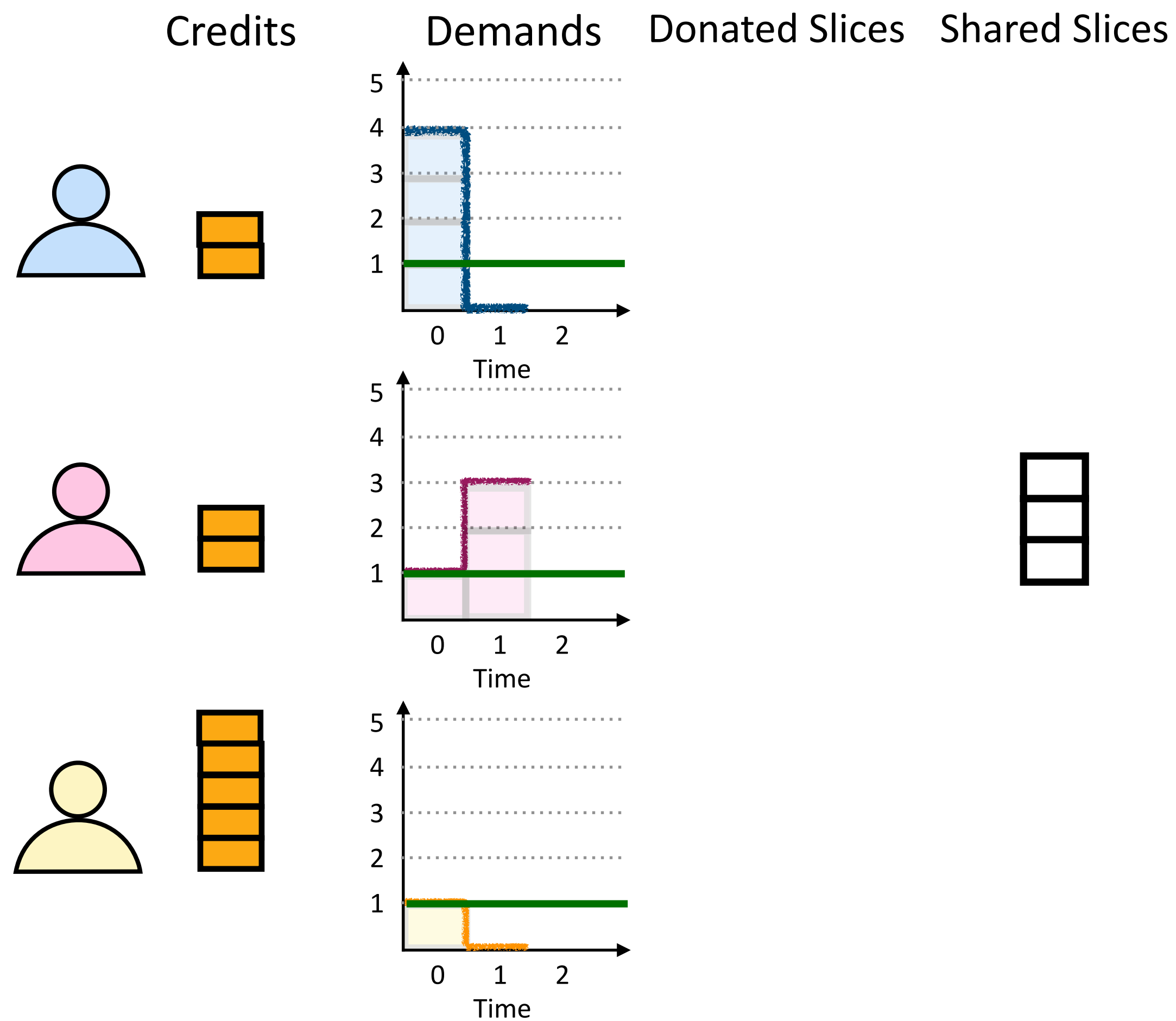
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Karma allocation algorithm

Running Example



 Pick **borrower** with **maximum** credits

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If no donors, then use a shared slice

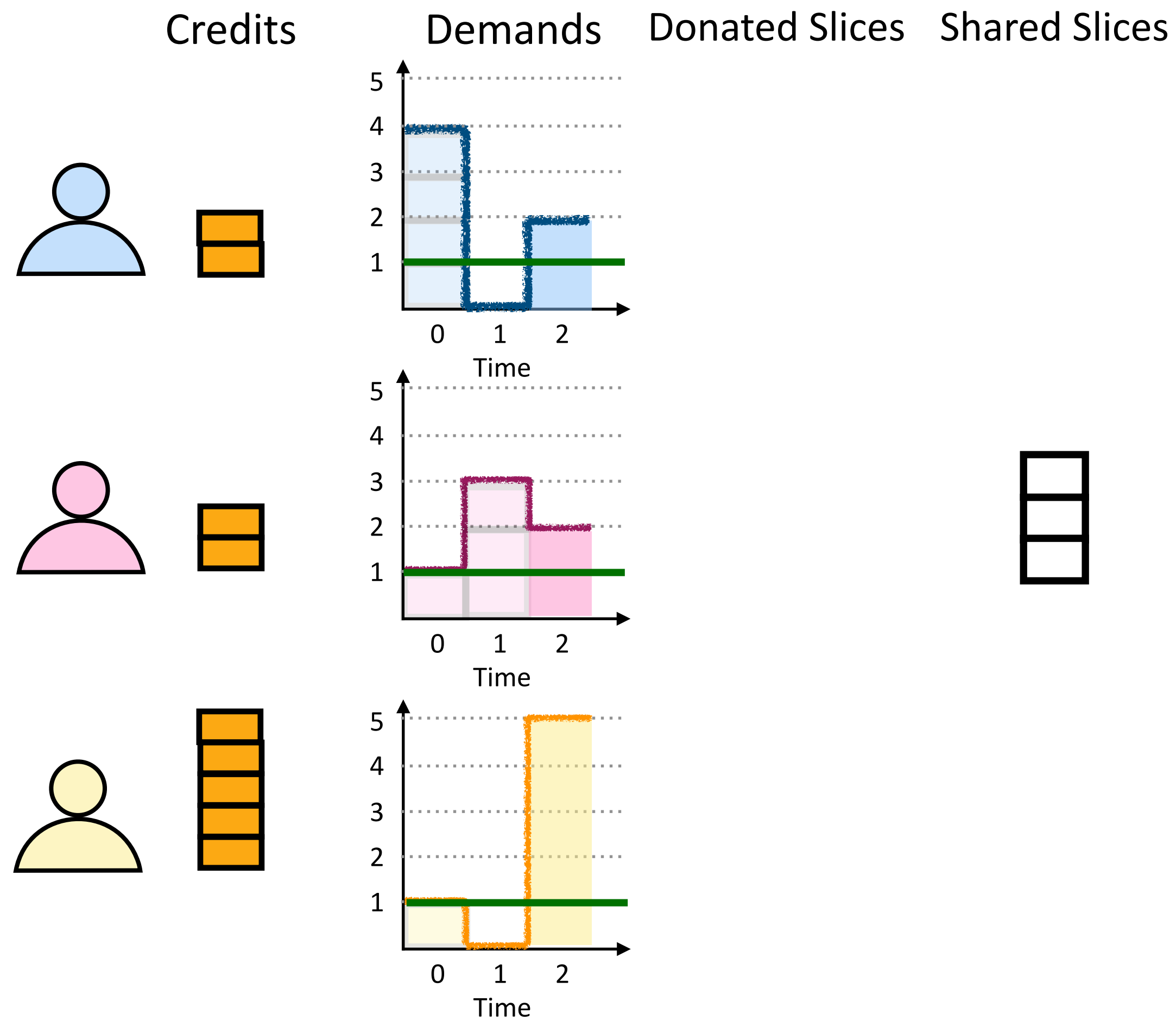
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Karma allocation algorithm

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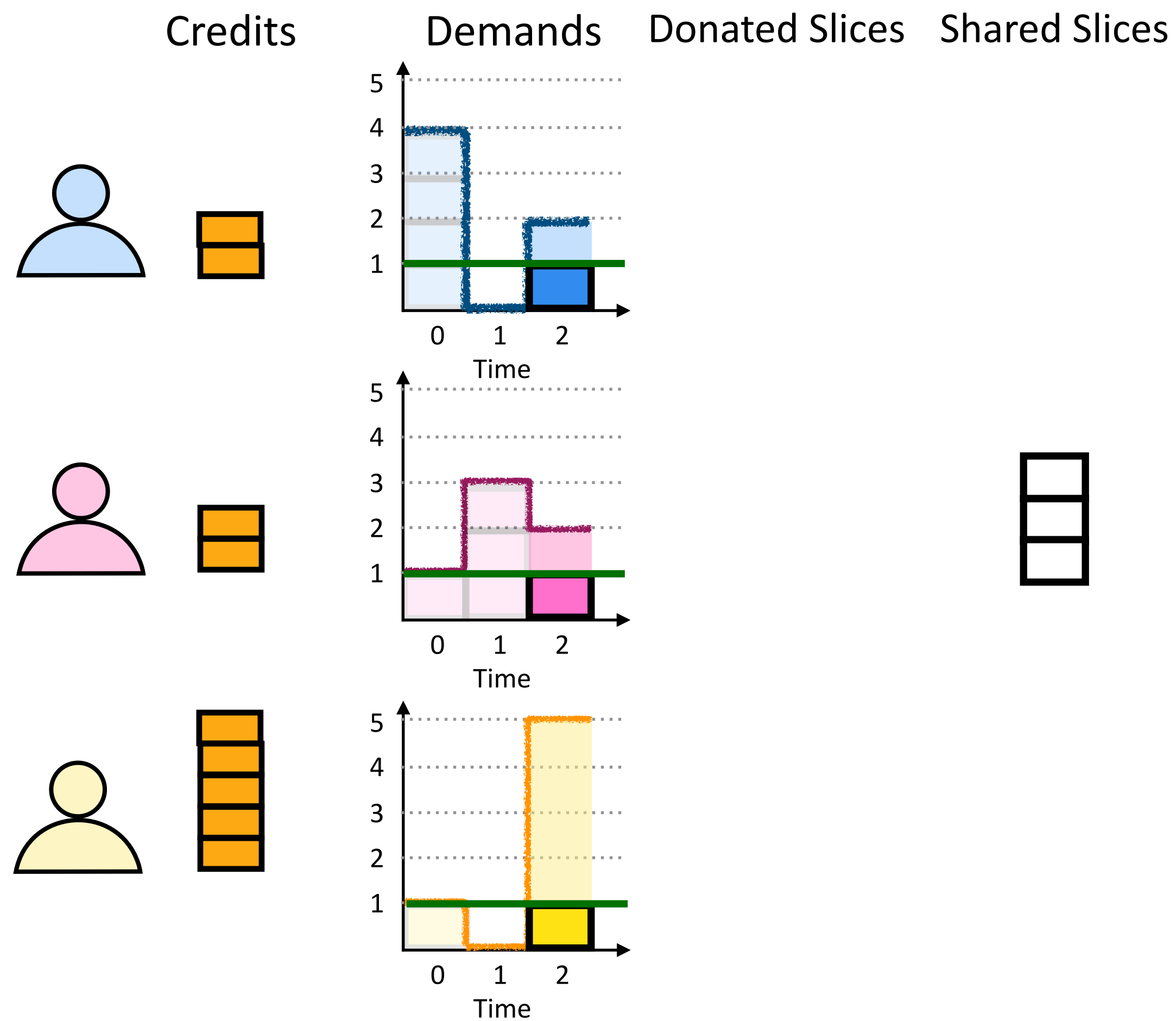
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Karma allocation algorithm

Running Example



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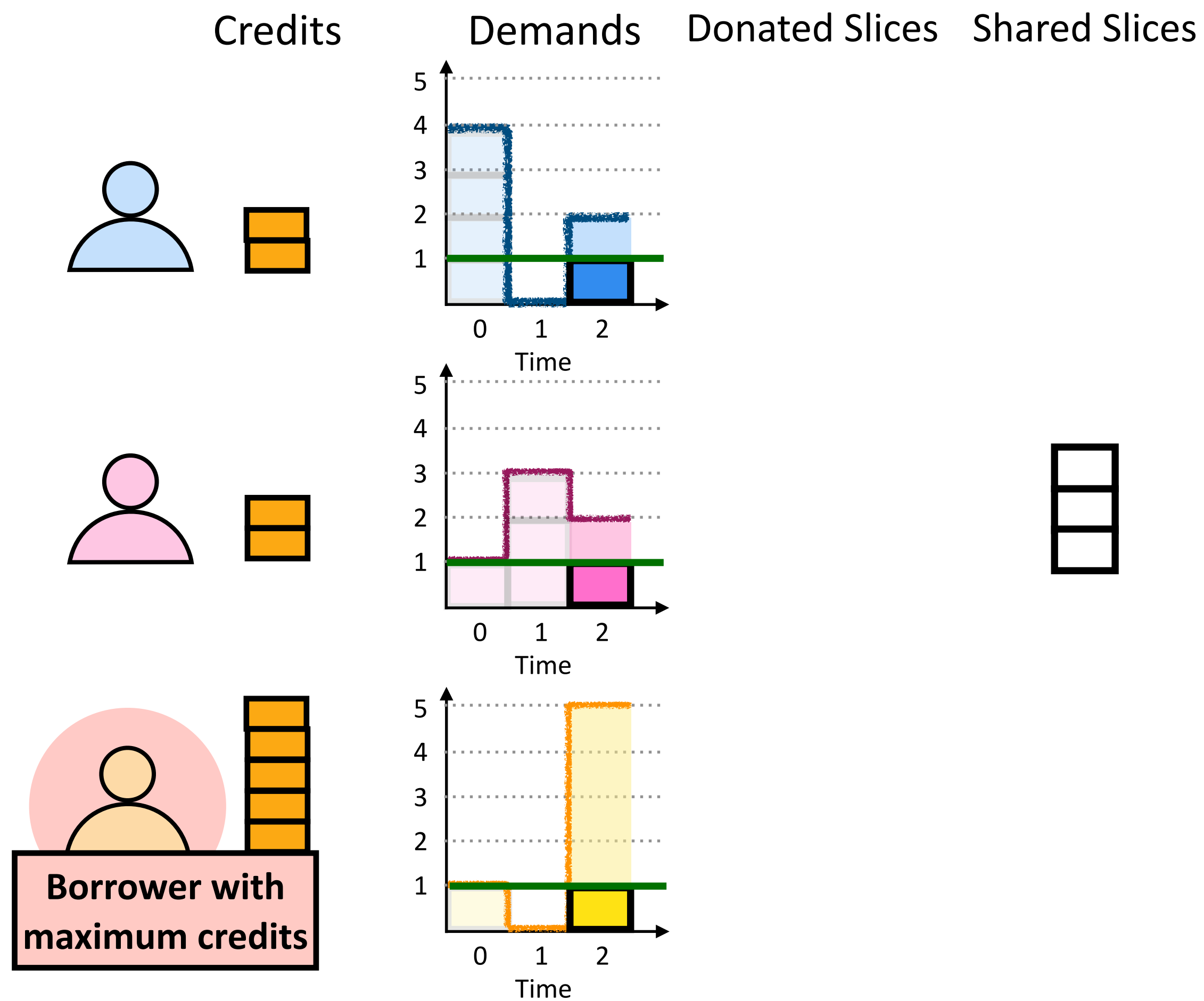
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Karma allocation algorithm

Running Example



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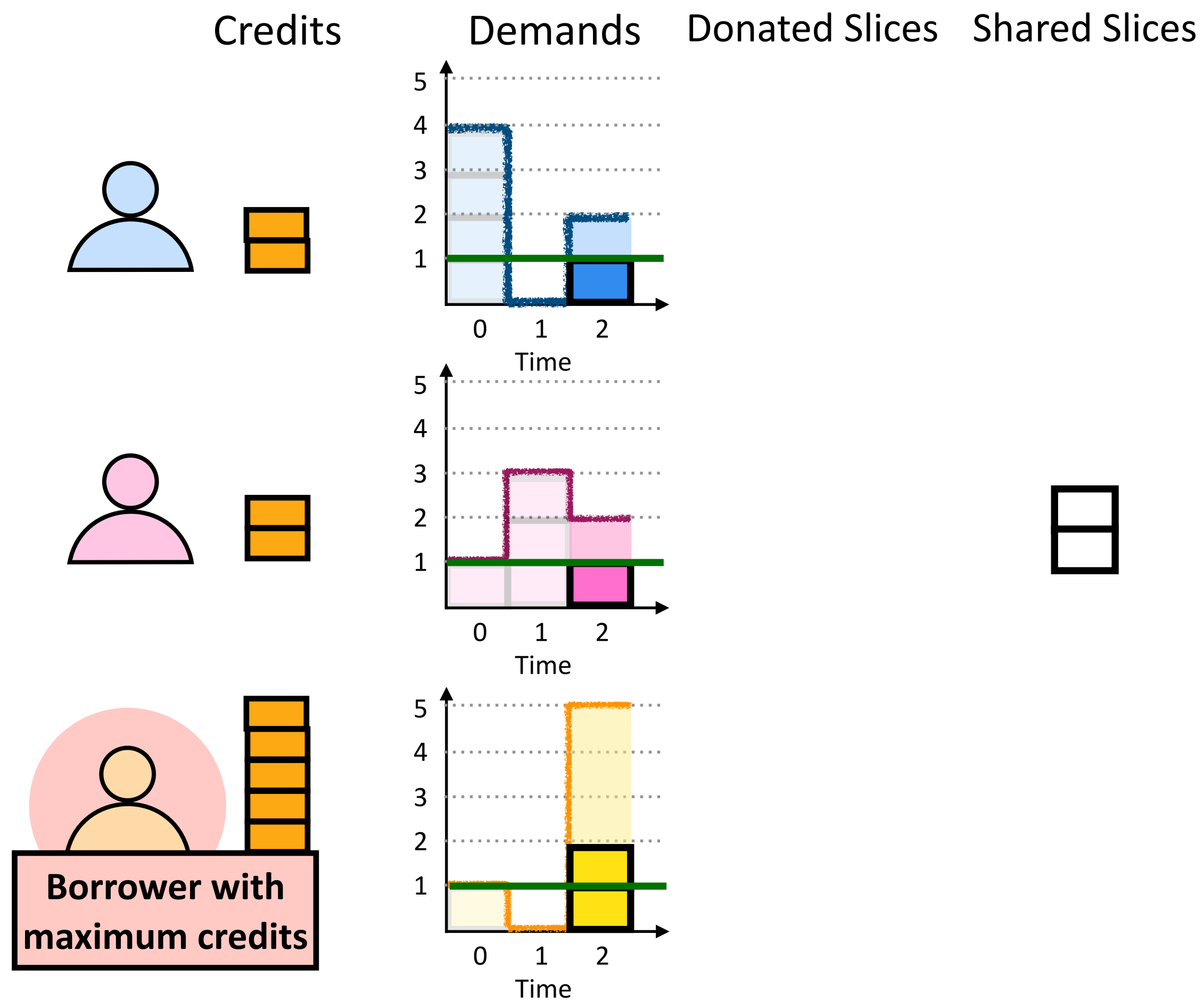
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Karma allocation algorithm

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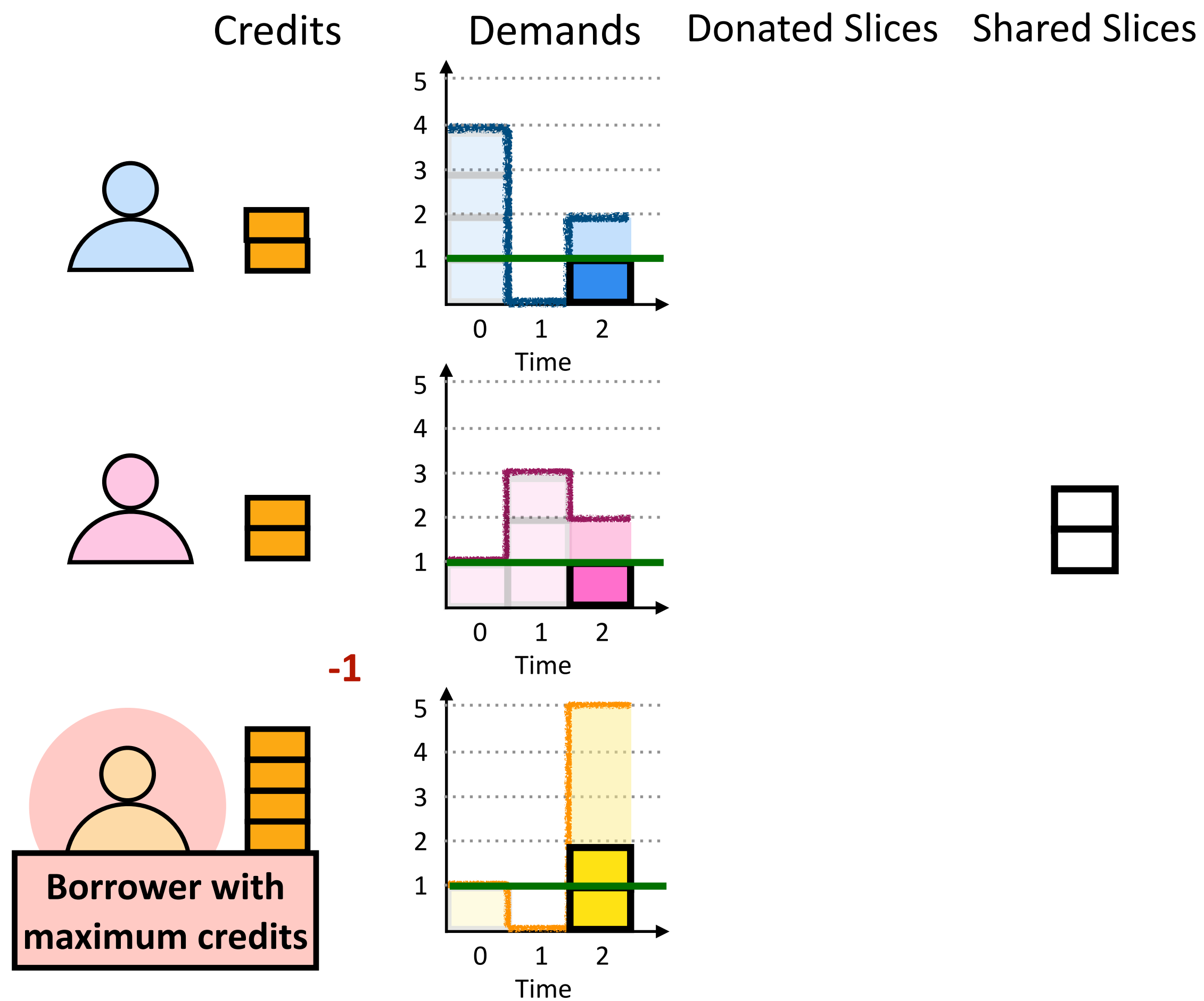
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Karma allocation algorithm

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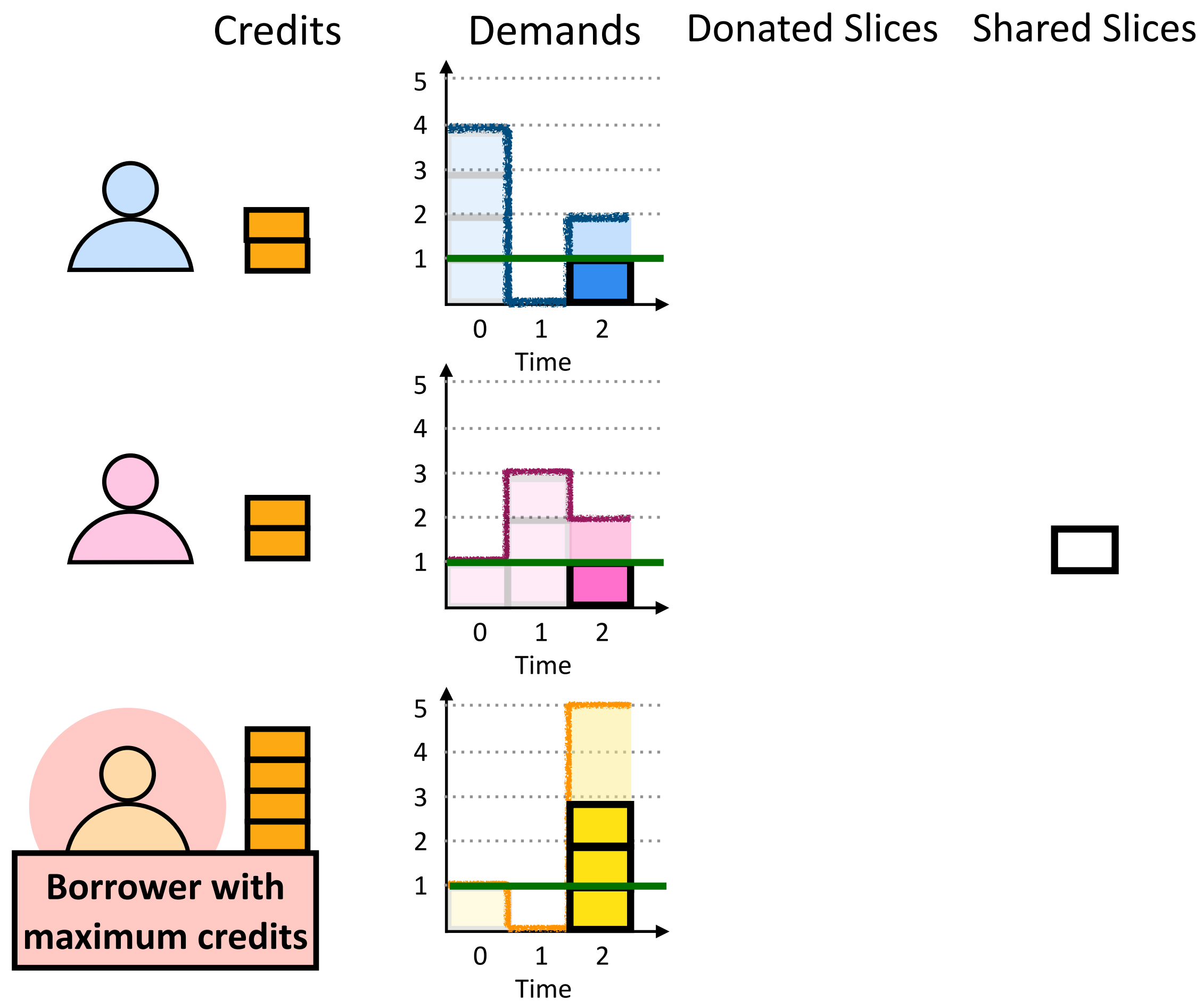
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Karma allocation algorithm

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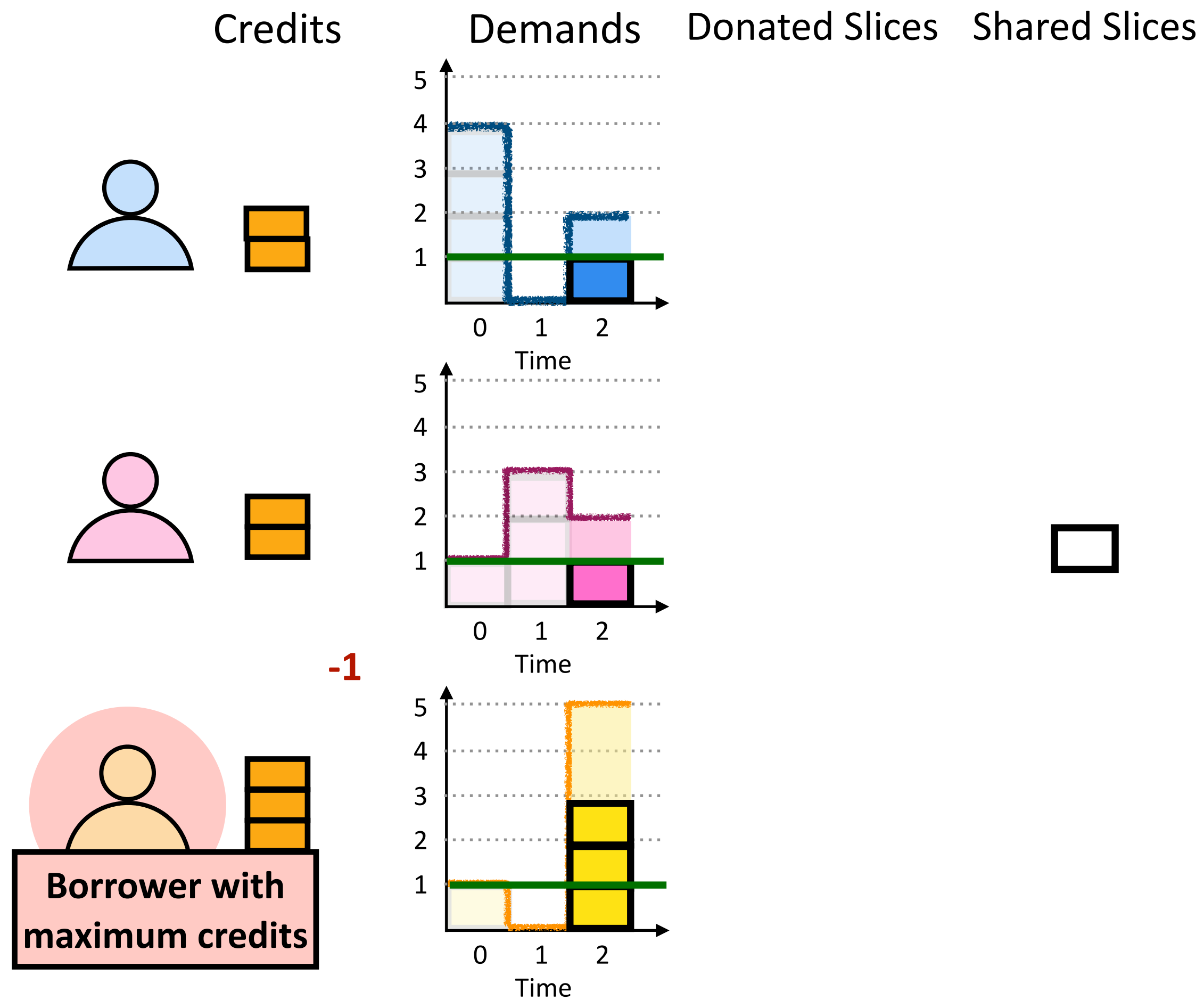
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Karma allocation algorithm

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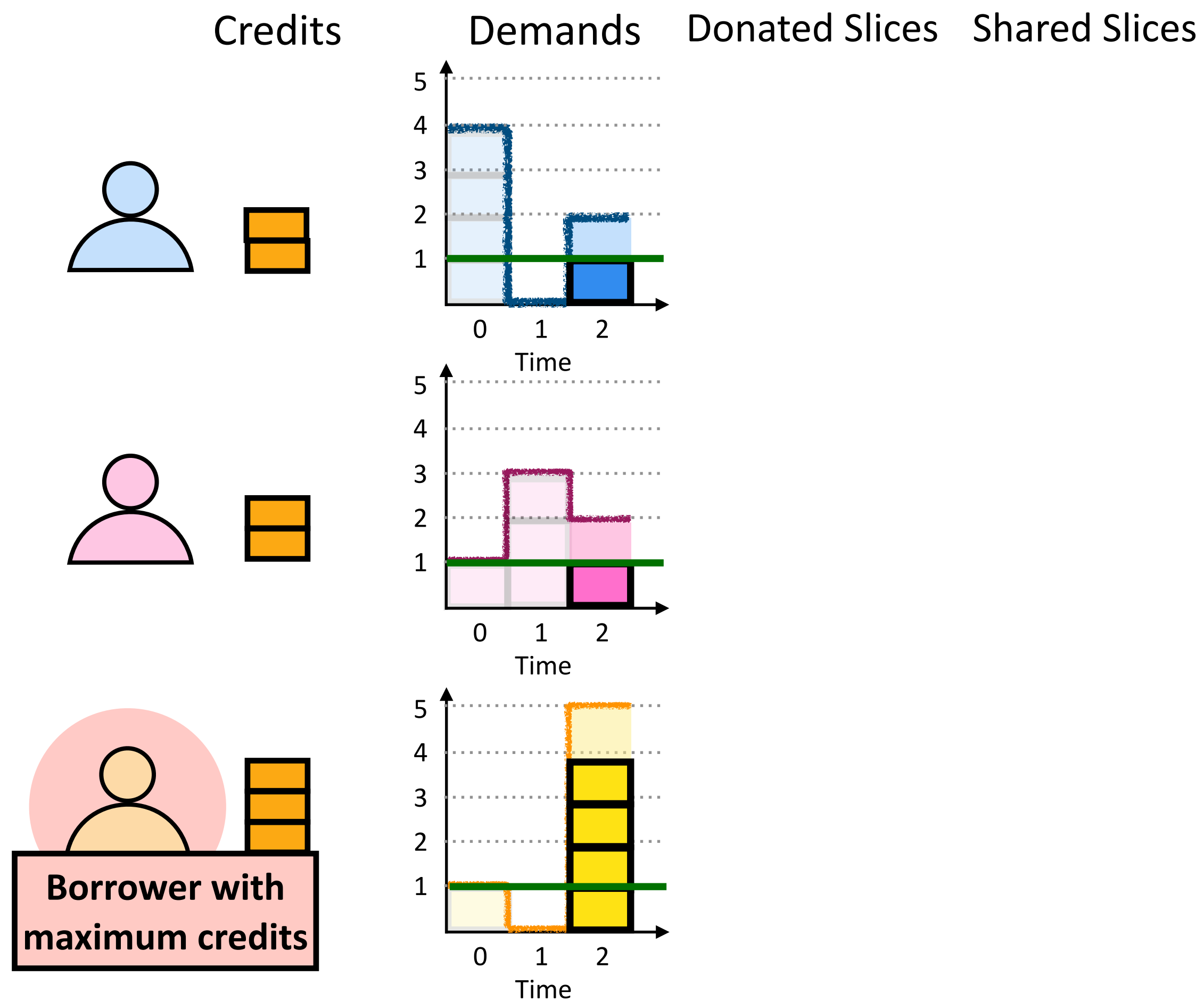
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Karma allocation algorithm

Running Example



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If no donors, then use a shared slice

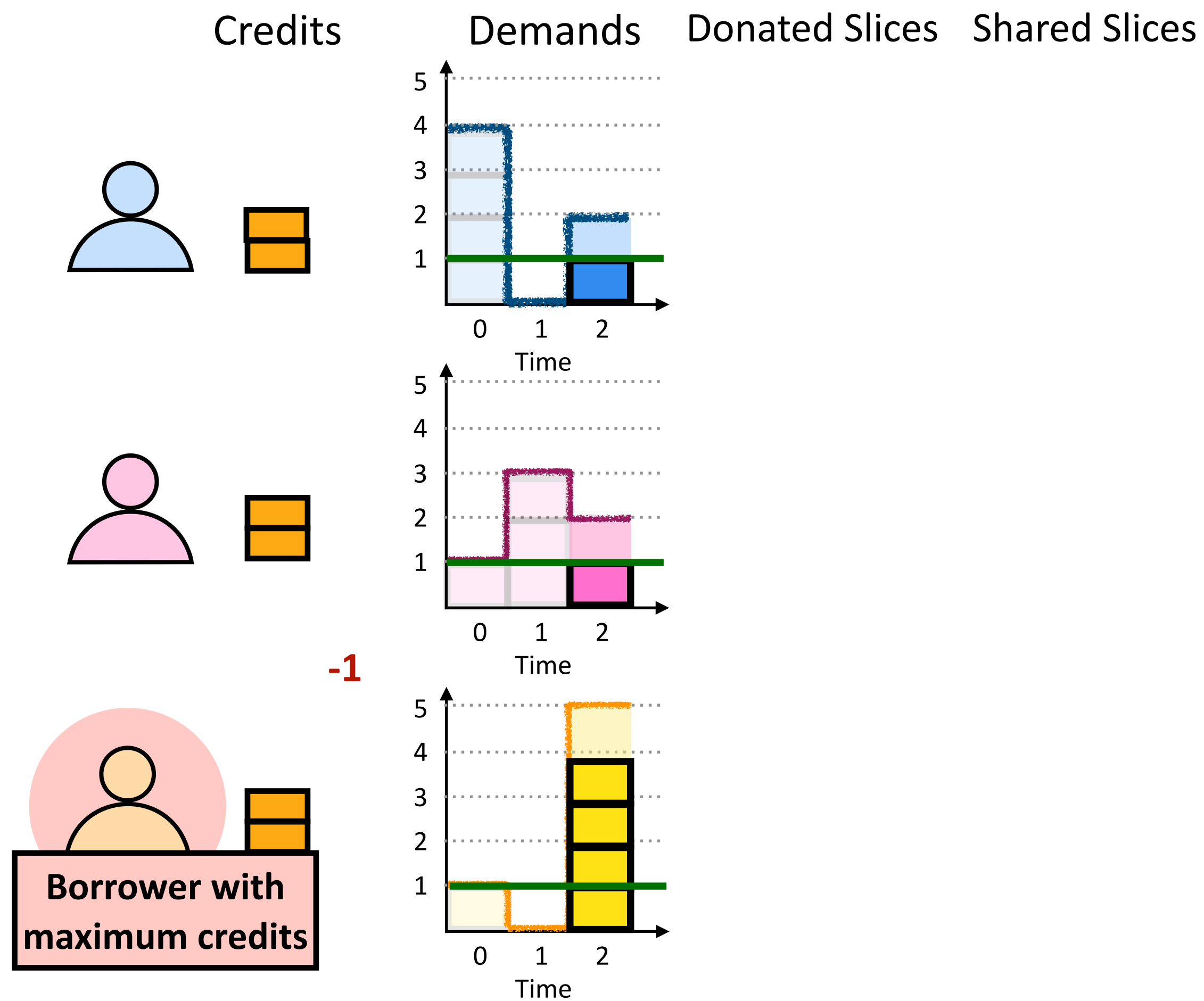
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Karma allocation algorithm

Running Example



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If no donors, then use a shared slice

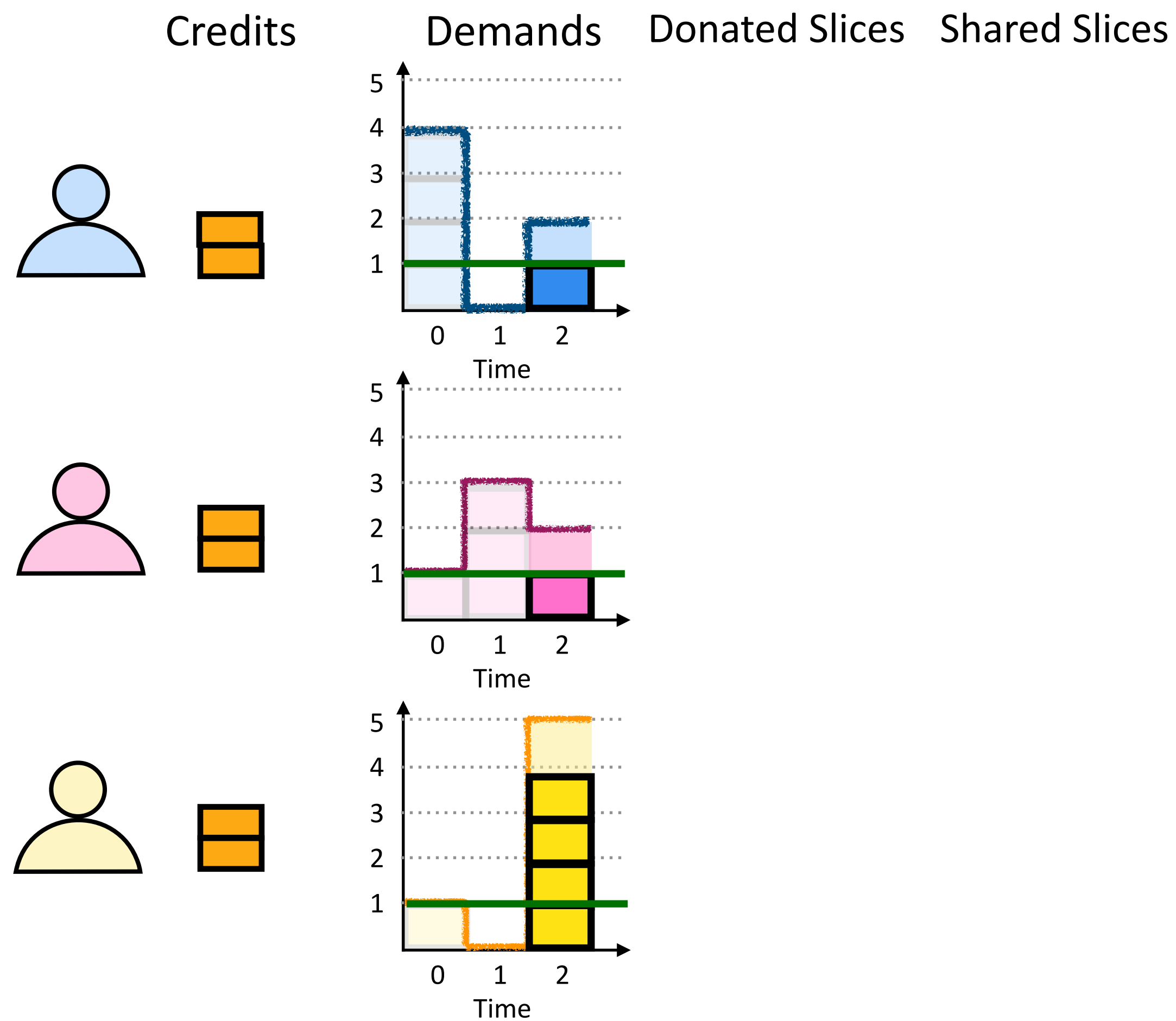
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Karma allocation algorithm

Running Example



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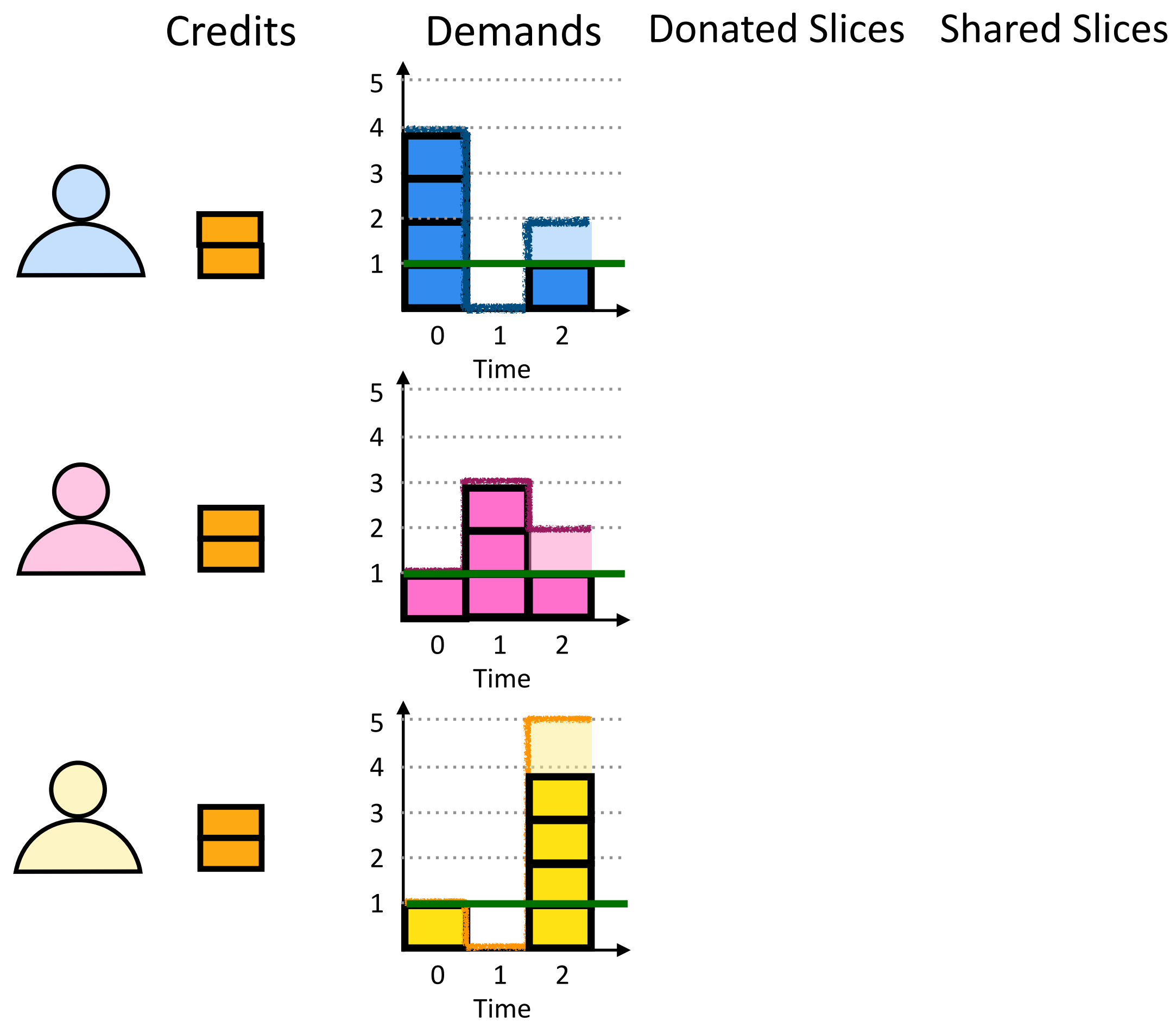
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Karma allocation algorithm

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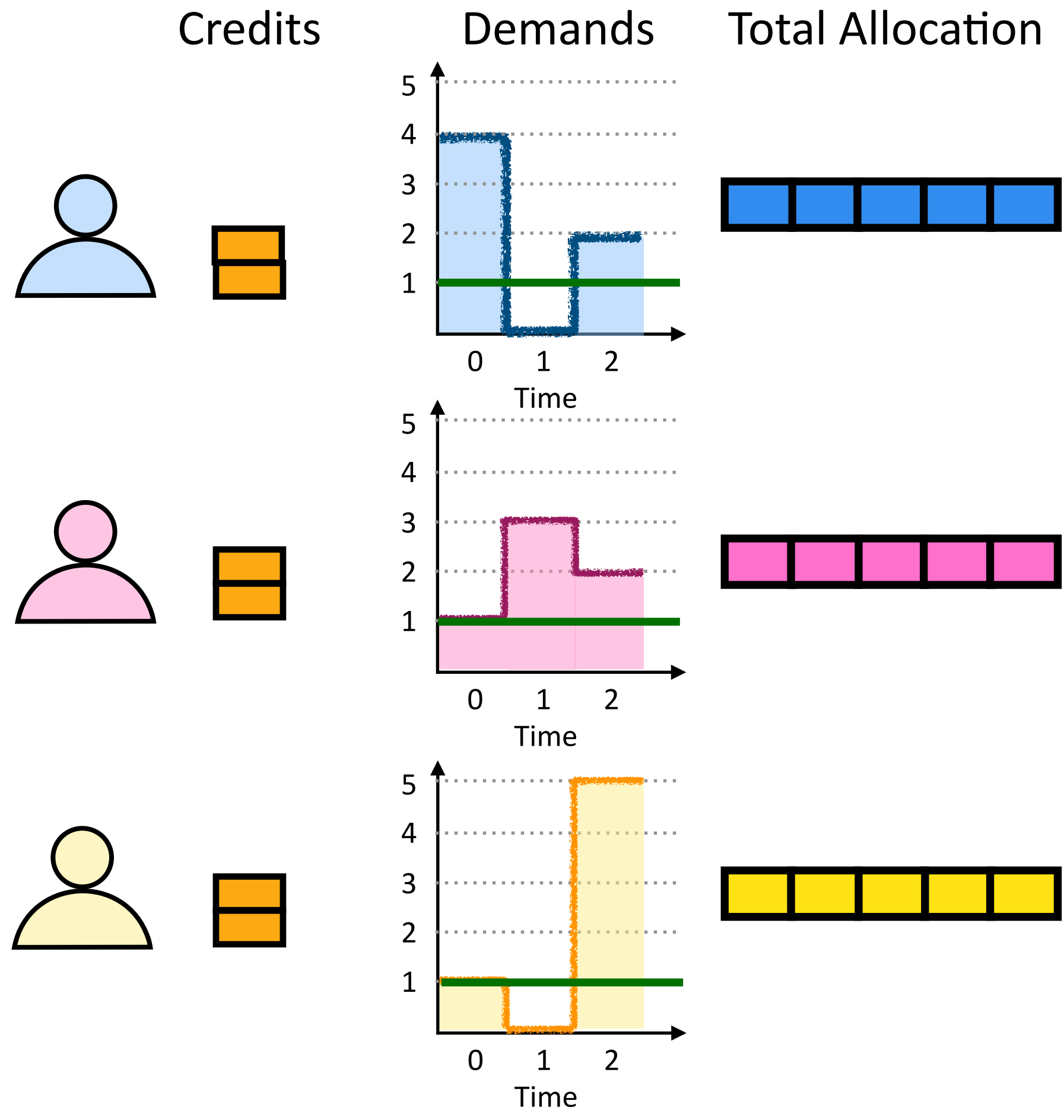
Karma allocation algorithm

Running Example



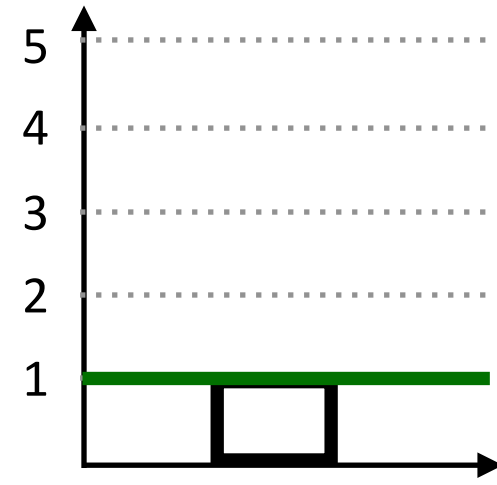
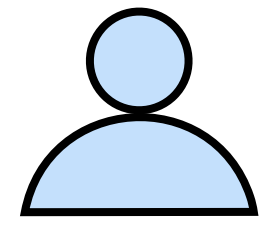
Karma allocation algorithm

Running Example

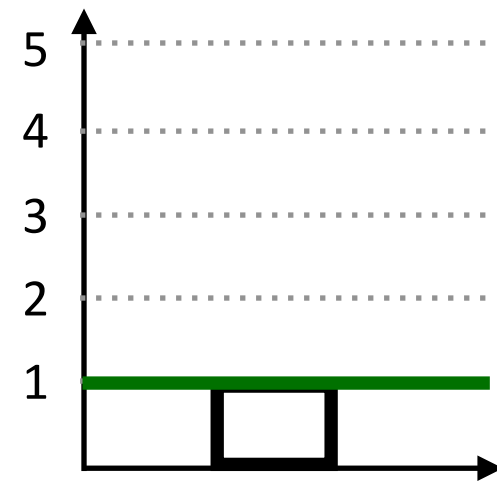
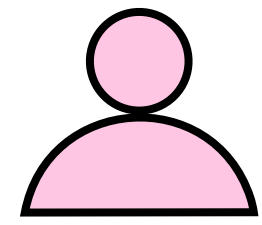


Equal total allocations!

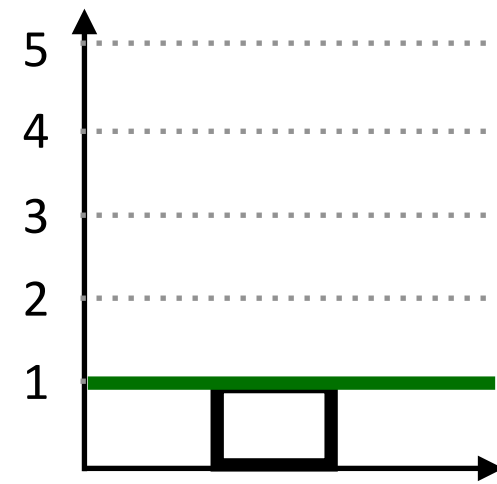
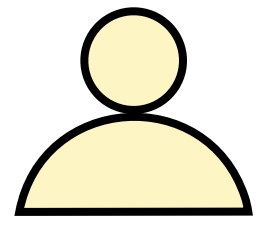
Karma parameterizes the trade-off between instantaneous and long-term fairness



Guaranteed Share

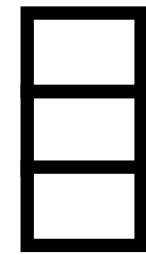


Guaranteed Share

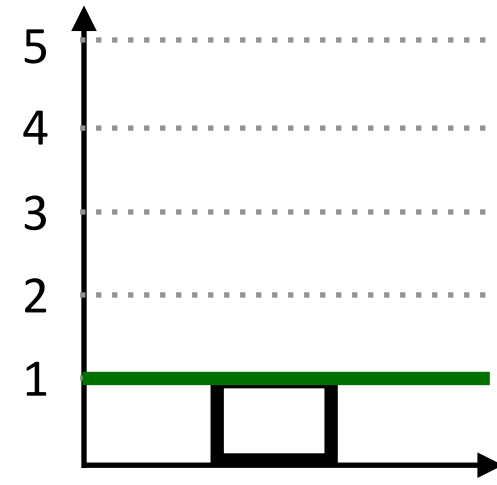
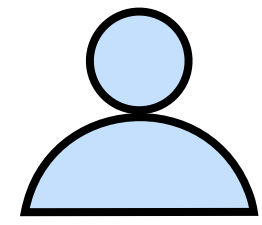


Guaranteed Share

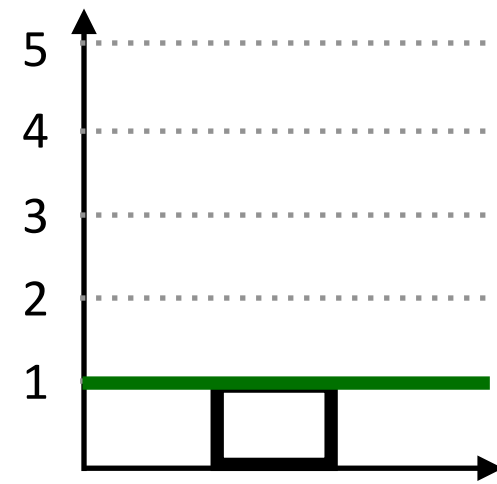
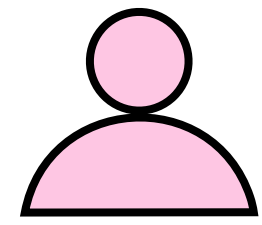
Shared Slices



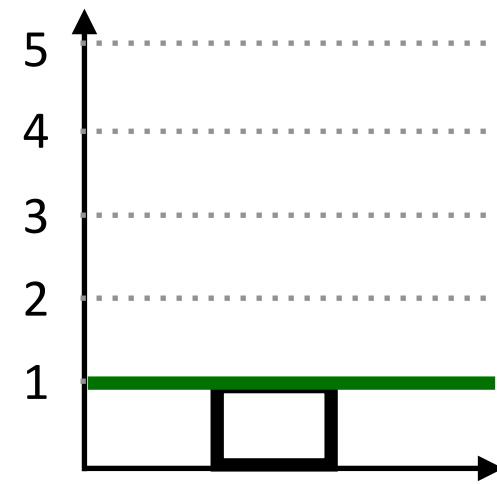
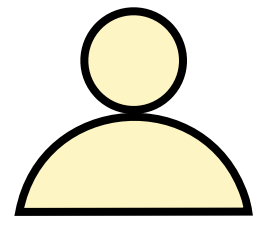
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Guaranteed Share

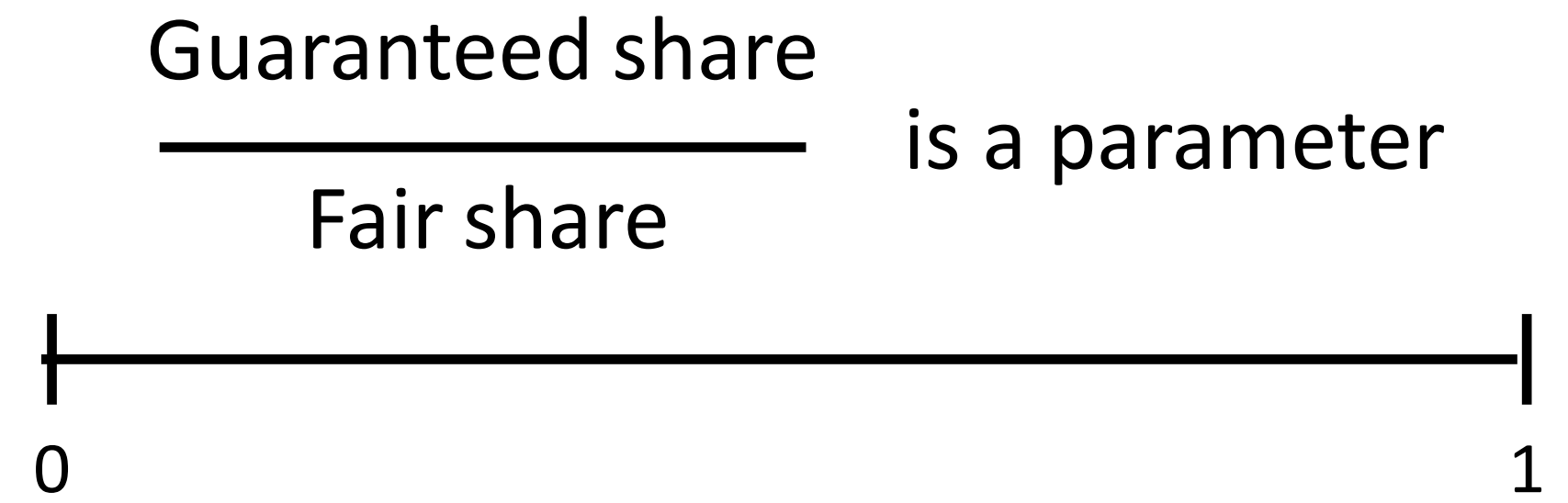
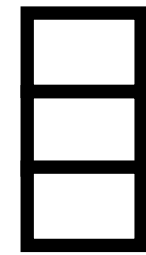


Guaranteed Share

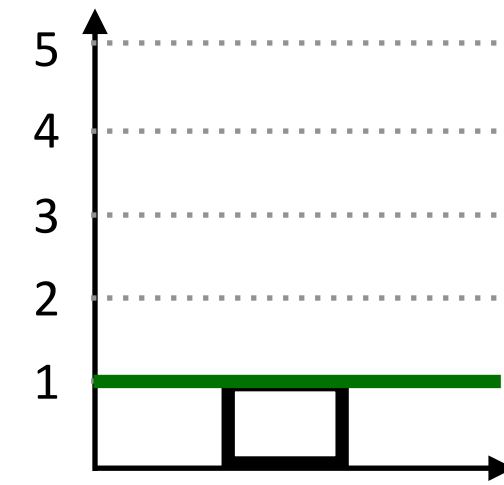
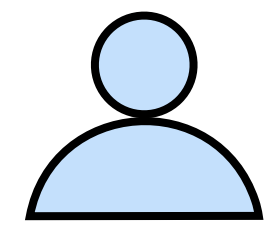


Guaranteed Share

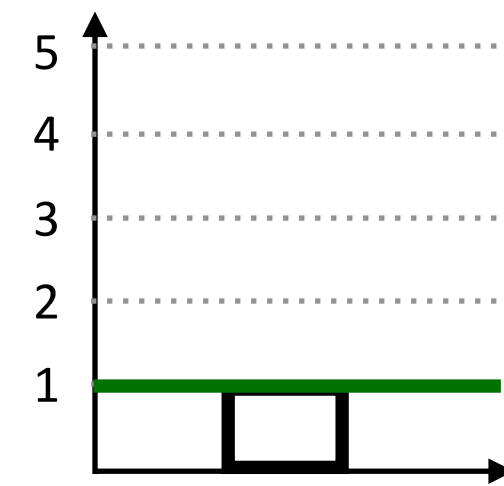
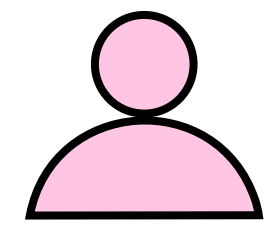
Shared Slices



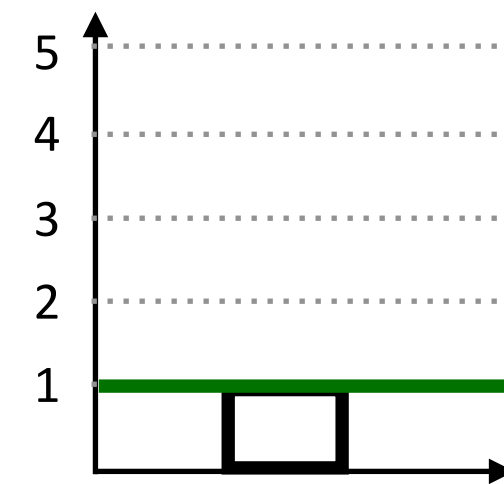
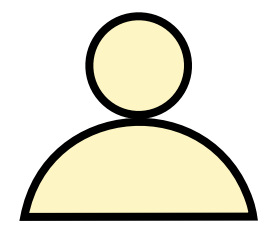
Karma parameterizes the trade-off between instantaneous and long-term fairness



Guaranteed Share

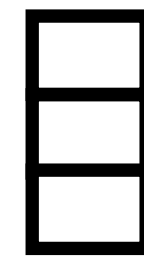


Guaranteed Share



Guaranteed Share

Shared Slices

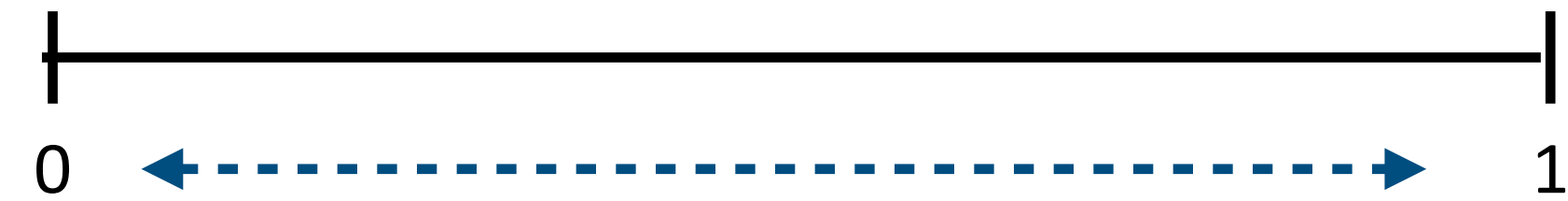


Guaranteed share



Fair share

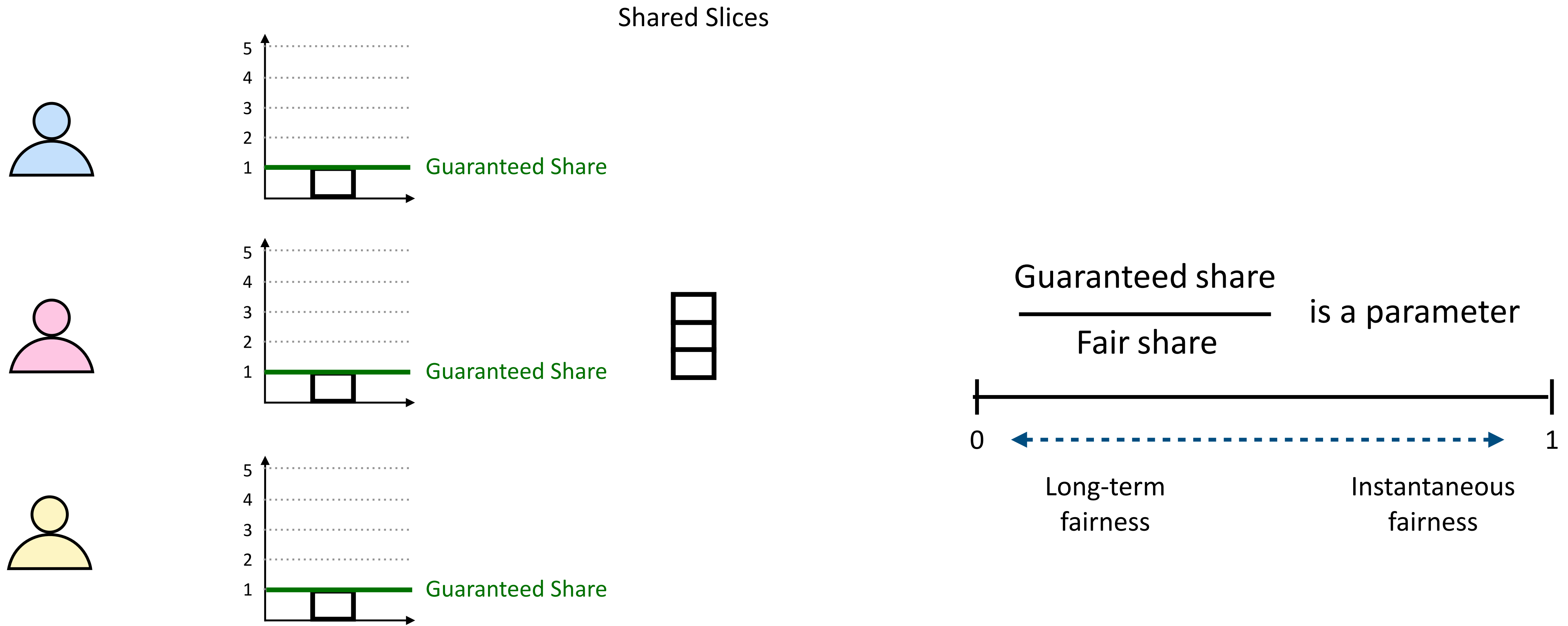
is a parameter



Long-term
fairness

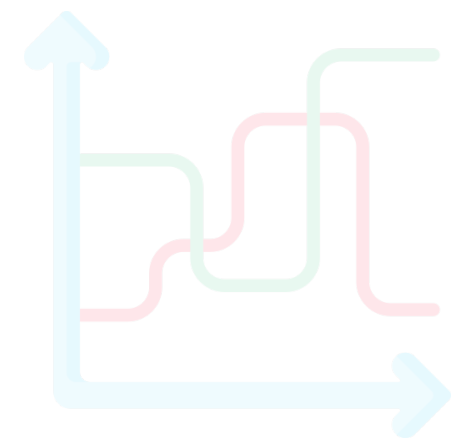
Instantaneous
fairness

Karma parameterizes the trade-off between instantaneous and long-term fairness

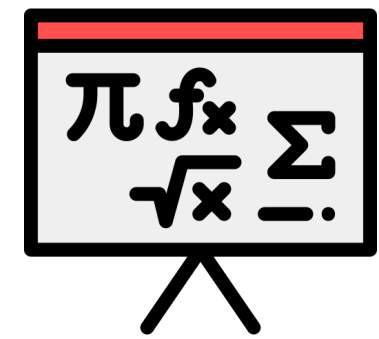


(See paper for more details)

Karma: Revisiting the classical resource allocation problem under dynamic demands



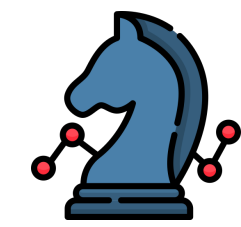
New resource allocation algorithm for dynamic demands



Theoretical guarantees



Pareto efficiency



Strategy-proofness



Fairness



Prototype implementation and evaluation

Karma is Pareto efficient



Pareto efficiency

Resources should not remain unused when there is demand

Karma is Pareto efficient



Pareto efficiency

Resources should not remain unused when there is demand

Karma Allocation Algorithm

 Pick **borrower** with **maximum** credits

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Karma is Pareto efficient



Pareto efficiency

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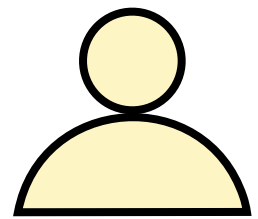
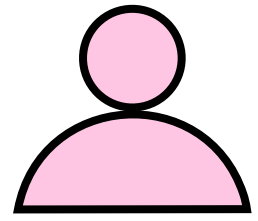
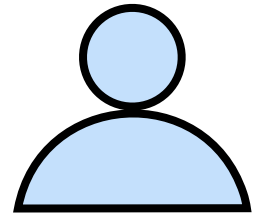
(Repeat until demands satisfied or resources exhausted)

Karma provides powerful strategy-proofness properties



Strategy-proofness

Selfish users cannot increase their allocation by lying
(selfish \neq adversarial)

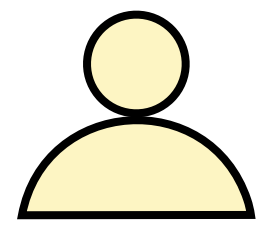
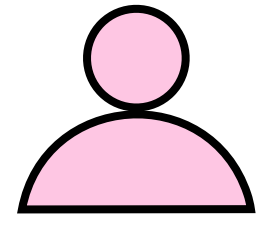
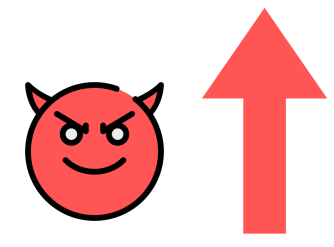
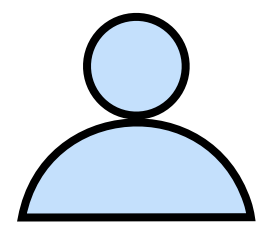


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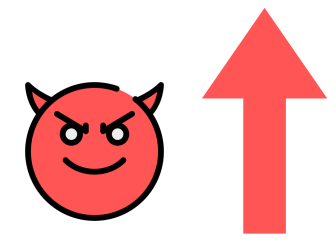
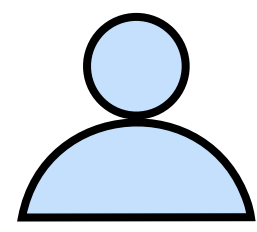


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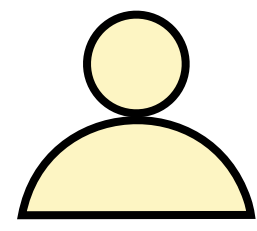
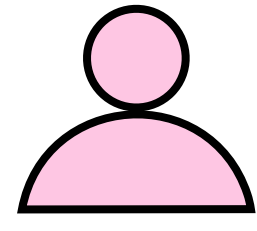


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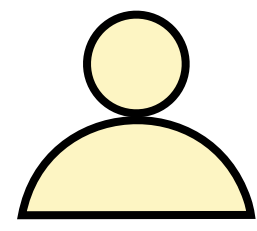
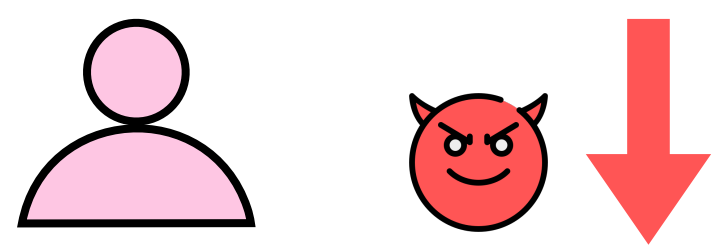


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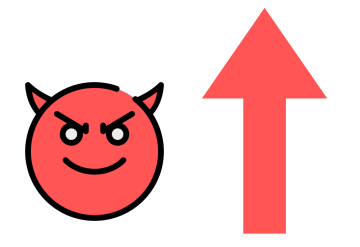
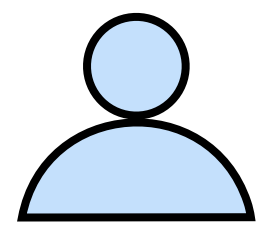


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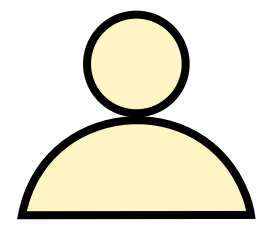
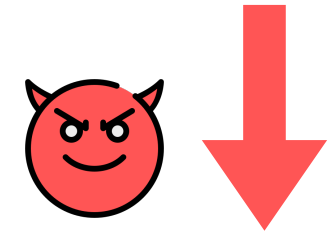
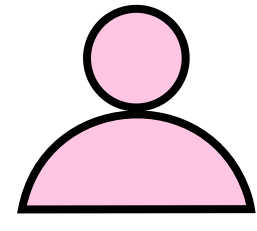
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Not possible to increase allocation

Perfect knowledge of
future demands of all users

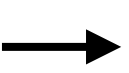
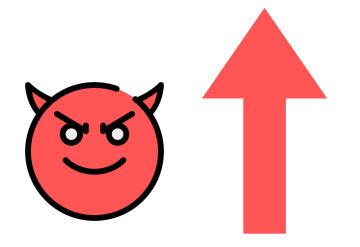
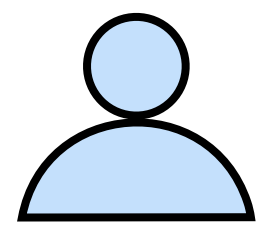


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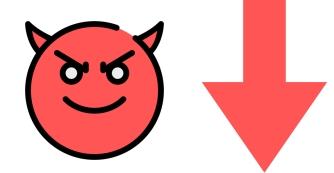
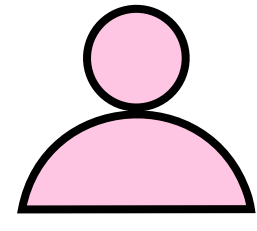
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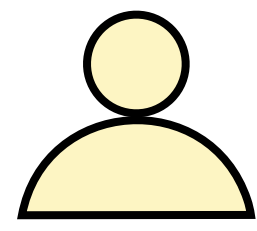


Not possible to increase allocation

Perfect knowledge of
future demands of all users



No more than 1.5x increase in allocation

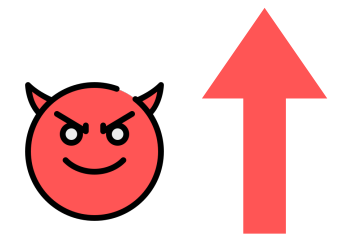
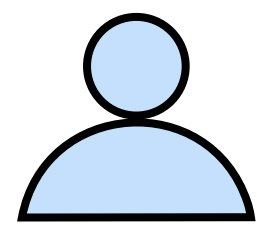


Karma provides powerful strategy-proofness properties



Strategy-proofness

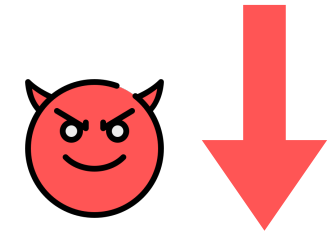
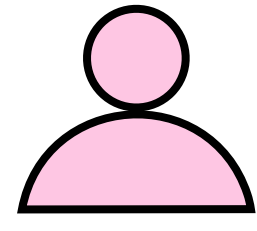
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(selfish ≠ adversarial)



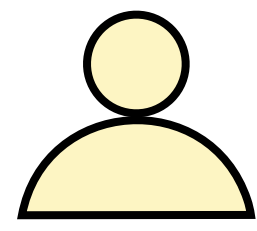
Not possible to increase allocation

Perfect knowledge of
future demands of all users

Far from realistic



No more than 1.5x increase in allocation

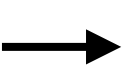
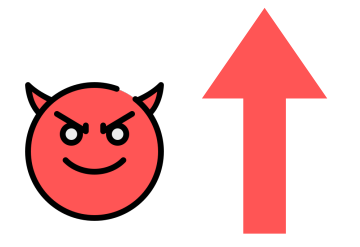
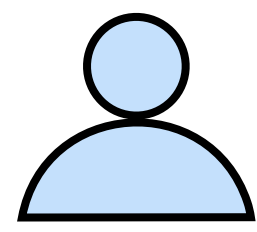


Karma provides powerful strategy-proofness properties



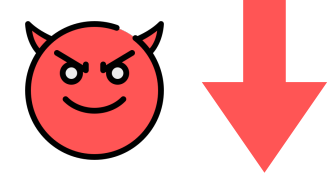
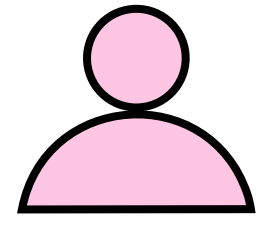
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Selfish users cannot increase their allocation by lying
(selfish \neq adversarial)



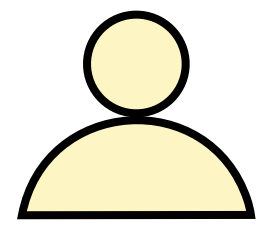
Not possible to increase allocation

Perfect knowledge of
future demands of all users



No more than 1.5x increase in allocation

Any imprecision in knowledge of
future demands of any user

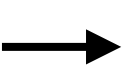
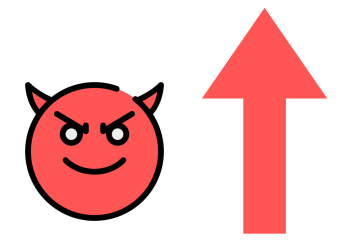
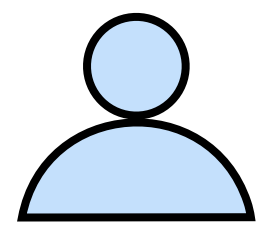


Karma provides powerful strategy-proofness properties



Strategy-proofness

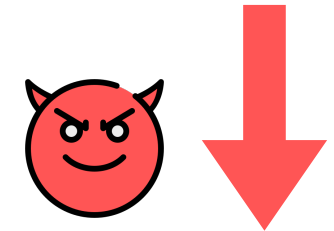
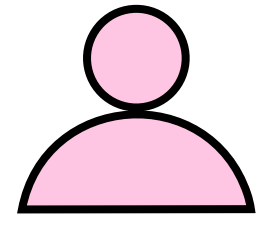
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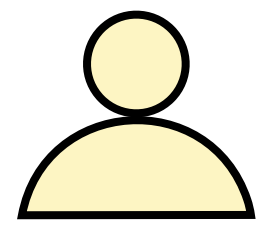
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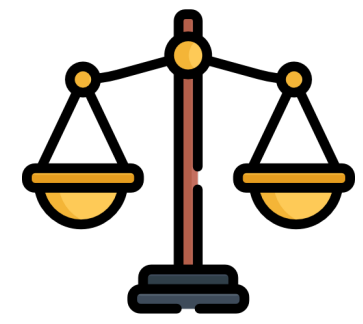


No more than 1.5x increase in allocation

As much as $\Omega(n)$ factor decrease in allocation

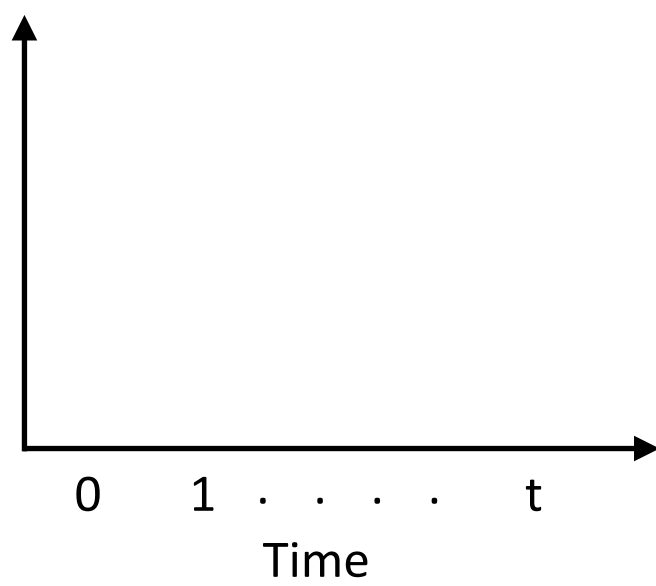
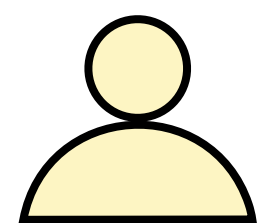
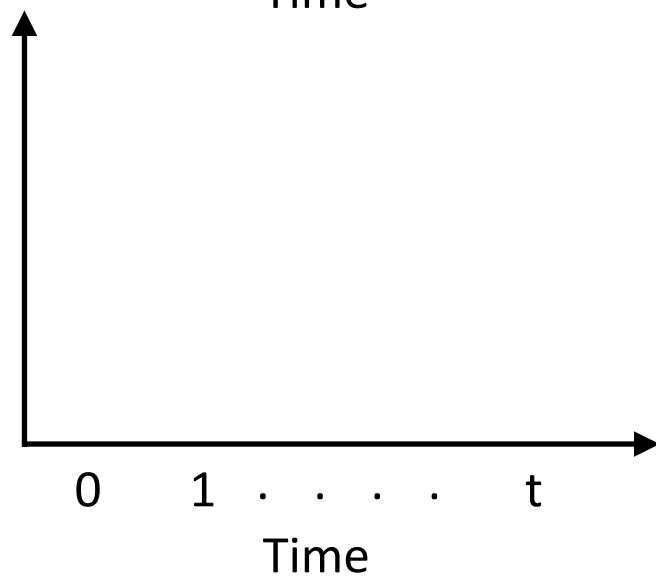
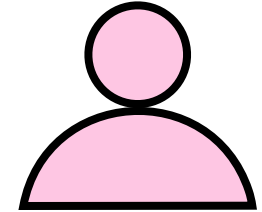
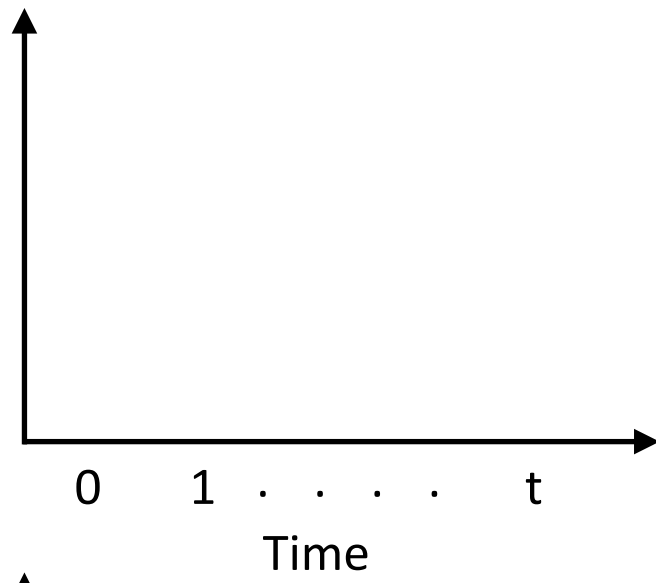
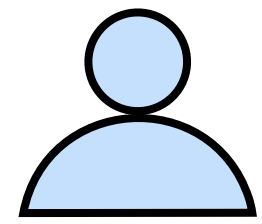


Karma maximizes the minimum total allocation (given past allocations)

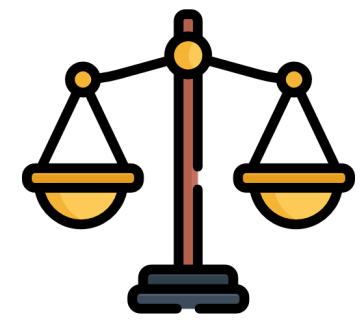


Fairness

Balanced resource allocations across users



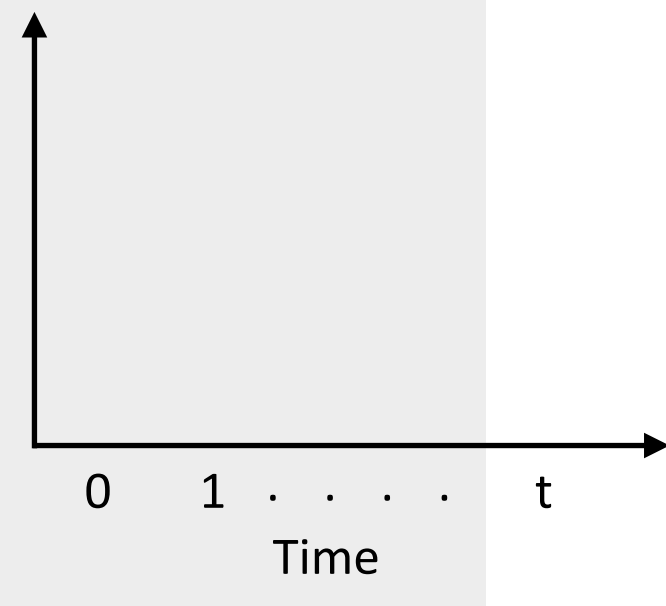
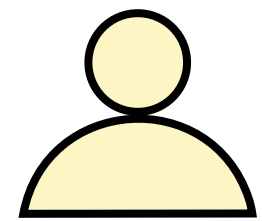
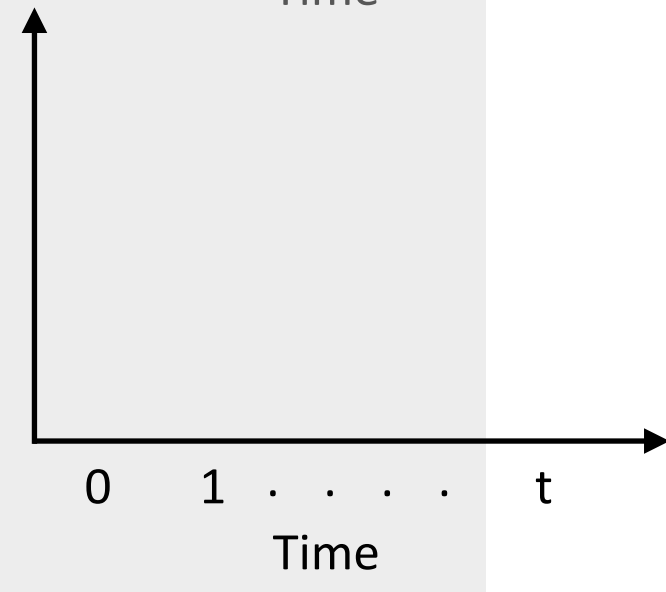
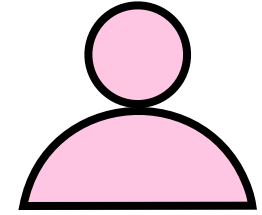
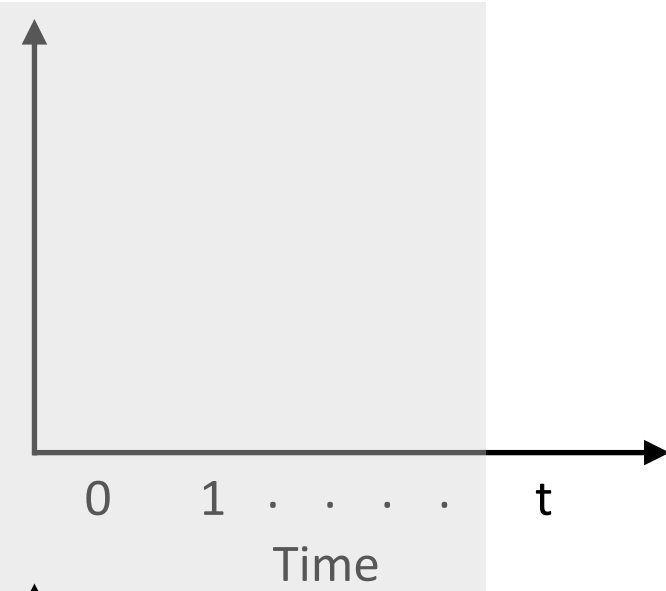
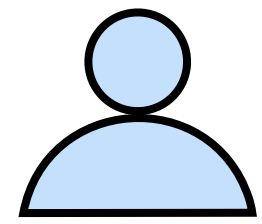
Karma maximizes the minimum total allocation (given past allocations)



Fairness

Balanced resource allocations across users

Fixed past allocations



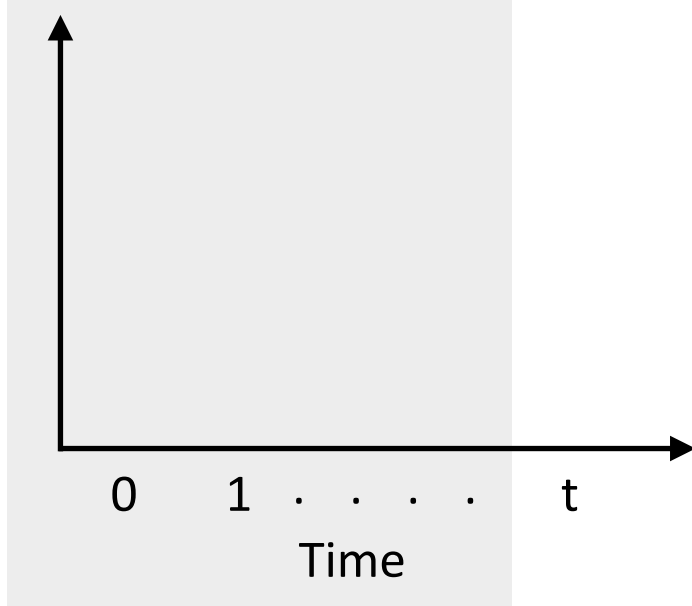
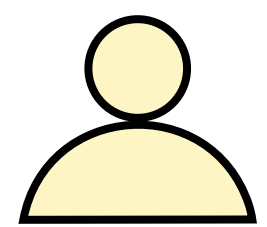
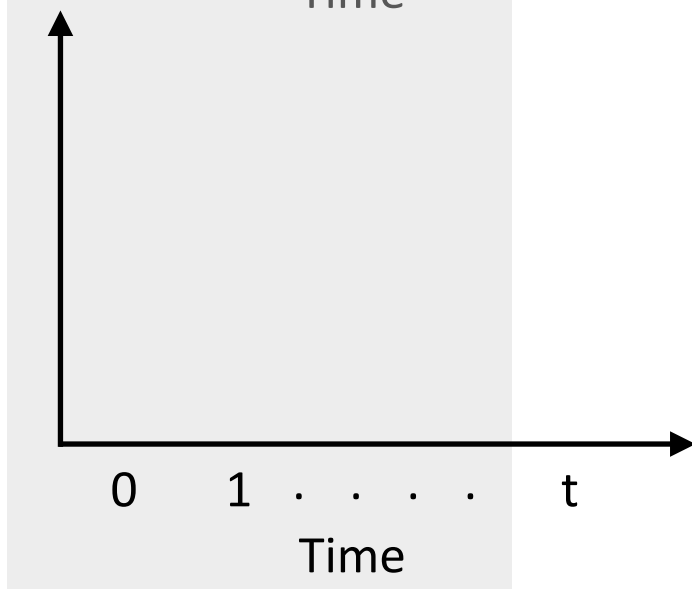
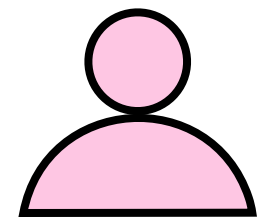
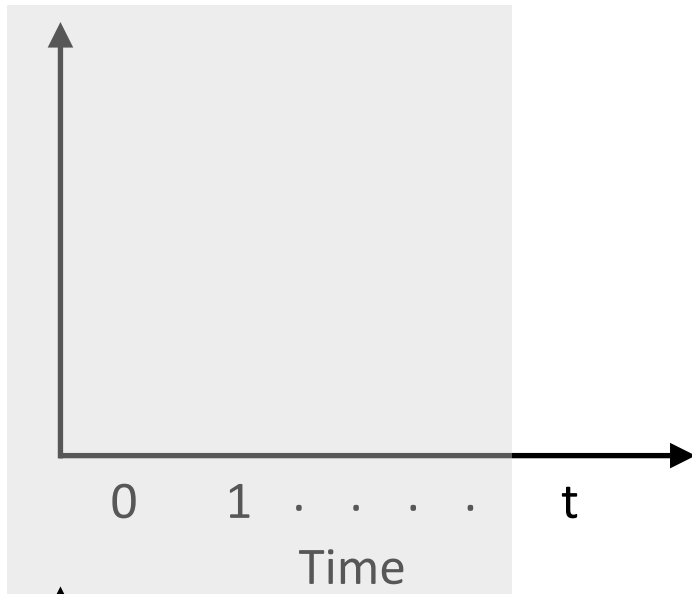
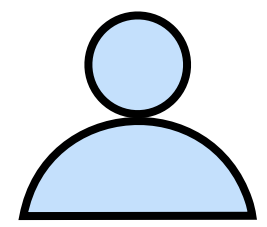
Karma maximizes the minimum total allocation (given past allocations)



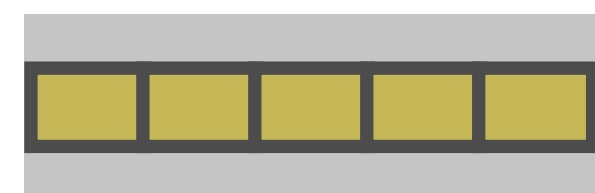
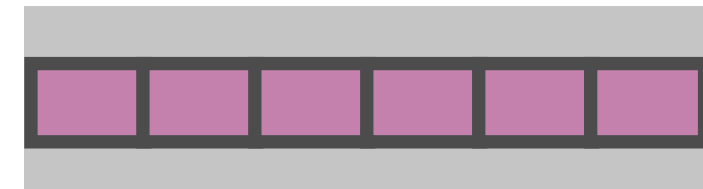
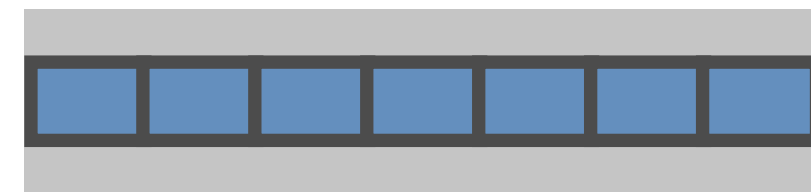
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Balanced resource allocations across users

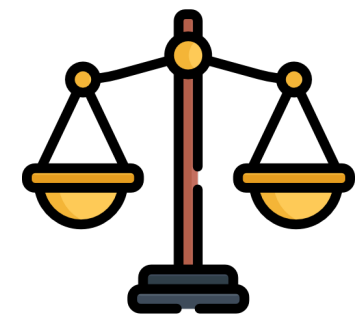
Fixed past allocations



Total Allocation (from 0 to t-1)



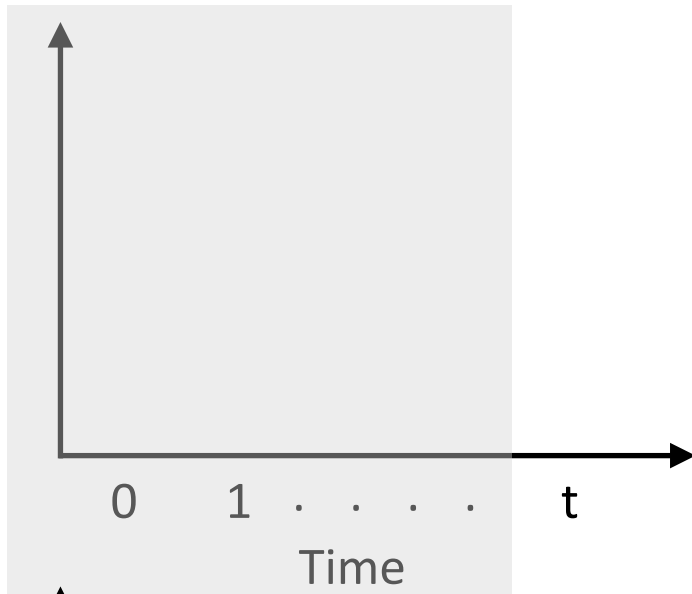
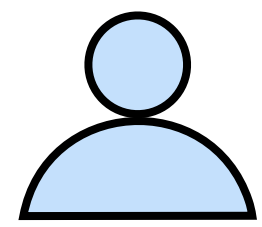
Karma maximizes the minimum total allocation (given past allocations)



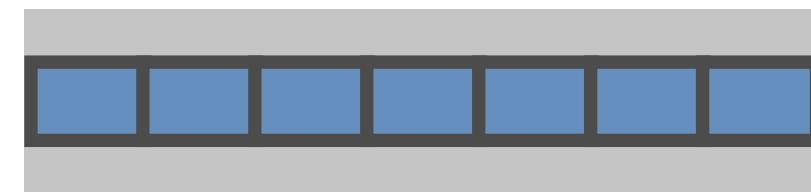
Fairness

Balanced resource allocations across users

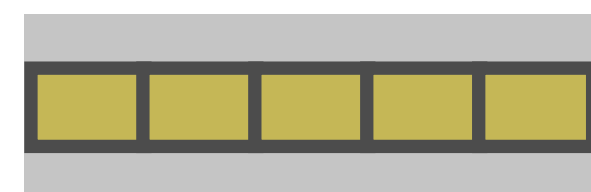
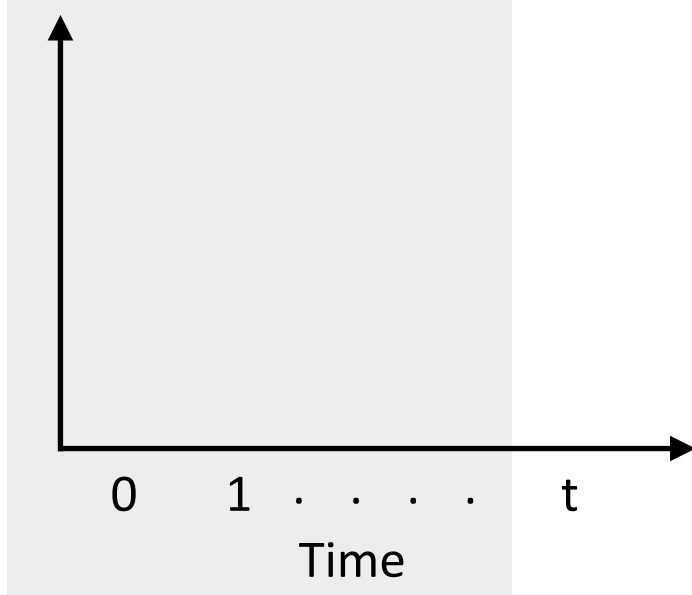
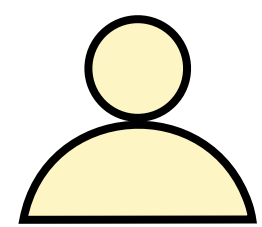
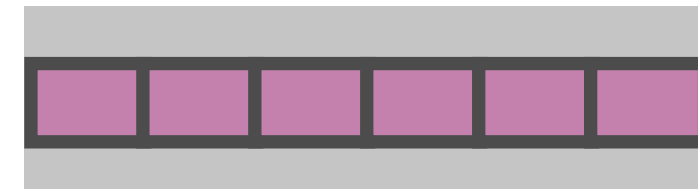
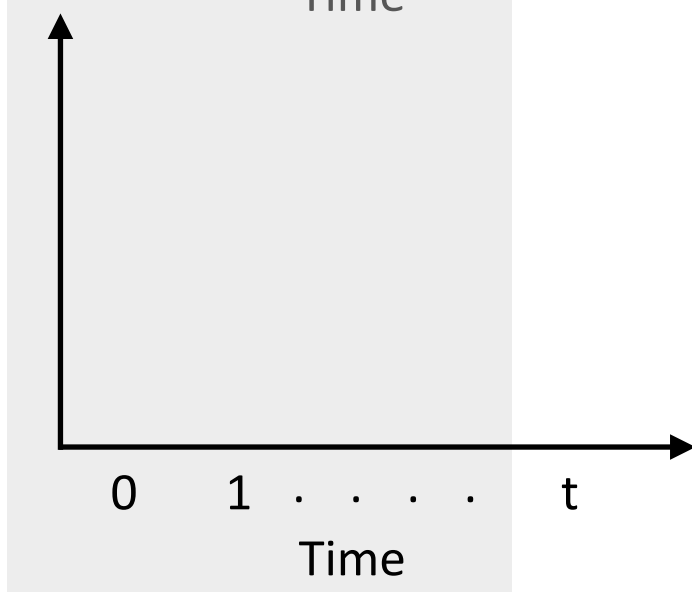
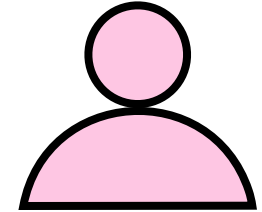
Fixed past allocations



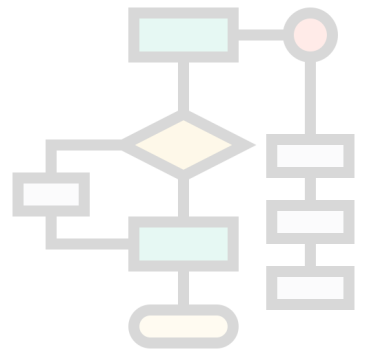
Total Allocation (from 0 to t-1)



Credits



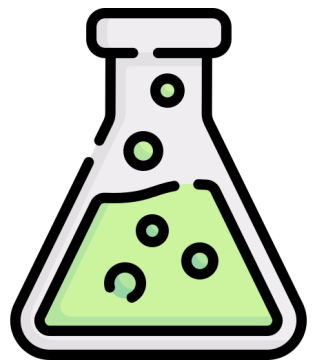
Karma: Resource Allocation for Dynamic Demands



New credit-based resource allocation algorithm



Strong theoretical guarantees



Prototype implementation and evaluation

Karma implementation & evaluation

Karma implementation & evaluation

Implemented in distributed elastic memory system (Jiffy [Eurosys'22])

Karma implementation & evaluation

Implemented in distributed elastic memory system (Jiffy [Eurosys'22])

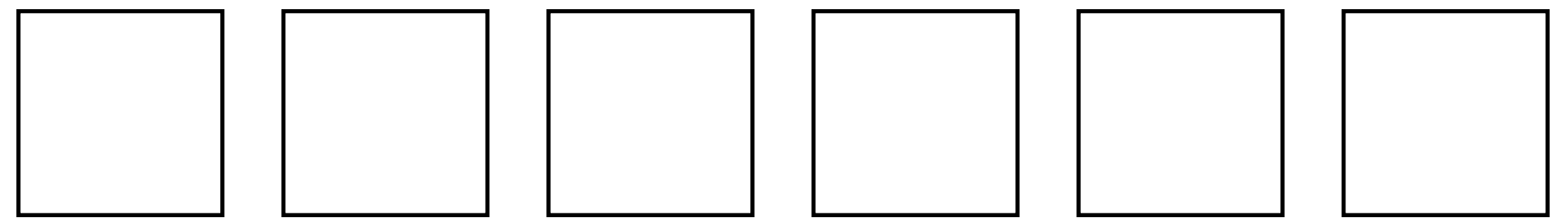
Evaluated in-memory key-value cache scenario

Karma implementation & evaluation

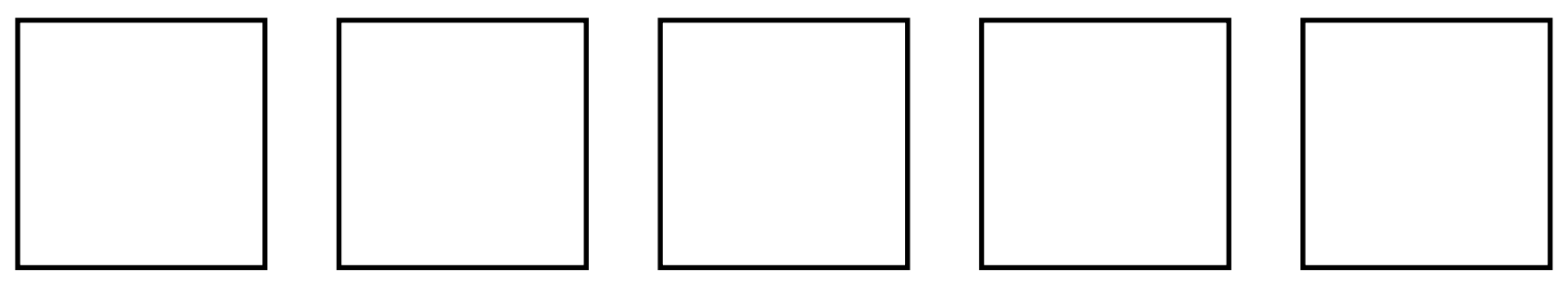
Implemented in distributed elastic memory system (Jiffy [Eurosys'22])

Evaluated in-memory key-value cache scenario

Experimental Setup



EC2 VMs

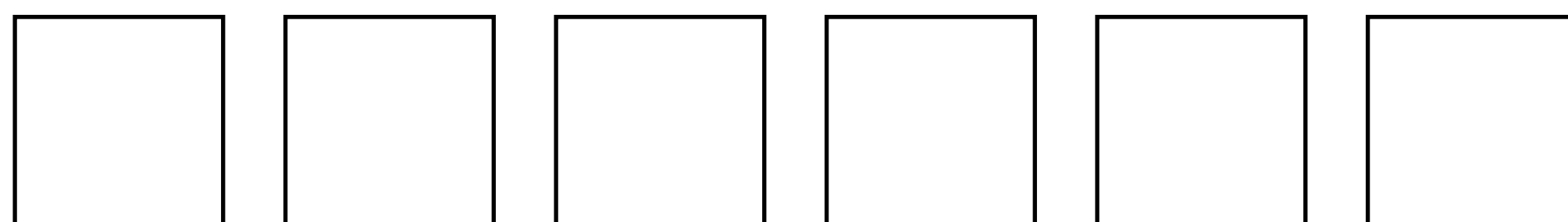


Karma implementation & evaluation

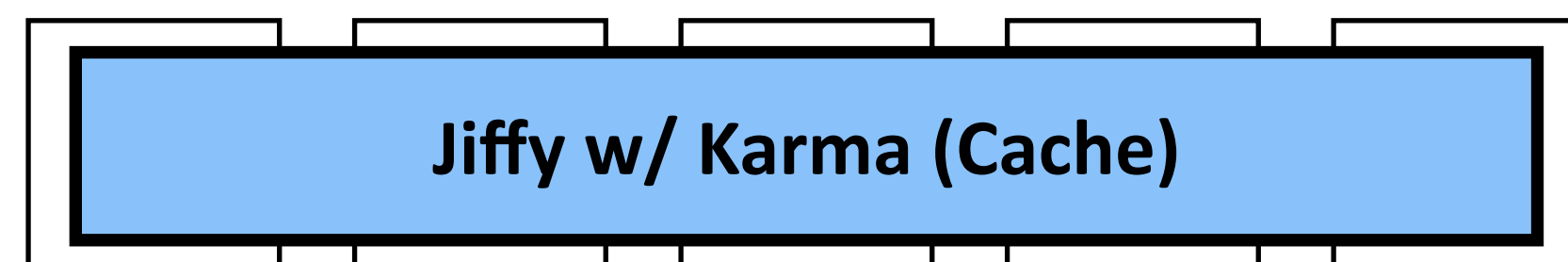
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Experimental Setup



EC2 VMs

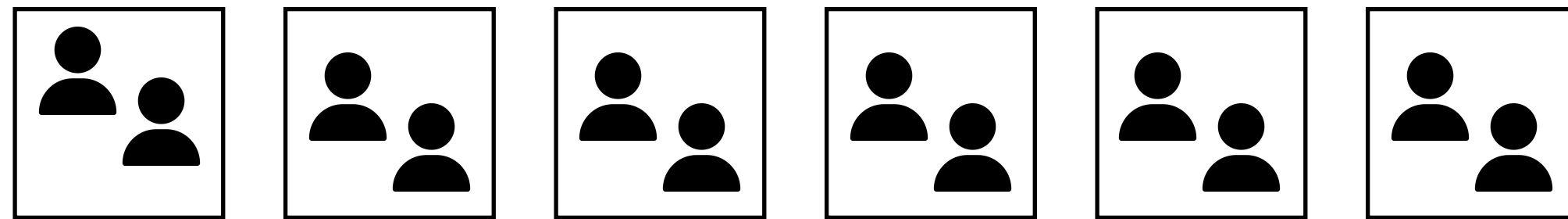


Karma implementation & evaluation

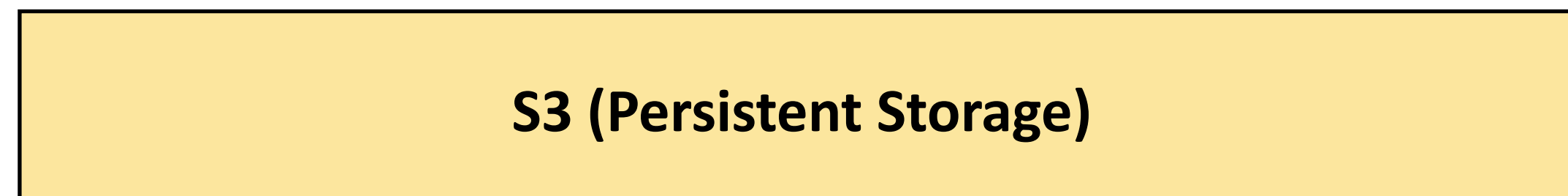
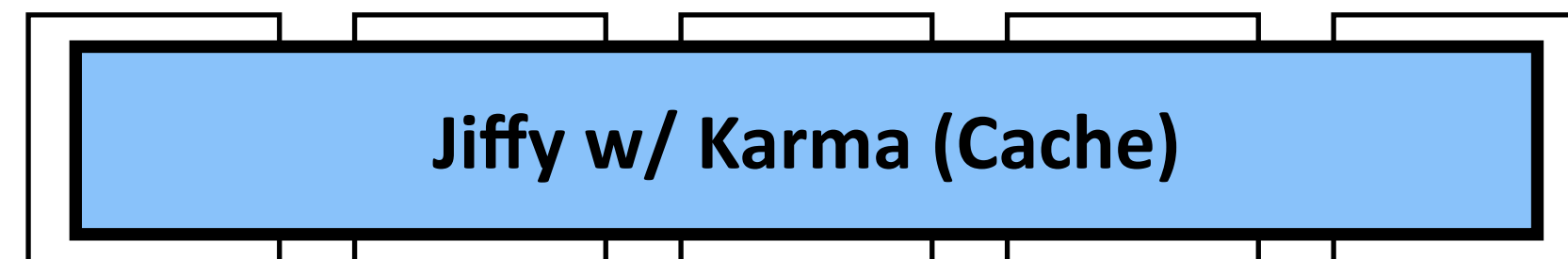
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Experimental Setup



EC2 VMs

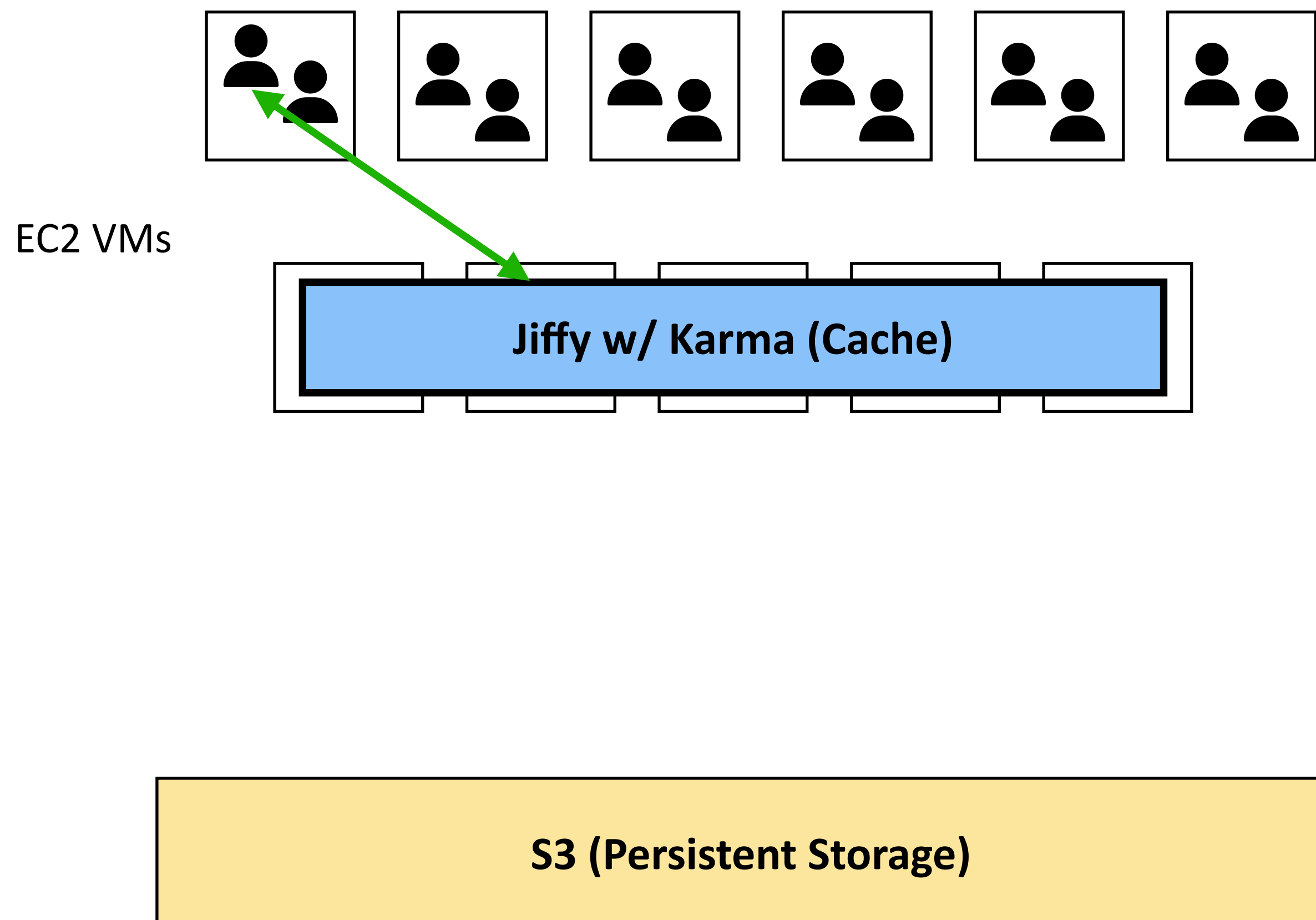


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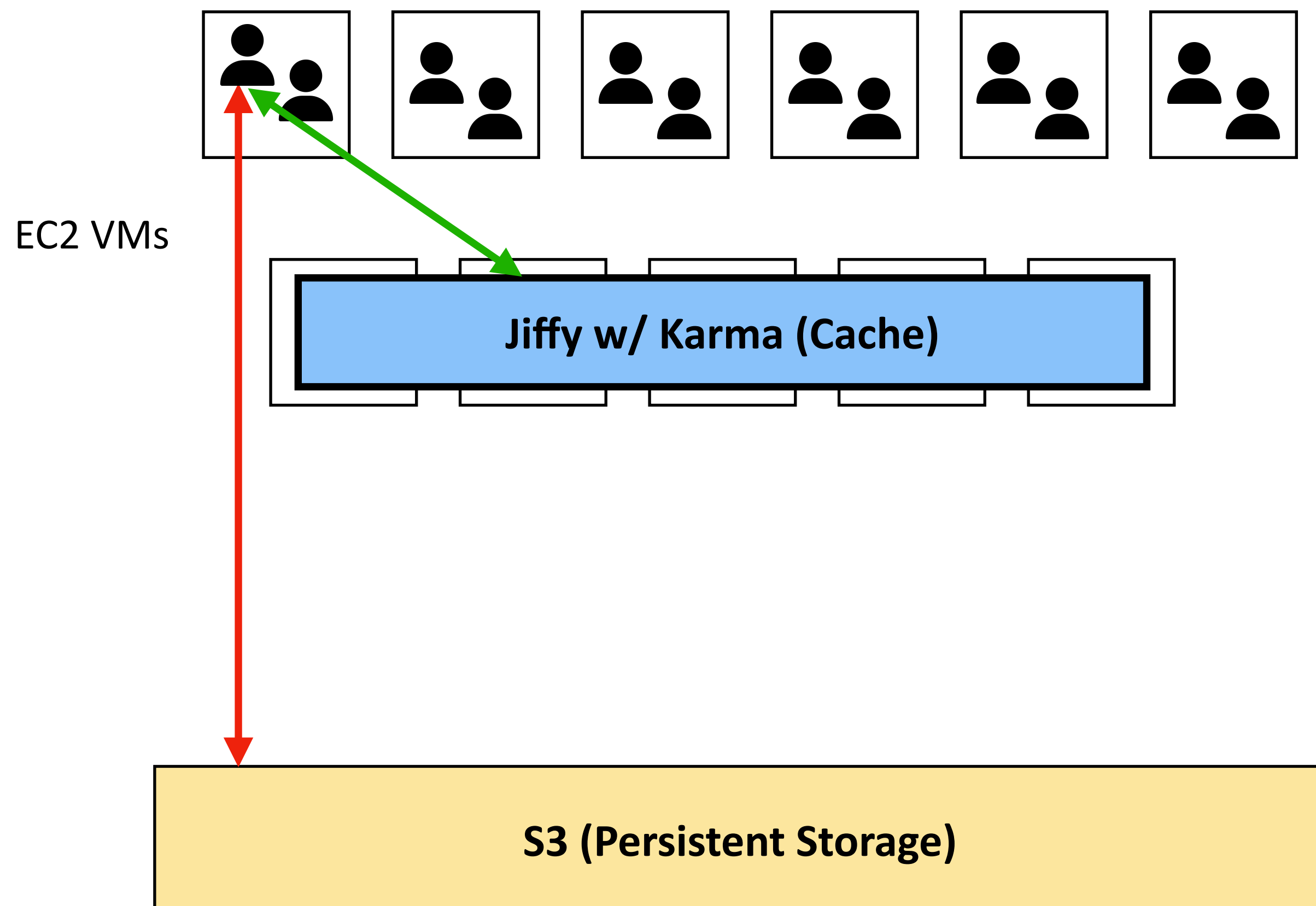


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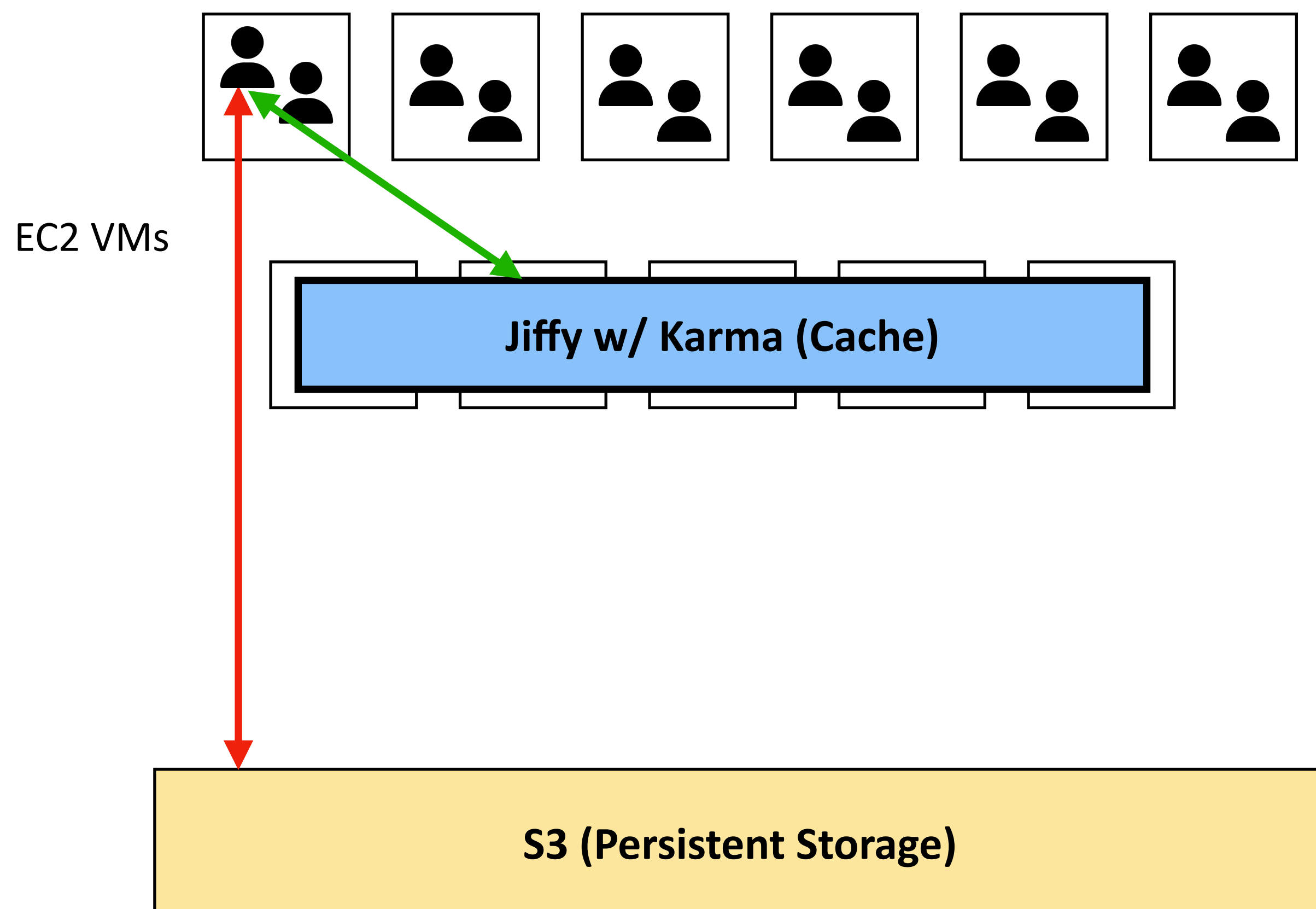


Karma implementation & evaluation

Implemented in distributed elastic memory system (Jiffy [Eurosys'22])

Evaluated in-memory key-value cache scenario

Experimental Setup



Workload

Dynamic demands -> vary working set size

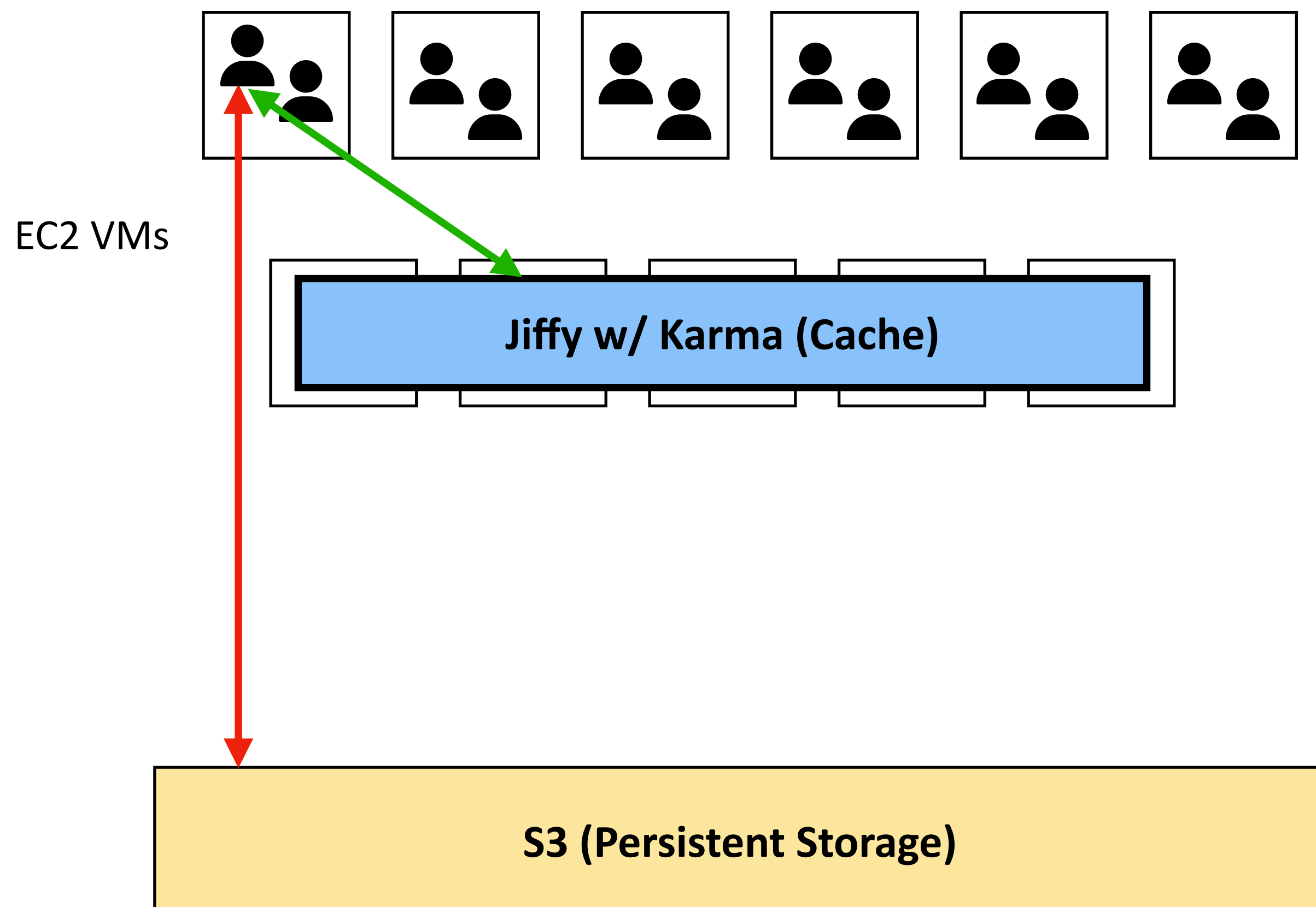
Demands taken from Snowflake dataset

Karma implementation & evaluation

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Evaluated in-memory key-value cache scenario

Experimental Setup



Workload

Dynamic demands -> vary working set size

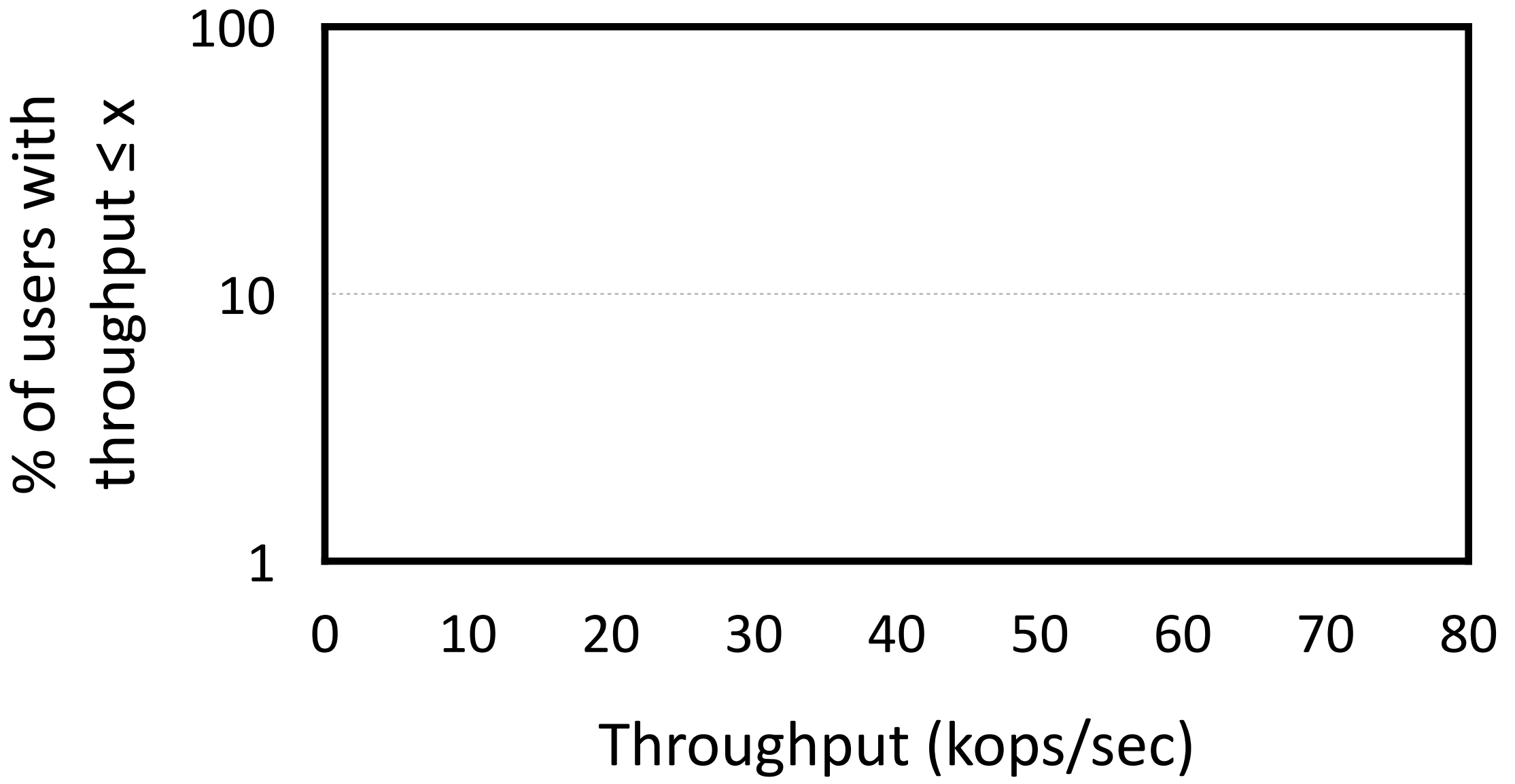
Demands taken from Snowflake dataset

(See paper for details)

Glimpse of Karma evaluation results

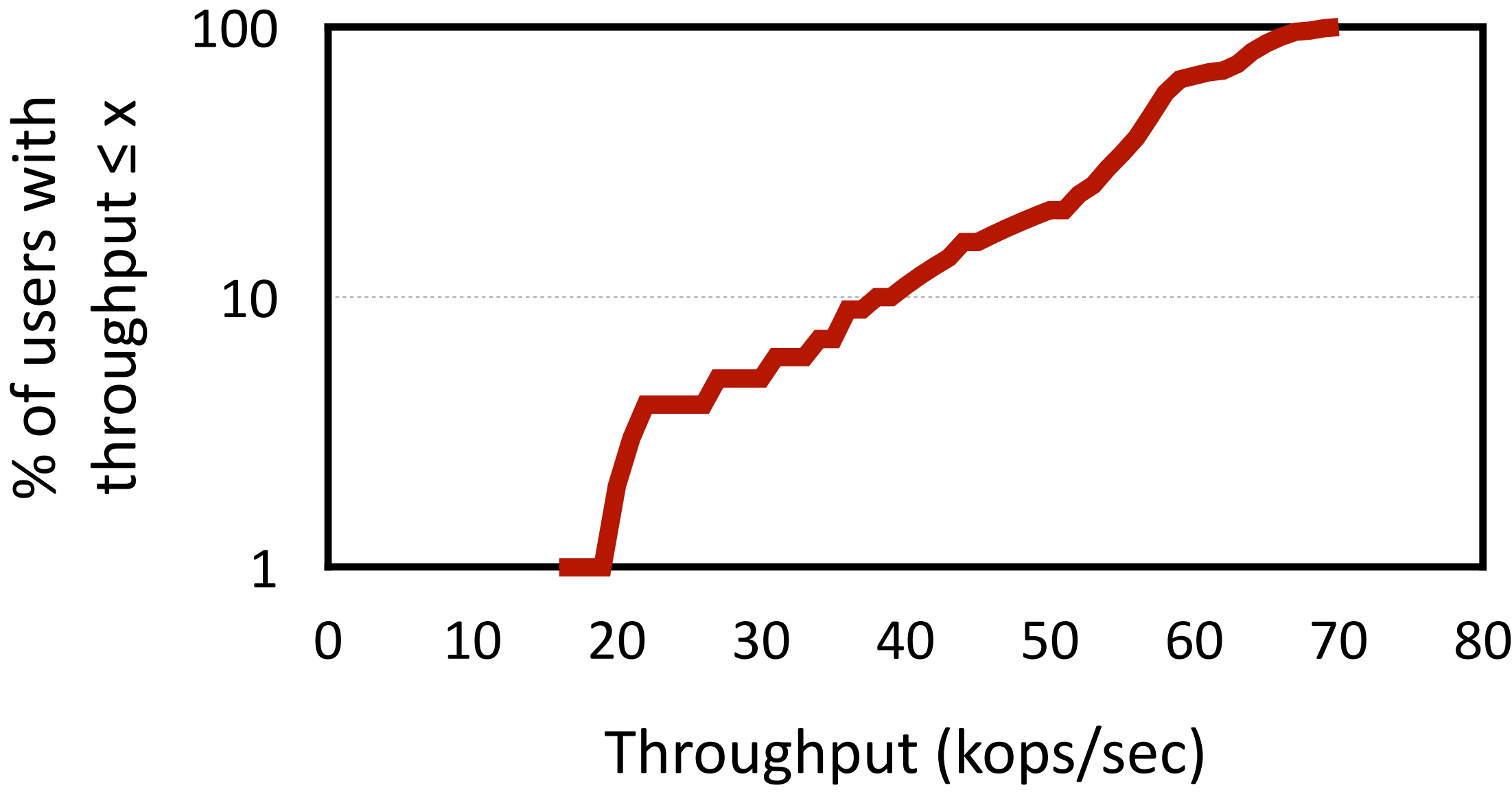
Glimpse of Karma evaluation results

- Max-min fairness (Periodic)
- Karma

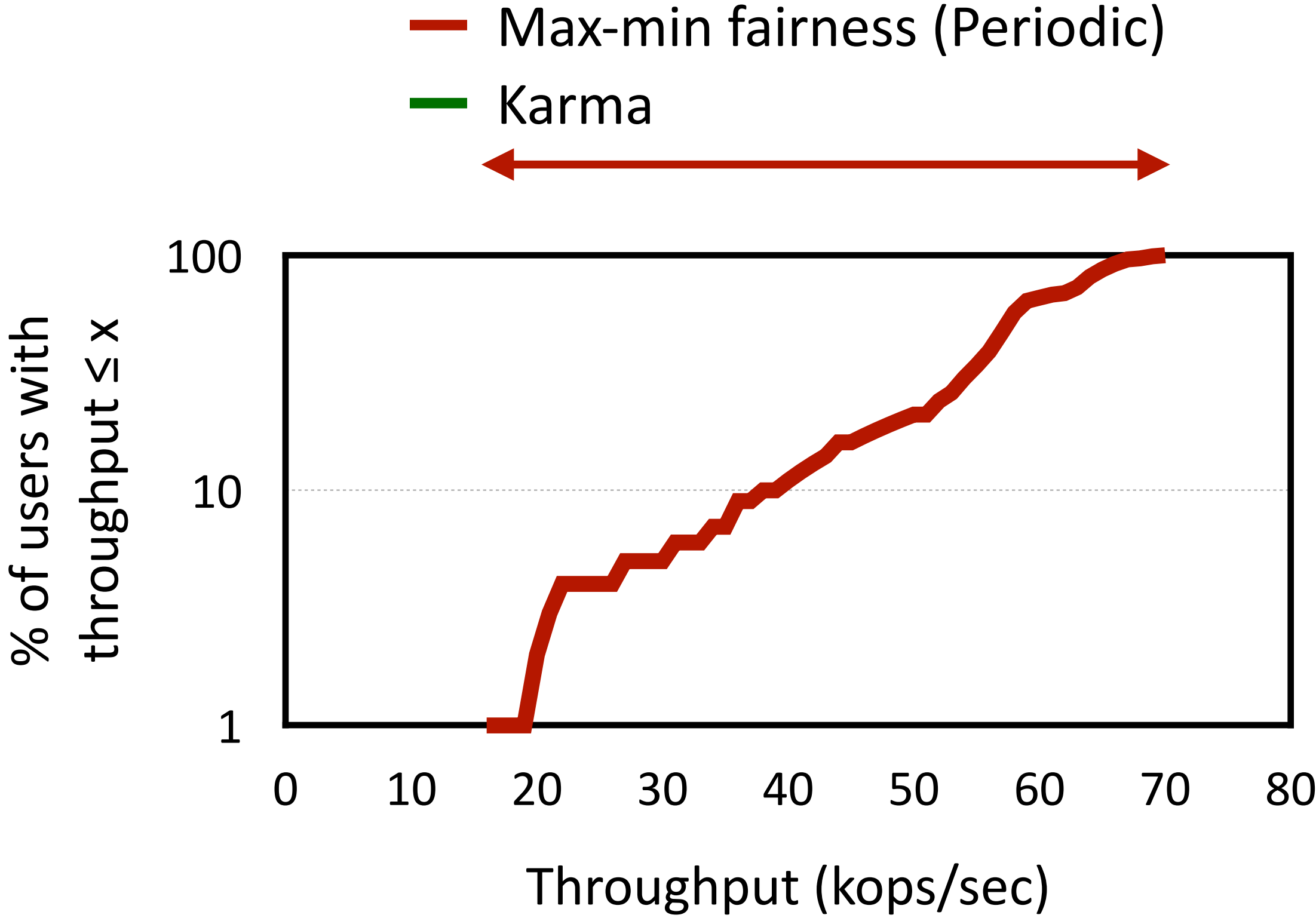


Glimpse of Karma evaluation results

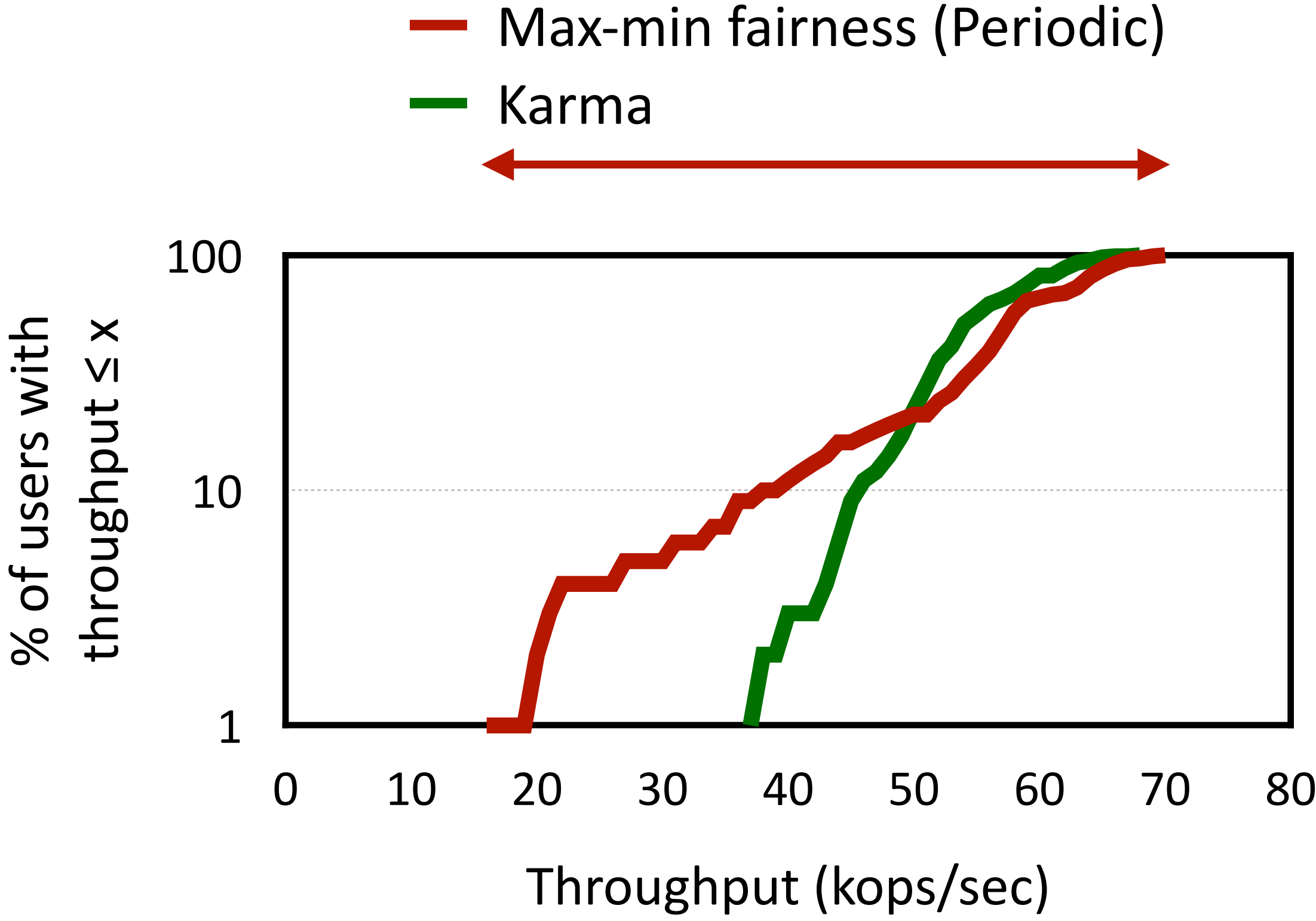
- Max-min fairness (Periodic)
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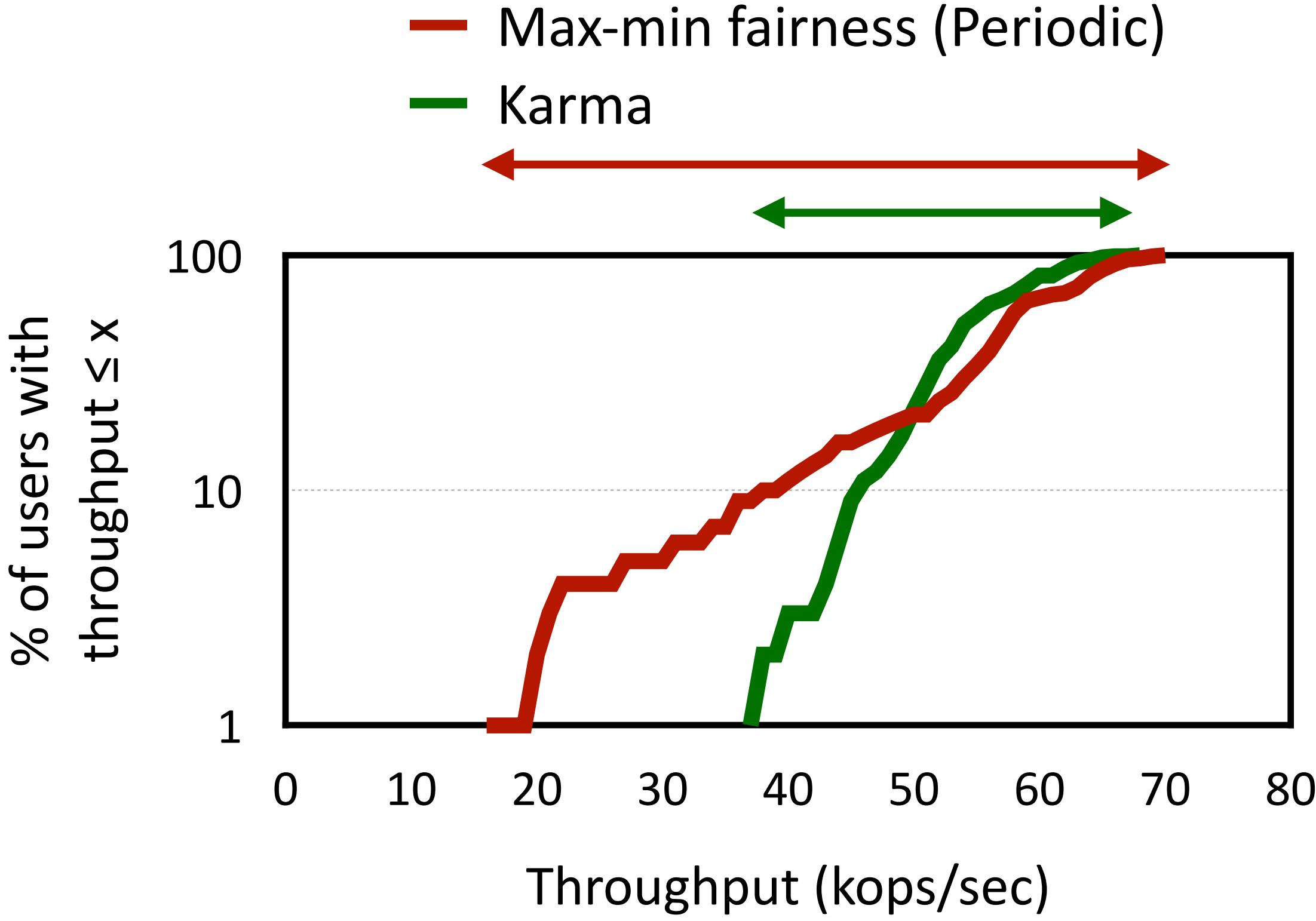
Glimpse of Karma evaluation results



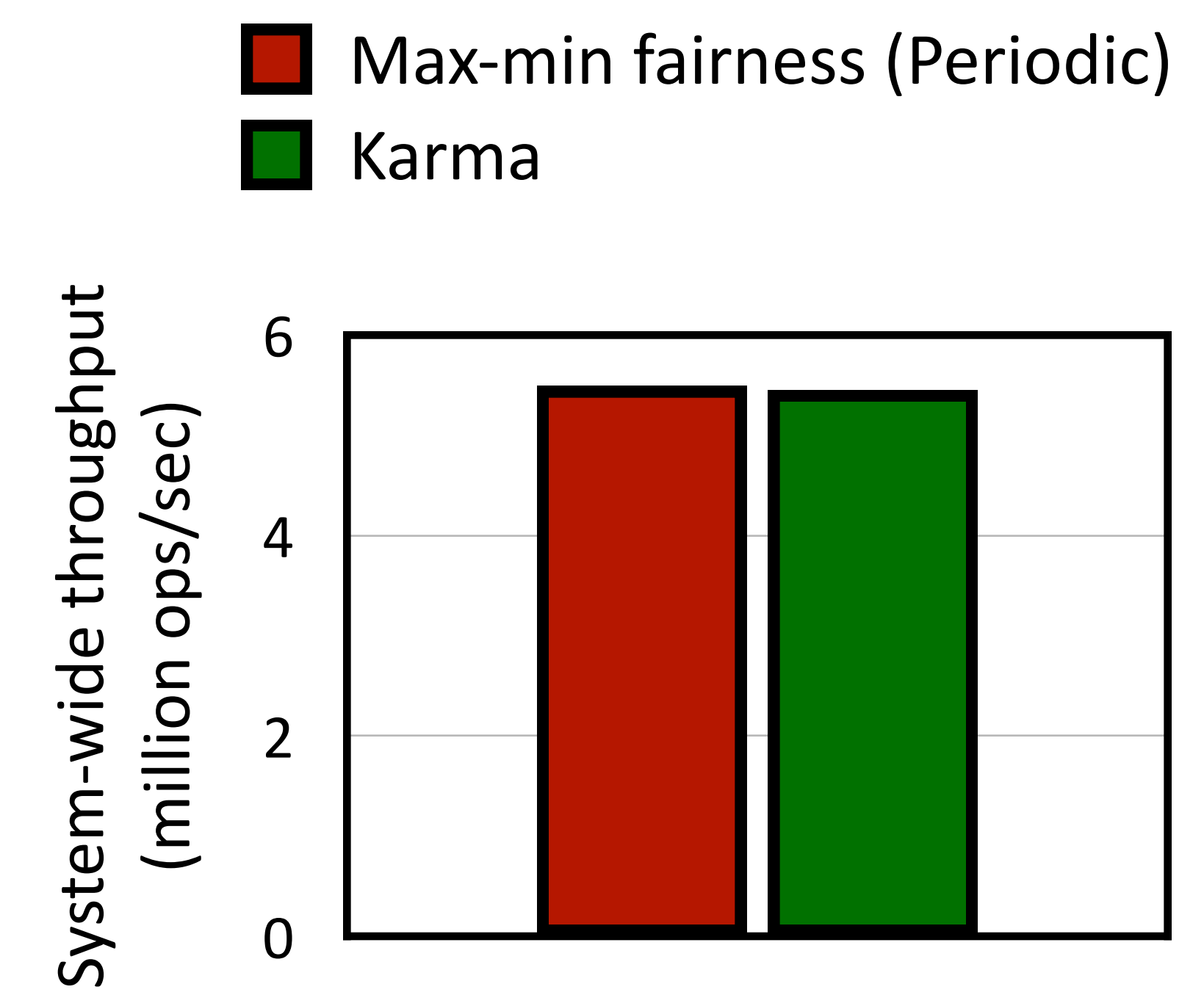
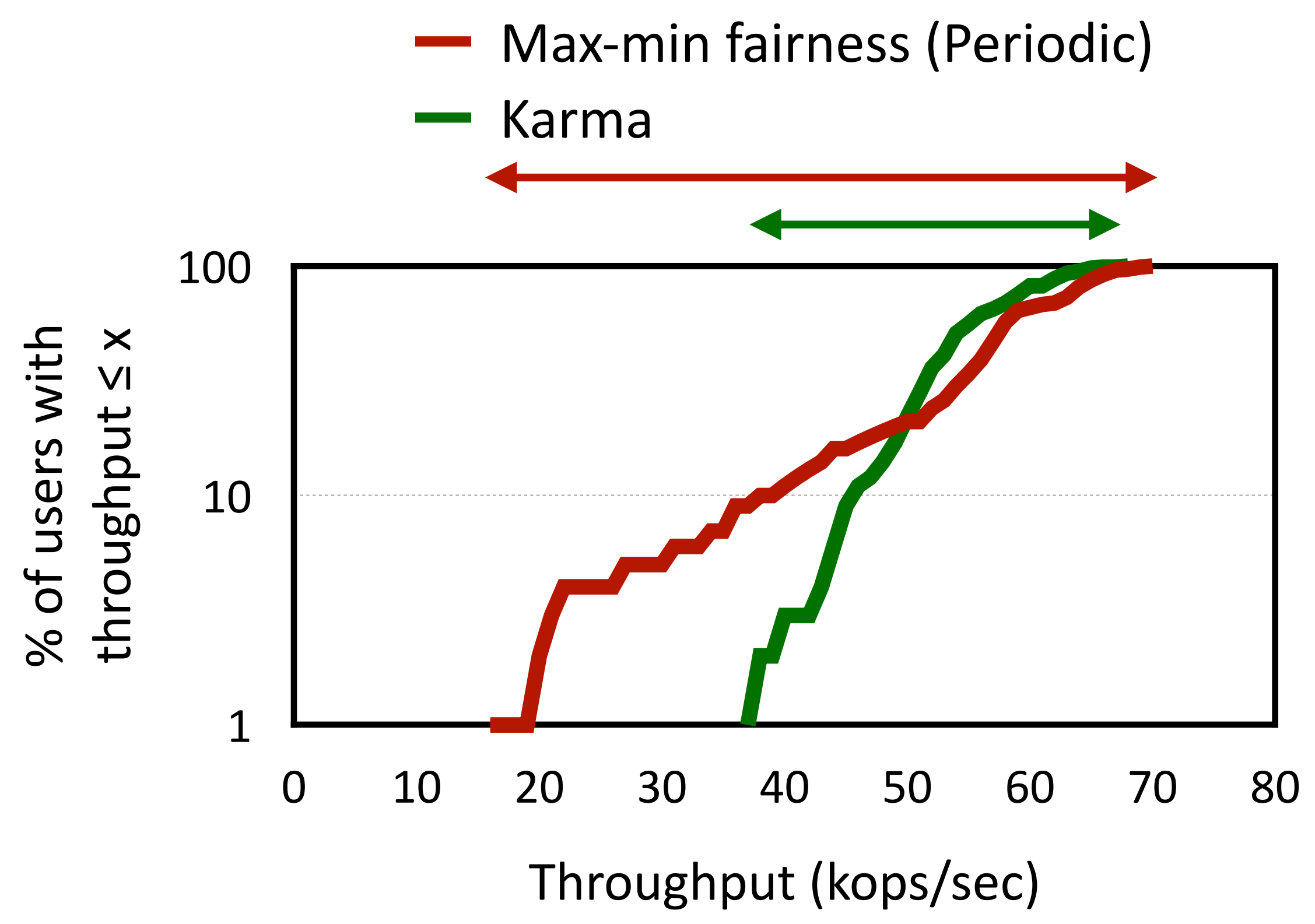
Glimpse of Karma evaluation results



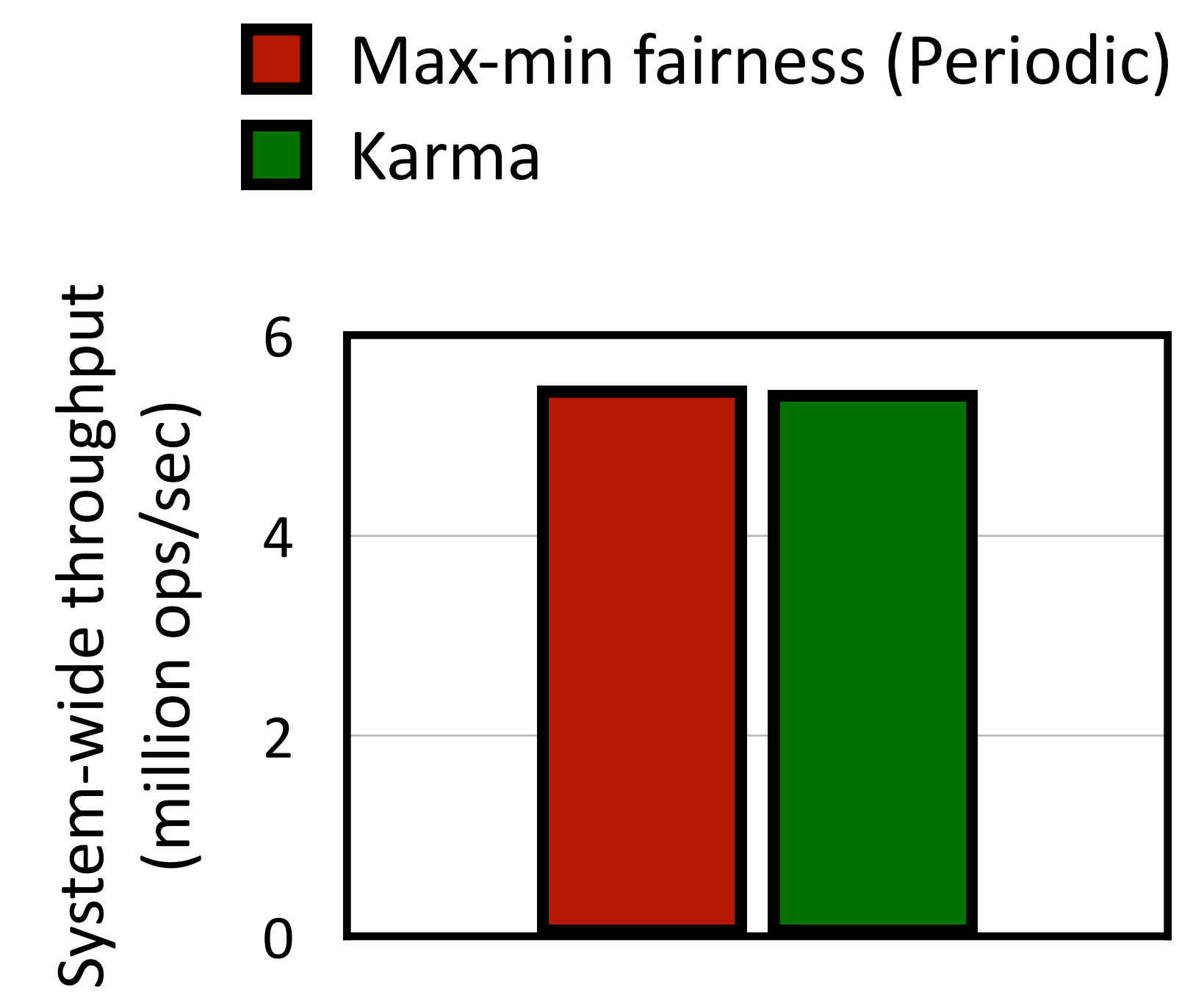
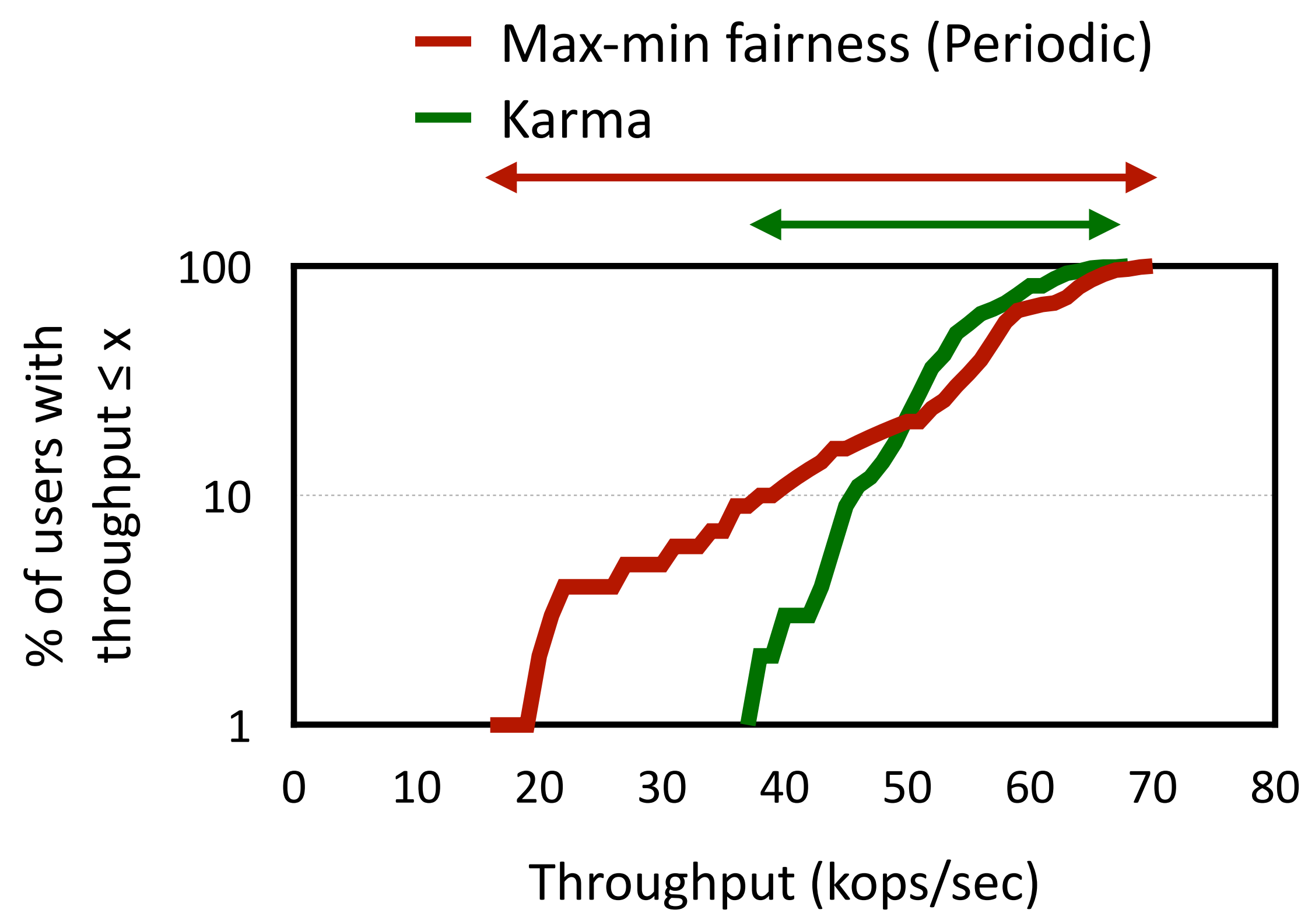
Glimpse of Karma evaluation results



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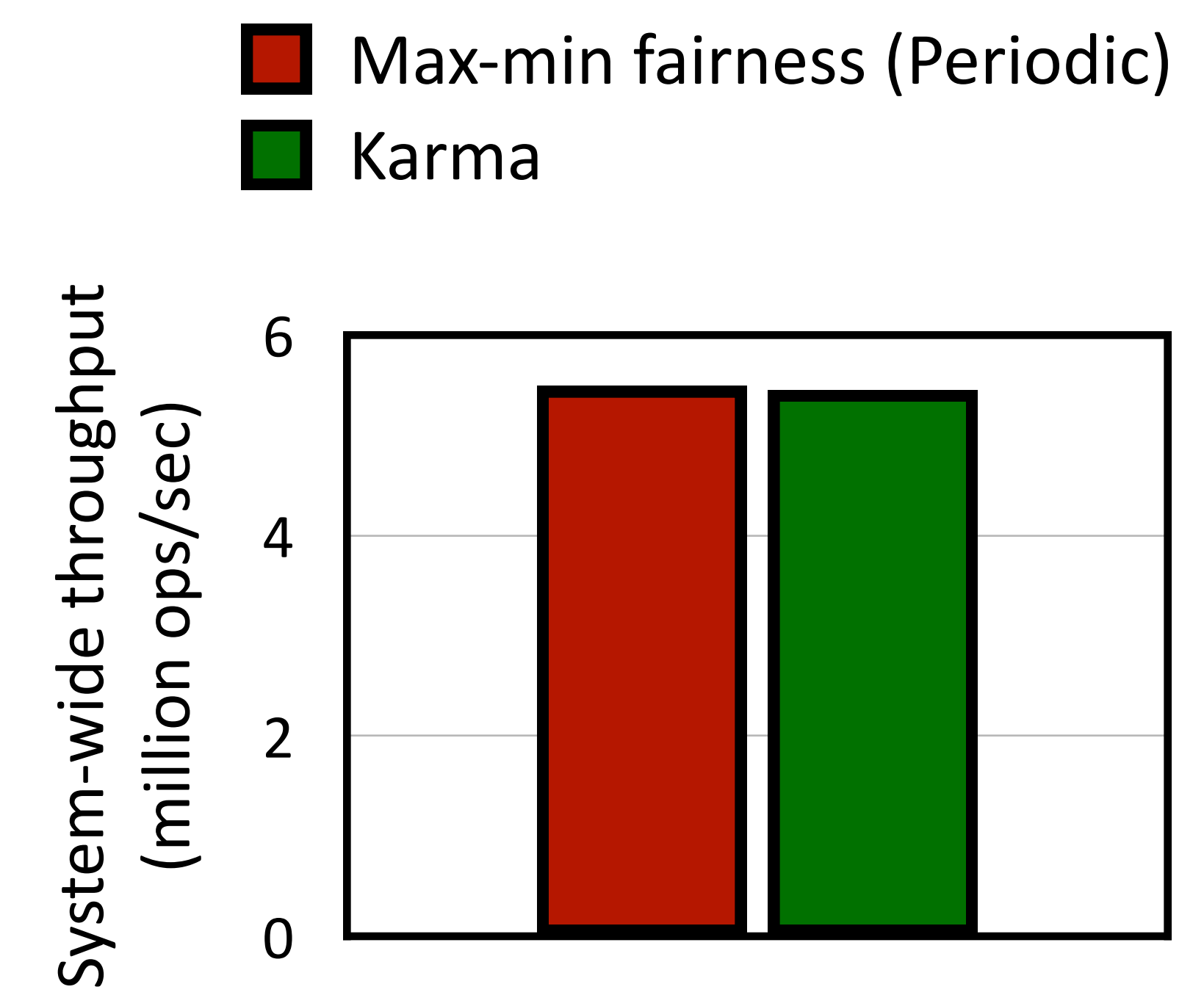
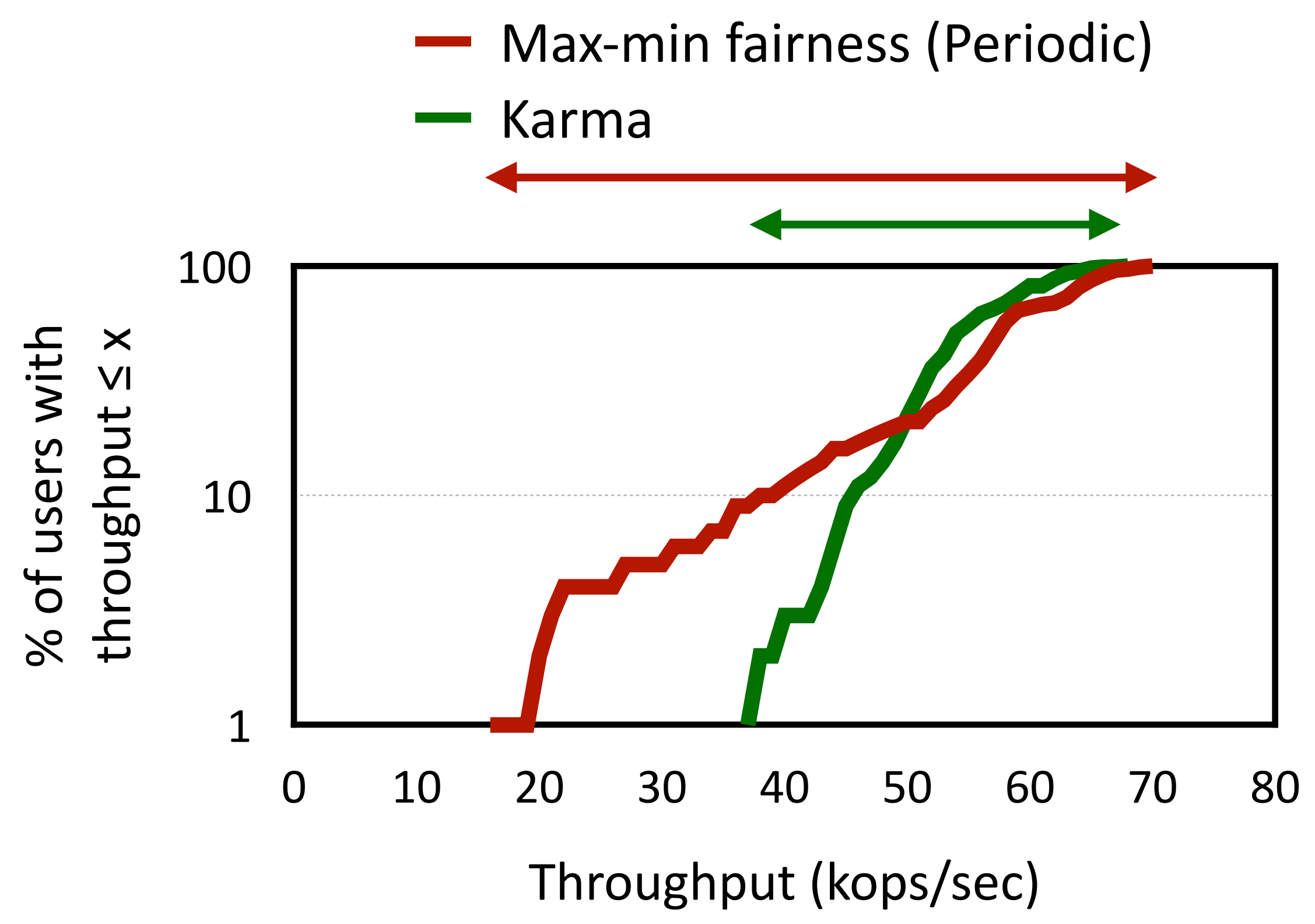


Glimpse of Karma evaluation results



**Karma minimizes disparity across users
(while maintaining high average performance)**

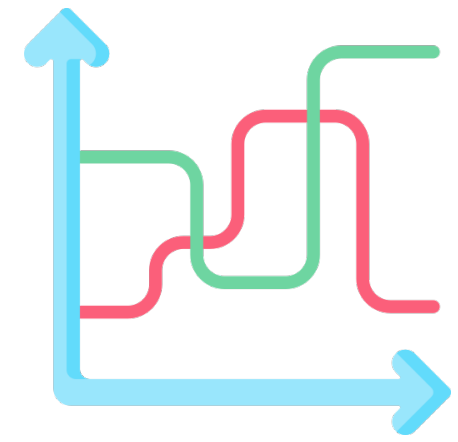
Glimpse of Karma evaluation results



**Karma minimizes disparity across users
(while maintaining high average performance)**

(See paper for more detailed evaluation results)

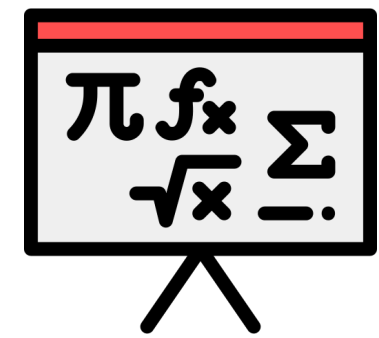
Karma: Revisiting the classical resource allocation problem under dynamic demands



New resource allocation algorithm for dynamic demands



Pareto efficiency



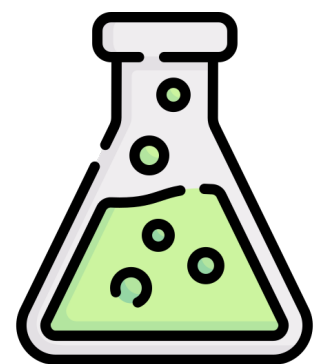
Theoretical guarantees



Strategy-proofness

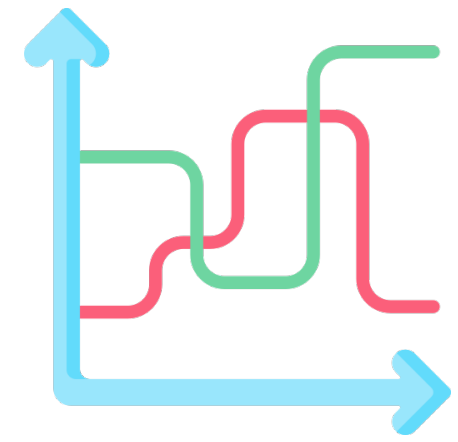


Fairness



Prototype implementation and evaluation

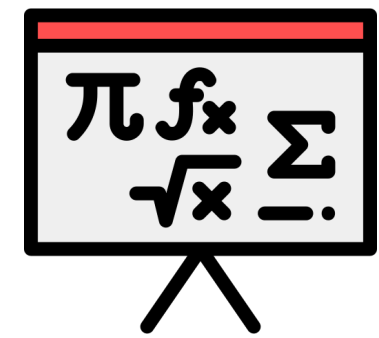
Karma: Revisiting the classical resource allocation problem under dynamic demands



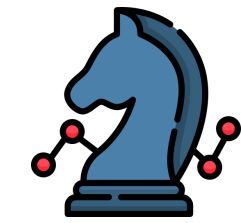
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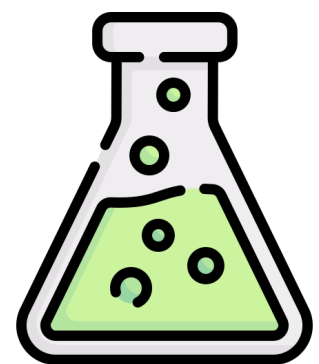
Theoretical guarantees



Strategy-proofness



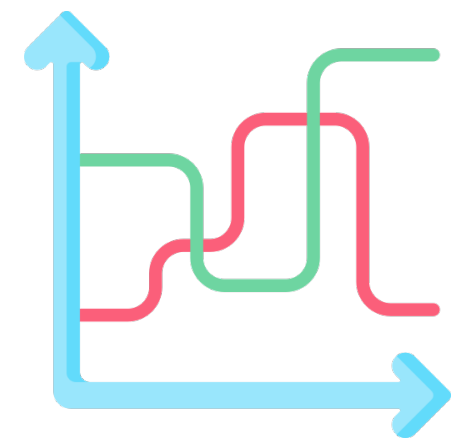
Fairness



Prototype implementation and evaluation

Karma opens many interesting avenues for future research, both in systems and in theory

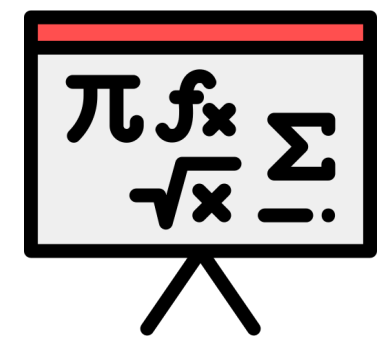
Karma: Revisiting the classical resource allocation problem under dynamic demands



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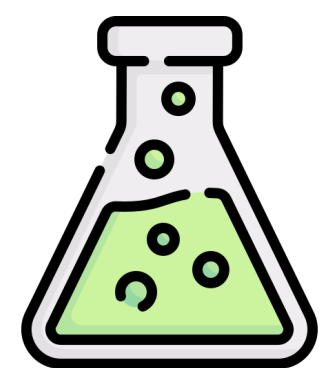
Theoretical guarantees



Strategy-proofness



Fairness



Prototype implementation and evaluation

Karma opens many interesting avenues for future research, both in systems and in theory

<https://github.com/resource-disaggregation/karma>

Midhul Vuppalapati (midhul@cs.cornell.edu)

