zkSaaS

Zero-Knowledge SNARKs as a Service

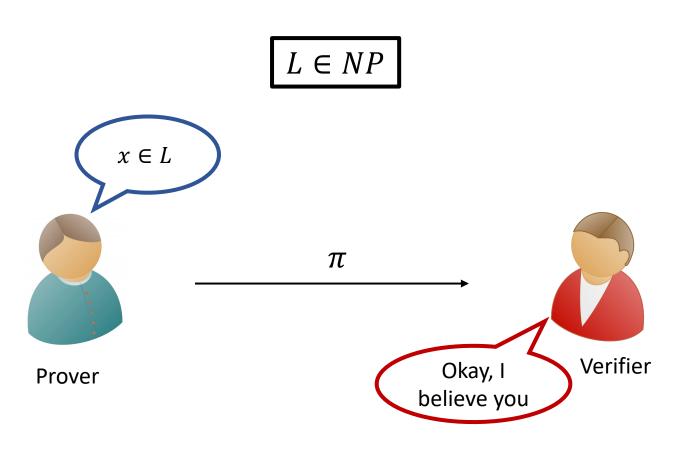
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zk-SNARKs: Zero-Knowledge Succinct Non-Interactive Arguments of Knowledge



zk-SNARKs: Zero-Knowledge Succinct Non-Interactive Arguments of Knowledge

 $L \in NP$ $x \in L$ π Verifier Okay, I Prover believe you Anyone can verify

Zero knowledge

Verifier should not learn the secret witness

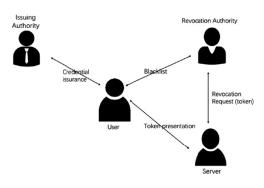
Soundness

Cheating prover cannot give accepting proof if $x \notin L$

Succinctness

Time to verify is smaller than time to compute

zk-SNARKs: Numerous Applications



Anonymous Credentials [Chaum82]



Proving existence of bugs in code [HK20]



Verifiable Inference of Machine Learning [LKKO20]



Verifying authenticity of images in media [NT16]

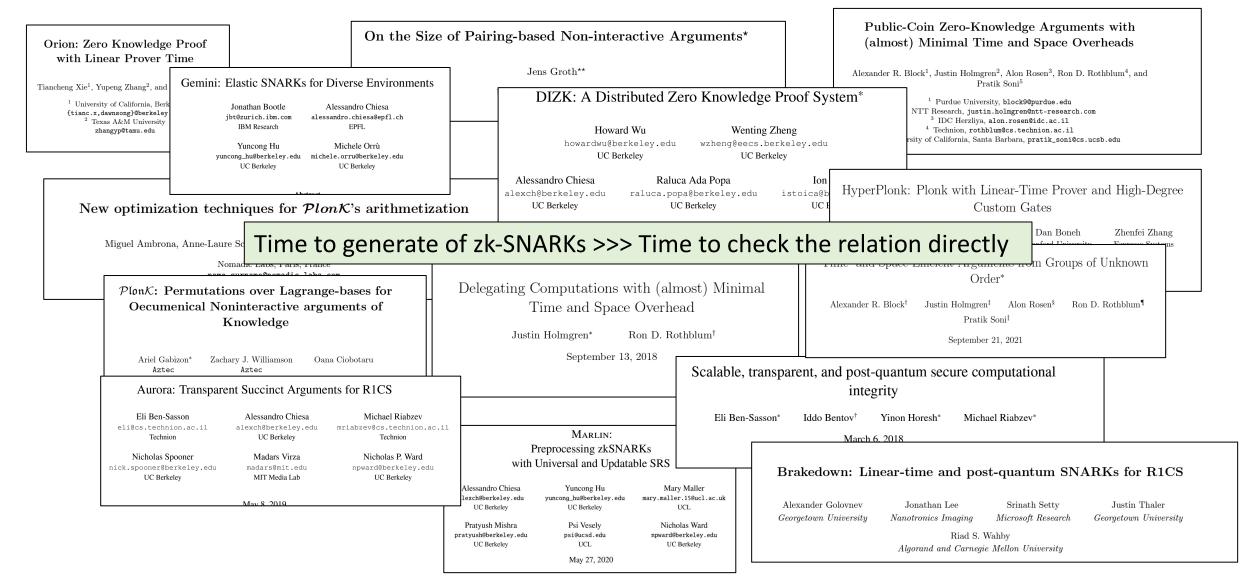


Private Smart Contracts
[BCGMMW20]



Privacy Respecting
Cryptocurrency [BCGGMTV14]

zk-SNARKs: Lots of Work on Improving Efficiency



Gru's Quest to be a Supervillain

Since Gru has a very long list of despicable achievements, computing a zk-SNARK will take a really long time



Prove this in zero-knowledge

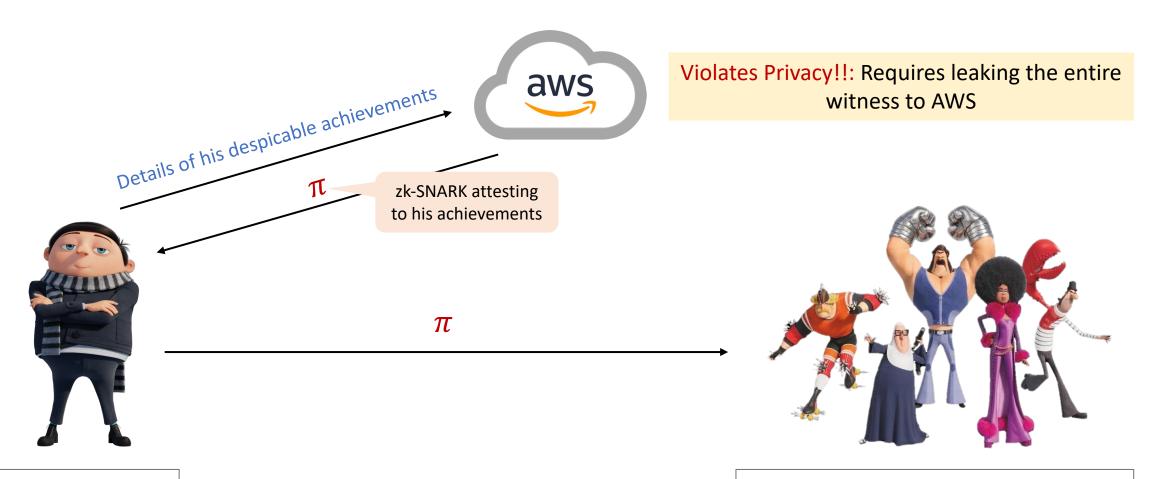
I am a great villain and deserve to be part of Vicious 6



Gru: Rising Villain

Vicious 6: A prolific set of Supervillains

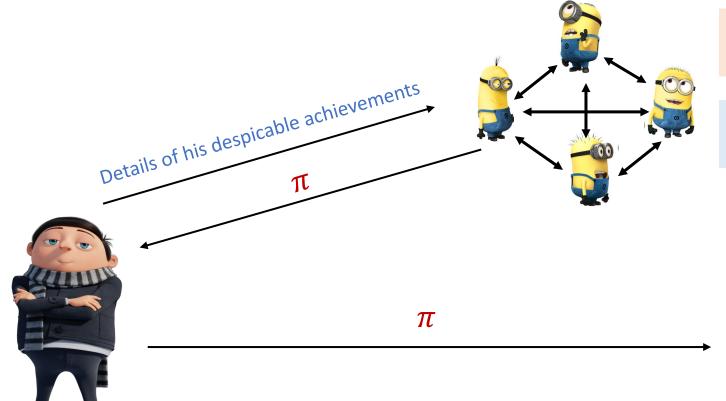
Can Gru Delegate zk-SNARK Computation?



Gru: Rising Villain

Vicious 6: A prolific set of Supervillains

Can Gru Delegate zk-SNARK Computation?



Delegate to a group of minions who run an MPC to compute the zk-SNARK

Each minion only gets a share of the witness



Gru: Rising Villain

Vicious 6: A prolific set of Supervillains

Can Gru Delegate zk-SNARK Computation?



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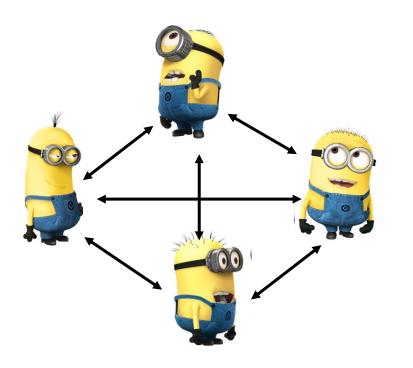
Collaborative zk-SNARKs [OB22]

 π

Vicious 6: A prolific set of Supervillains

Gru: Rising Villair

Collaborative zk-SNARKs [OB22]



Efficient MPC for computing zk-SNARKs

Privacy



Each party does work proportional to a single prover





[WZCAS18] leverage parallelism to distribute work across machines in a compute cluster to get faster proof generation

Not Privacy Preserving

Our Goal

Better utilization of resources of the parties in collaborative zk-SNARKs, for faster proof generation, in a privacy-preserving manner

Our Results: zkSaaS

Framework

For privacy preserving delegation of zk-SNARK computation. Each servers is expected to run for a shorter duration than a single local prover.

Design

Design zkSaaS for Groth16 [Gro16], Marlin [CHMMVW20] and Plonk [GWC19].

Implementation

Implement a prototype of zkSaaS for Groth16, Plonk and get $\approx 22 \times$ speed-up when run with 128 parties for $2^{21} - 2^{25}$ constraints

zkSqqS Framework

Typical zk-SNARKs

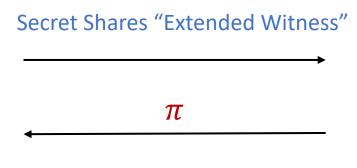
Step 1: Computing Extended Witness

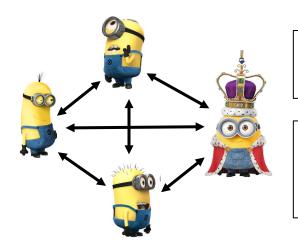
Step 2: Generating Proof

(Cryptographic Operations + Field Operations)

<u>Pre-Processing:</u> each server gets a part of the correlated randomness







Cryptographic Operations get equally divided amongst all servers

Field Operations get equally divided amongst small servers. King does work linear in the number of field operations.

Client computes Step 1

Servers collectively compute Step 2

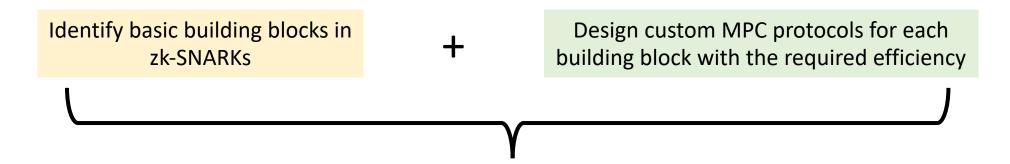
Applicability of zkSaaS

To aid users with small devices

For extremely large computations

Designing zkSaaS

General Template [OB22]



Combine them to get a zkSaaS for the corresponding zk-SNARK

Building Blocks in Groth16, Marlin, Plonk

Multi-Scalar Multiplications (MSM)

$$F(g_1, \alpha_1, \dots, g_m, \alpha_m) = \prod_{i \in [m]} g_i^{\alpha_i}$$

Fast Fourier Transform (FFT)

For converting between coefficient and evaluation representation of polynomials

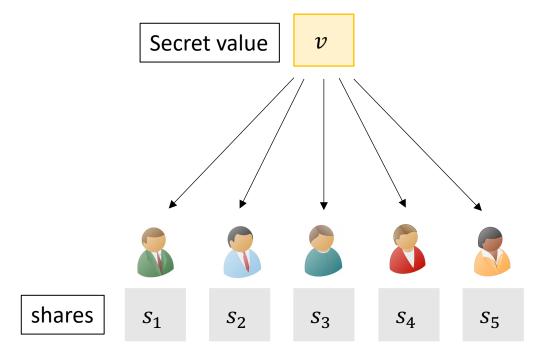
Partial Products

$$F(x_1, \dots, x_m) = \left(\prod_{i \in [j]} x_i\right)_{j \in [m]}$$

Polynomial Multiplication and Division

A combination of addition, multiplication and FFT operations

Packed Secret Sharing (PSS) [FY92]

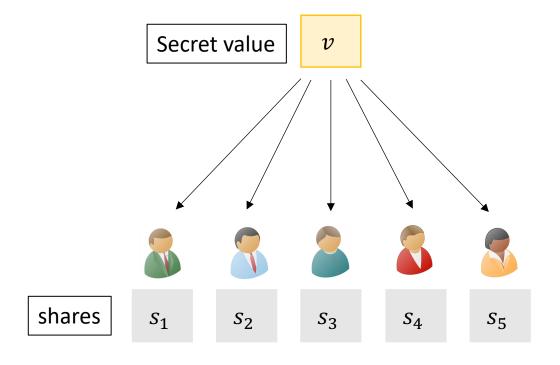


Regular Secret Sharing

1 Value $\rightarrow n$ shares

Corruption threshold: $t < \frac{n}{2}$

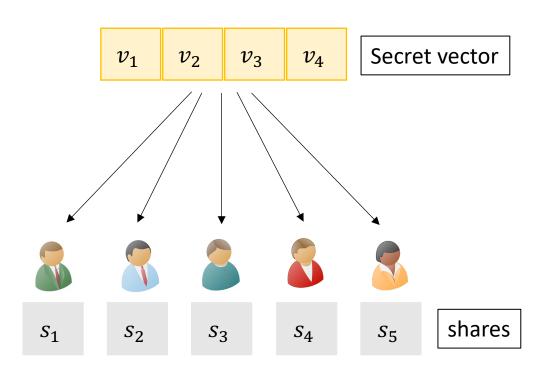
Packed Secret Sharing (PSS) [FY92]



Regular Secret Sharing

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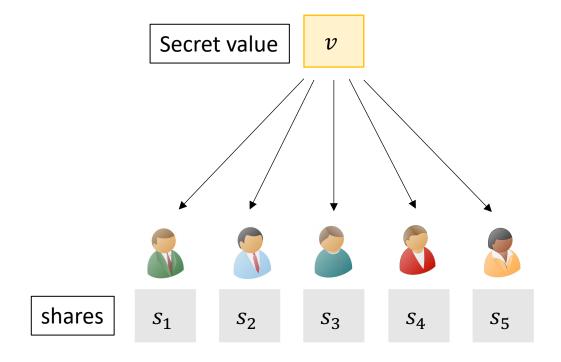
Corruption threshold: $t < \frac{n}{2}$



Packed Secret Sharing

O(n) Values $\rightarrow n$ shares

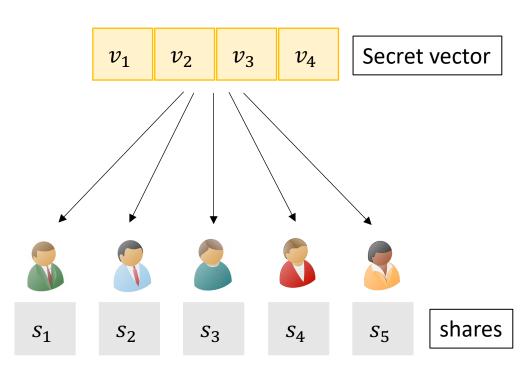
Packed Secret Sharing (PSS) [FY92]



Regular Secret Sharing

1 Value $\rightarrow n$ shares

Corruption threshold: $t < \frac{n}{2}$



Packed Secret Sharing

O(n) Values $\rightarrow n$ shares

Corruption threshold $t < n(\frac{1}{2} - \frac{1}{\varepsilon})$

Experimental Results

zkSaaS for Groth16: Setup

N1 GCP Instances





1vCPU and 4 GB RAM

zkSaaS Servers









96vCPU and 128 GB RAM

1vCPU and 2 GB RAM each

zkSaaS for Groth16

No. of Servers = 128
Packing constant = 32
No. of corrupt servers =31

Local Prover



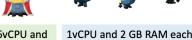
zkSaaS Servers



128 GB RAM









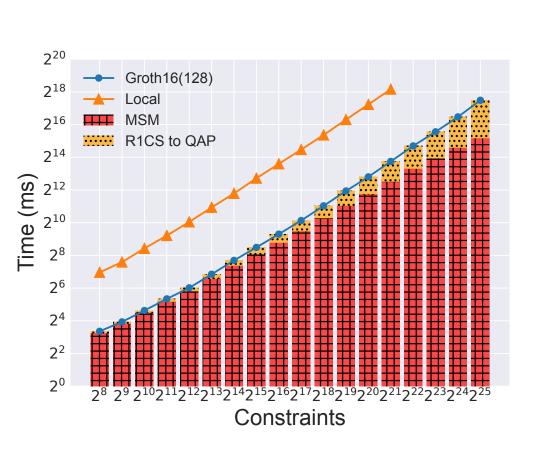
Weak servers can handle 16 times more constraints than consumer machine before running out of memory

Running Time

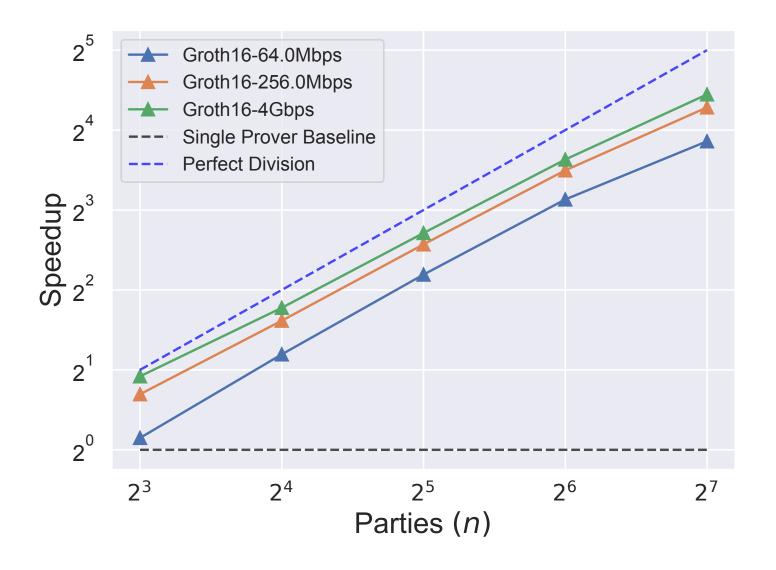
We get ≈ 22× speed-up over consumer machine

Why not 32 times?

- L. FFT doesn't achieve equal division of work
- 2. Sub-optimal use of Pippenger's algorithm for MSMs



zkSaaS for Groth16



Local Prover





No. of Constraints = 2¹⁹
Packing constant = n/4
No. of corrupt servers = n/4

128 GB RAM





Paper Code

Thanks!



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https://aarushigoel.github.io/